1. CFGs
Construct CFGs for the following languages:

(a) All binary strings that end in 00.

(b) All binary strings that contain at least three 1’s.

(c) All binary strings with an equal number of 1’s and 0’s.

2. Relations
(a) Draw the transitive-reflexive closure of \{(1, 2), (2, 3), (3, 4)\}.

(b) Suppose that \(R\) is reflexive. Prove that \(R \subseteq R^2\).

(c) Consider the relation \(R = \{(x, y) : x = y + 1\}\) on \(\mathbb{N}\). Is \(R\) reflexive? Transitive? Symmetric? Anti-symmetric?

(d) Consider the relation \(S = \{(x, y) : x^2 = y^2\}\) on \(\mathbb{R}\). Prove that \(S\) is reflexive, transitive, and symmetric.

3. DFAs, Stage 1
Construct DFAs to recognize each of the following languages. Let \(\Sigma = \{0, 1, 2, 3\}\).

(a) All binary strings.

(b) All strings whose digits sum to an even number.
4. DFAs, Stage 2
Construct DFAs to recognize each of the following languages. Let \( \Sigma = \{0, 1\} \).

(a) All strings which do not contain the substring 101.

(b) All strings containing at least two 0’s and at most one 1.

(c) All strings containing an even number of 1’s and an odd number of 0’s and not containing the substring 10.