







Since we have epsilon transitions to each, it's the union machine!



## Three ways of thinking about NFAs

- Outside observer: Is there a path labeled by x from the start state to some final state?
- Perfect guesser: The NFA has input x and whenever there is a choice of what to do it magically guesses a good one (if one exists)
- Parallel exploration: The NFA computation runs all possible computations on x step-by-step at the same time in parallel





- -a is a regular expression for any  $a \in \Sigma$
- If **A** and **B** are regular expressions then so are:













## NFAs and DFAs

Every DFA is an NFA

- DFAs have requirements that NFAs don't have

Can NFAs recognize more languages? No!

**Theorem:** For every NFA there is a DFA that recognizes exactly the same language

## Conversion of NFAs to a DFAs

- Proof Idea:
  - The DFA keeps track of ALL the states that the part of the input string read so far can reach in the NFA
  - There will be one state in the DFA for each subset of states of the NFA that can be reached by some string





















