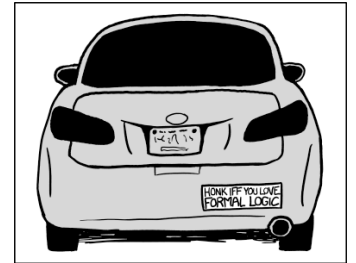


CSE 311

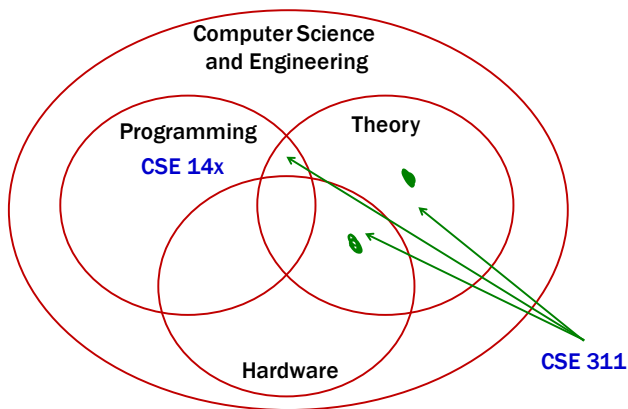
Foundations of Computing I

CSE 311: Foundations of Computing I

Lecture 1: Propositional Logic



Some Perspective



About the Course

We will study the theory needed for CSE:

Logic:

How can we describe ideas *precisely*?

Formal Proofs:

How can we be *positive* we're correct?

Number Theory:

How do we keep data *secure*?

Relations/Relational Algebra:

How do we store information?

Finite State Machines:

How do we design hardware and software?

Turing Machines:

Are there problems computers *can't* solve?

About the Course

It's about perspective!

- Example: Sudoku
 - Given *one*, solve it by hand
 - Given *most*, solve them with a program
 - Given *any*, solve it with computer science
- Tools for reasoning about difficult problems
- Tools for communicating ideas, methods, objectives...
- Tools for automating difficult problems
- Fundamental structures for computer science

This is NOT a programming course!

Administrivia

Instructor: Adam Blank

Teaching Assistants:

John Armstrong	Ollin Boer Bohan
Phillip Huang	Jasper Huginin
Johan Michalove	Michael Lee
Emerson Matson	Evan McCarty
Melissa Medsker	Matthew Rockett
Logan Weber	
Jefferson Van Wagenen	

Homework: *(Yes!)*
Due WED at start of class
 Write up individually

Section:
 Thursdays

(Optional) Books:
 Rosen, Velleman, MIT Book
 Don't buy new copies!

Grading (roughly):
 50% Homework
 20% Midterm
 30% Final Exam

All Course Information @ cs.uw.edu/311

Logic: The Language of Reasoning

Why not use English?

- Turn right here...

Does "right" mean the direction or now?

- Buffalo buffalo Buffalo buffalo buffalo buffalo Buffalo buffalo

This means "Bison from Buffalo, that bison from Buffalo bully, themselves bully bison from Buffalo."

- We saw her duck

Does "duck" mean the animal or crouch down?

"Language of Reasoning" like Java or English

- Words, sentences, paragraphs, arguments...
- Today is about **words** and **sentences**

Why Learn A New Language?

Logic, as the "language of reasoning", will help us...

- Be more **precise**
- Be more **concise**
- Figure out what a statement means more **quickly**

Propositions

A **proposition** is a statement that

- has a truth value, and
- is "well-formed"

and hello wpt.

Are These Propositions?

$$2 + 2 = 5$$

This is a proposition. It's okay for propositions to be false.

The home page renders correctly in IE.

This is a proposition. It's okay for propositions to be false.

Turn in your homework on Wednesday.

This is a "command" which means it doesn't have a truth value.

This statement is false.

This statement does not have a truth value! (If it's true, it's false, and vice versa.)

Akjsdf!

This is not a proposition because it's gibberish.

Who are you?

This is a question which means it doesn't have a truth value.

Every positive even integer can be written as the sum of two primes.

This is a proposition. We don't know if it's true or false, but we know it's one of them!

Propositions

A **proposition** is a statement that

- has a truth value, and
- is "well-formed"

We need a way of talking about *arbitrary* ideas...

Propositional Variables: p, q, r, s, \dots

Truth Values:

- **T** for true
- **F** for false

A Proposition

"Roger is an orange elephant who has toenails if he has tusks, and has toenails, tusks, or both."

We'd like to *understand* what this proposition means.

This is where logic comes in. There are pieces that appear multiple times in the phrase (e.g., "Roger has tusks").

These are called **atomic propositions**. Let's list them:

RElephant: "Roger is an orange elephant"

RTusks: "Roger has tusks"

RToenails: "Roger has toenails"

Putting Them Together

“Roger is an orange elephant who has toenails if he has tusks, and has toenails, tusks, or both.”

RElephant: “Roger is an orange elephant”

RTusks: “Roger has tusks”

RToenails: “Roger has toenails”

Now, we put these together to make the sentence:

RElephant **and** (RToenails **if** RTusks) **and** (RToenails **or** RTusks **or** (RToenails **and** RTusks))

This is the general idea, but now, let's define our *formal language*.

Logical Connectives

Negation (not) $\neg p$

Conjunction (and) $p \wedge q$

Disjunction (or) $p \vee q$

Exclusive Or $p \oplus q$

Implication $p \rightarrow q$

Biconditional $p \leftrightarrow q$

RElephant:
“Roger is an orange elephant”
RTusks:
“Roger has tusks”
RToenails:
“Roger has toenails”

“Roger is an orange elephant who has toenails if he has tusks, and has toenails, tusks, or both.”

RElephant **and** (RToenails **if** RTusks) **and** (RToenails **or** RTusks **or** (RToenails **and** RTusks))

$RElephant \wedge (RToenails \text{ if } RTusks) \wedge (RToenails \vee RTusks \vee (RToenails \wedge RTusks))$

Some Truth Tables

p	$\neg p$
T	F
F	T

p	q	$p \wedge q$
T	T	T
T	F	F
F	T	F
F	F	F

p	q	$p \vee q$
T	T	T
T	F	T
F	T	T
F	F	F

p	q	$p \oplus q$
T	T	F
T	F	T
F	T	T
F	F	F

Implication

“If it's raining, then I have my umbrella”

It's useful to think of implications as promises. That is “Did I lie?”

p	q	$p \rightarrow q$
T	T	T
T	F	F
F	T	T
F	F	T

	It's raining	It's not raining
I have my umbrella	No	No
I do not have my umbrella	Yes	No

The only lie is when:

(a) It's raining AND

(b) I don't have my umbrella

Implication

“If it's raining, then I have my umbrella”

p	q	$p \rightarrow q$
T	T	T
T	F	F
F	T	T
F	F	T

Are these true?

$2 + 2 = 4 \rightarrow \text{earth is a planet}$

The fact that these are unrelated doesn't make the statement false! “ $2 + 2 = 4$ ” is true; “earth is a planet” is true. $T \rightarrow T$ is true. So, the statement is true.

$2 + 2 = 5 \rightarrow 26 \text{ is prime}$

Again, these statements may or may not be related. “ $2 + 2 = 5$ ” is false; so, the implication is true. (Whether 26 is prime or not is irrelevant).

Implication is not a causal relationship!