

Section 8: CFGs, Relations, DFAs, NFAs, and Minimization

1. CFGs

Construct CFGs for the following languages:

- All binary strings that end in 00.
- All binary strings that contain at least three 1's.
- All binary strings with an equal number of 1's and 0's.

2. Relations

- Draw the transitive-reflexive closure of $\{(1, 2), (2, 3), (3, 4)\}$.
- Suppose that R is reflexive. Prove that $R \subseteq R^2$.
- Consider the relation $S = \{(x, y) : x^2 = y^2\}$ on \mathbb{R} . Prove that S is reflexive, transitive, and symmetric.

3. DFAs, Stage 1

Construct DFAs to recognize each of the following languages. Let $\Sigma = \{0, 1, 2, 3\}$.

- All binary strings.
- All strings whose digits sum to an even number.
- All strings whose digits sum to an odd number.

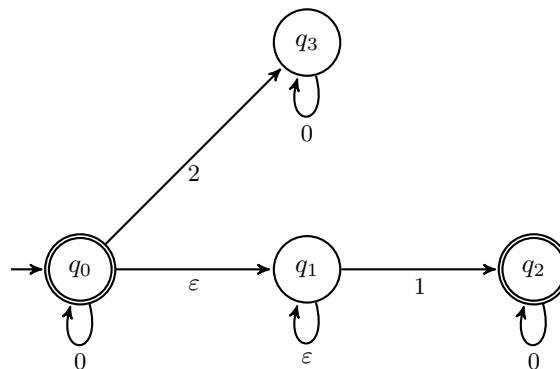
4. DFAs, Stage 2

Construct DFAs to recognize each of the following languages. Let $\Sigma = \{0, 1\}$.

- All strings which do not contain the substring 101.
- All strings containing at least two 0's and at most one 1.
- All strings containing an even number of 1's and an odd number of 0's and not containing the substring 10.

5. NFAs

- What language does the following NFA accept?



- Create an NFA for the language “all binary strings that have a 1 as one of the last three digits”.

6. Minimization

Minimize the following DFA:

