

**CSE  
31F**

# Foundations of Computing I

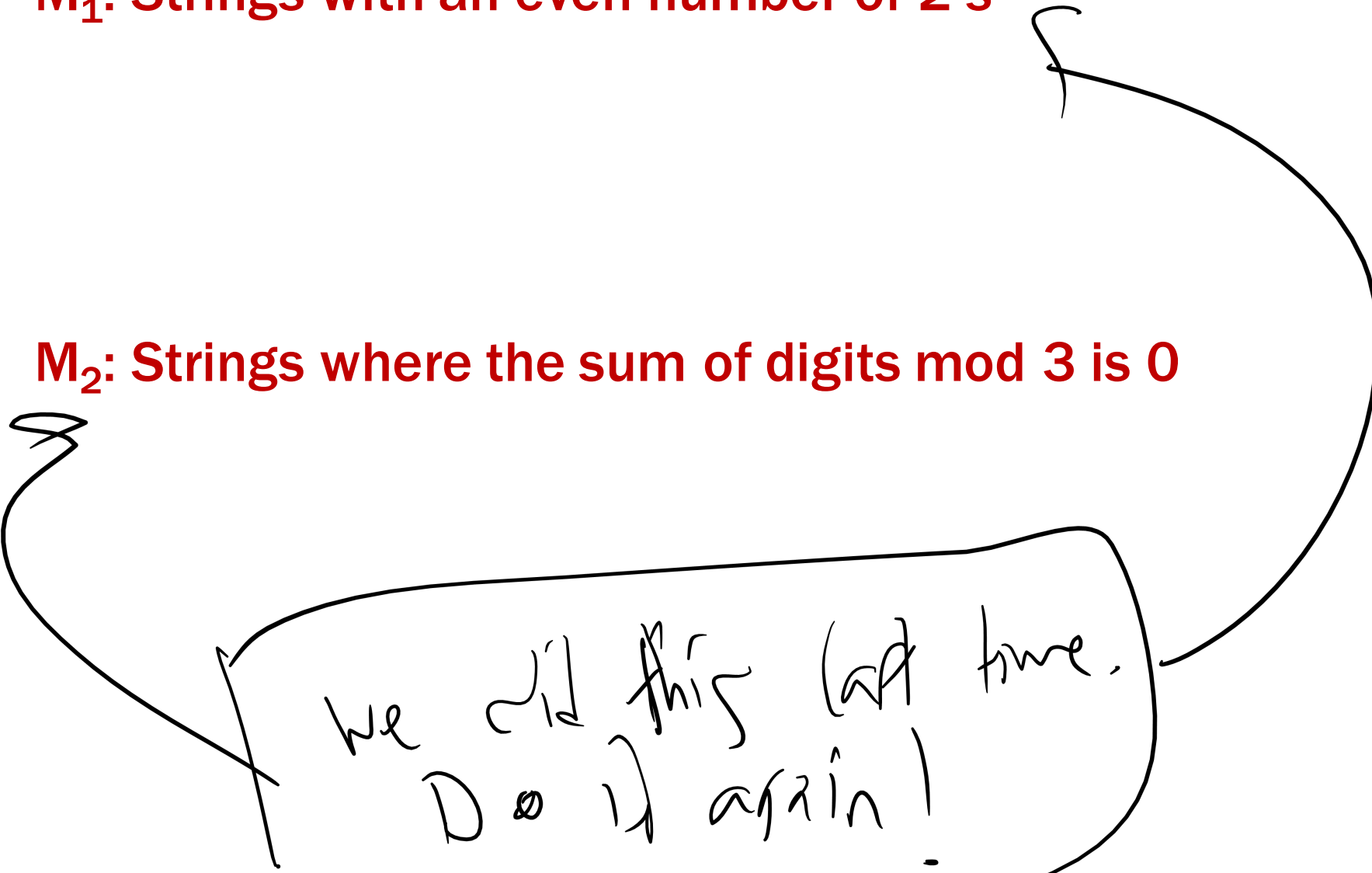
\* All slides are a combined effort between  
previous instructors of the course

# Strings over $\{0, 1, 2\}^*$

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$M_1$ : Strings with an even number of 2's

$M_2$ : Strings where the sum of digits mod 3 is 0

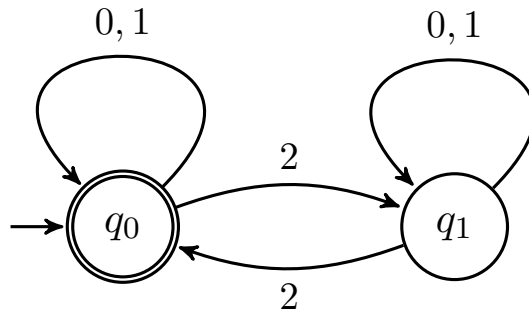


We did this last time.  
Do it again!

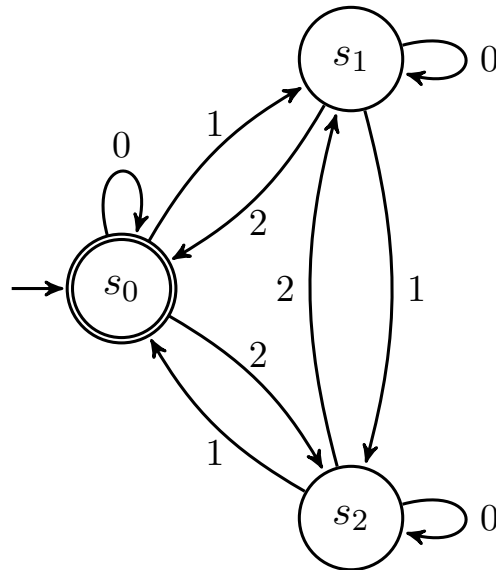
# Strings over $\{0, 1, 2\}^*$

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**$M_1$ : Strings with an even number of 2's**

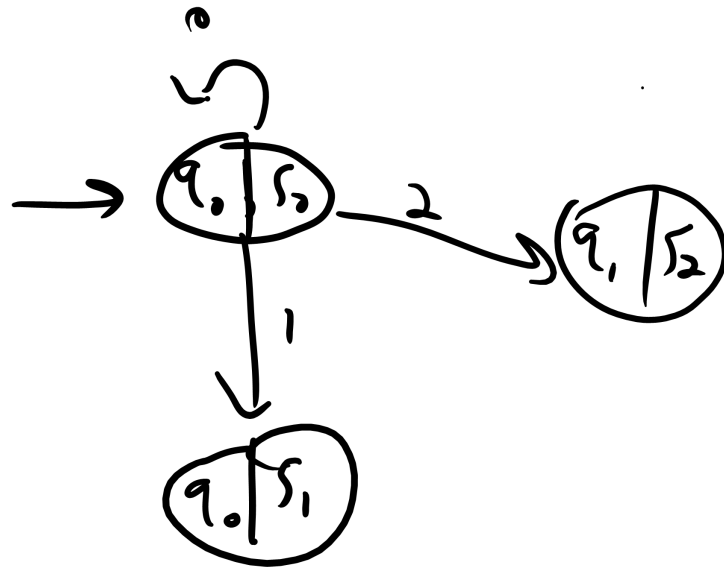
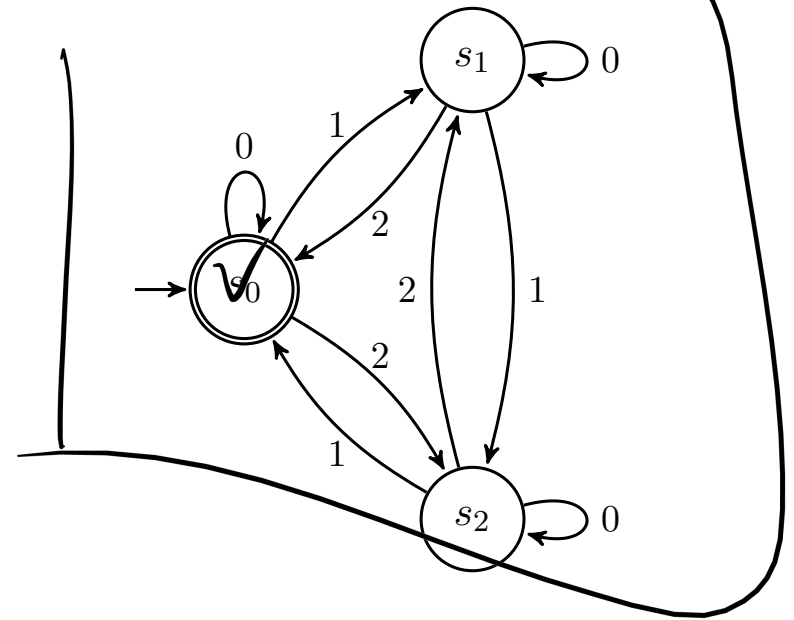
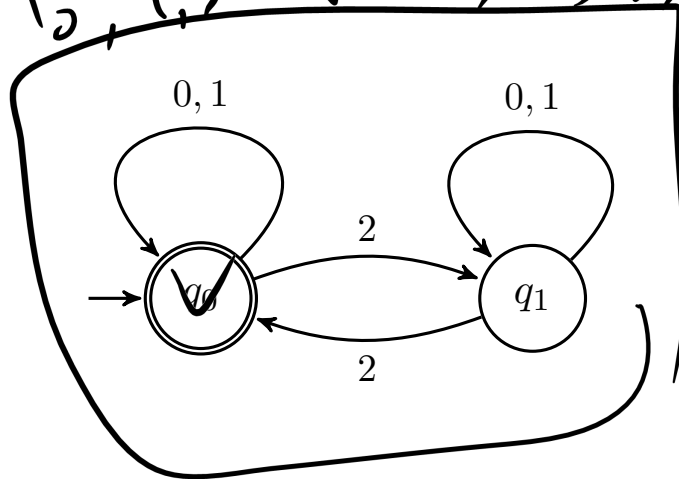


**$M_2$ : Strings where the sum of digits mod 3 is 0**



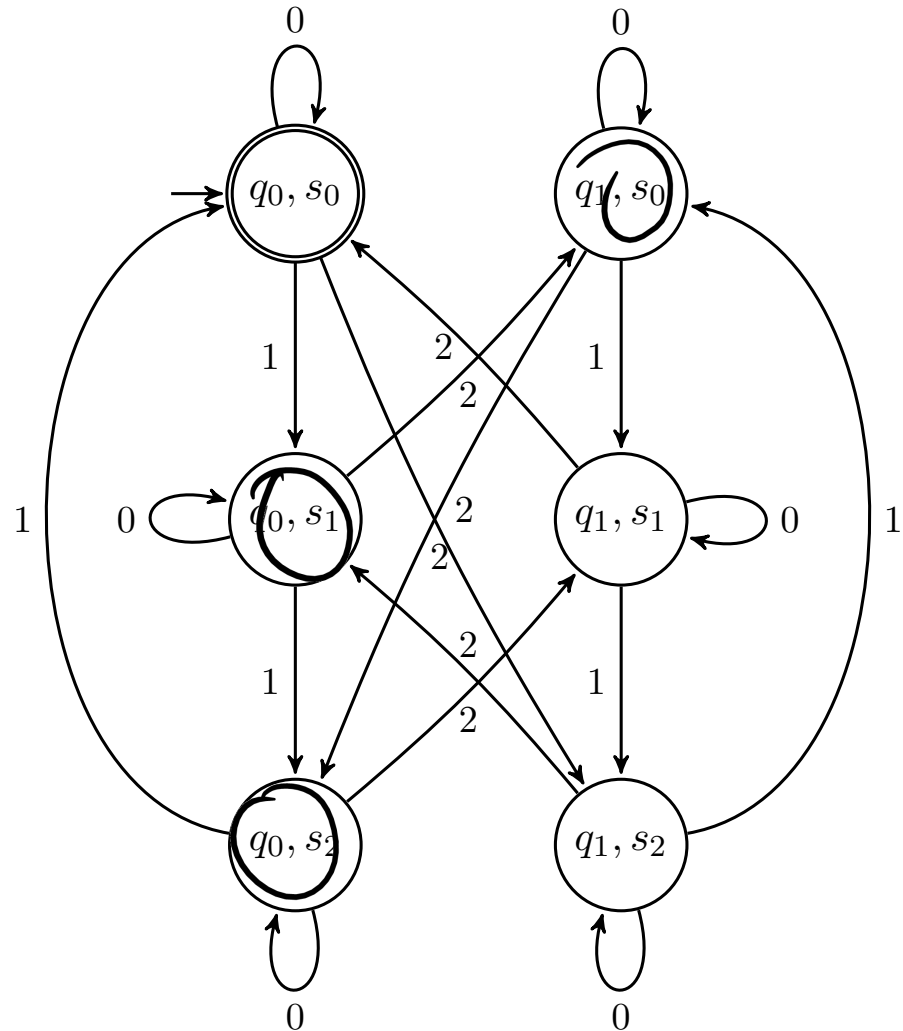
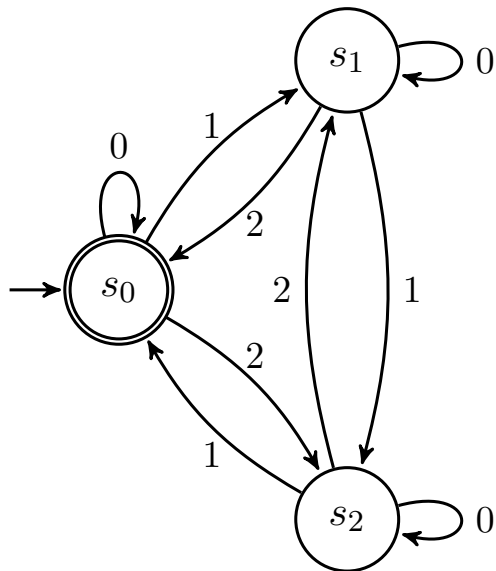
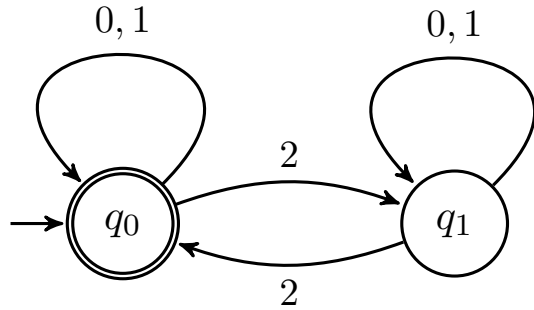
# Strings with an even number of 2's AND a mod 3 sum of 0

$\{q_0, q_1\} \times \{s_0, s_1, s_2\}$



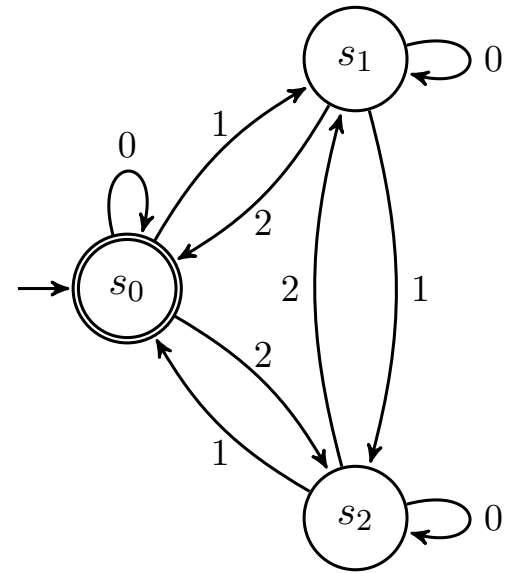
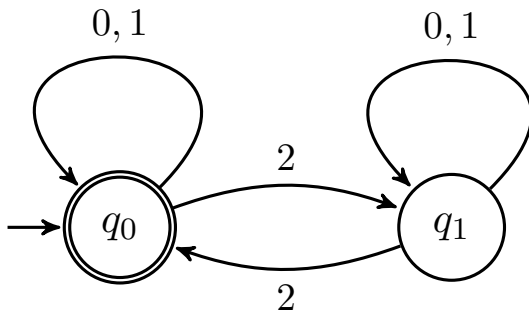
# Strings with an even number of 2's <sup>OR</sup> ~~AND~~ a mod 3 sum of 0

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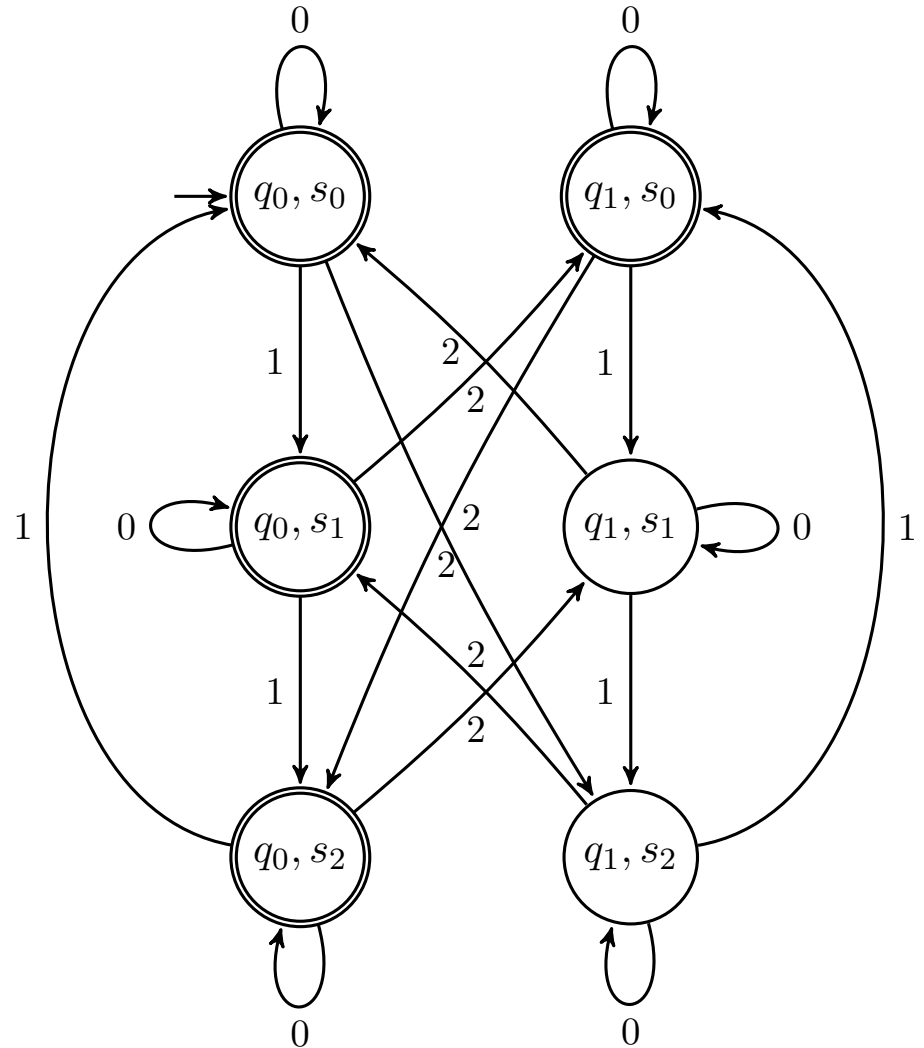
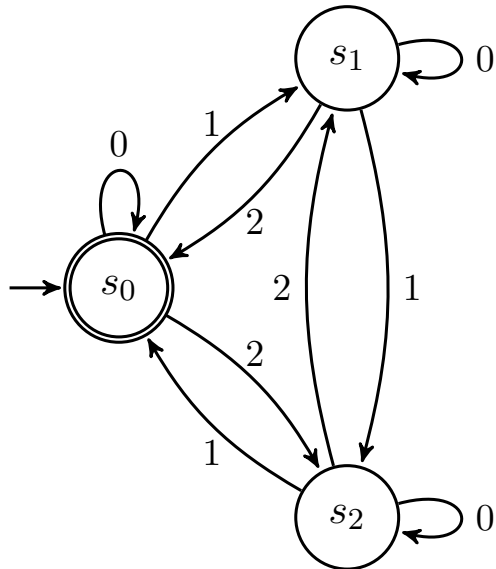
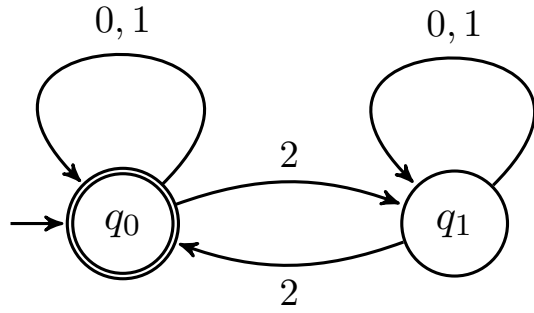
# Strings with an even number of 2's OR a mod 3 sum of 0

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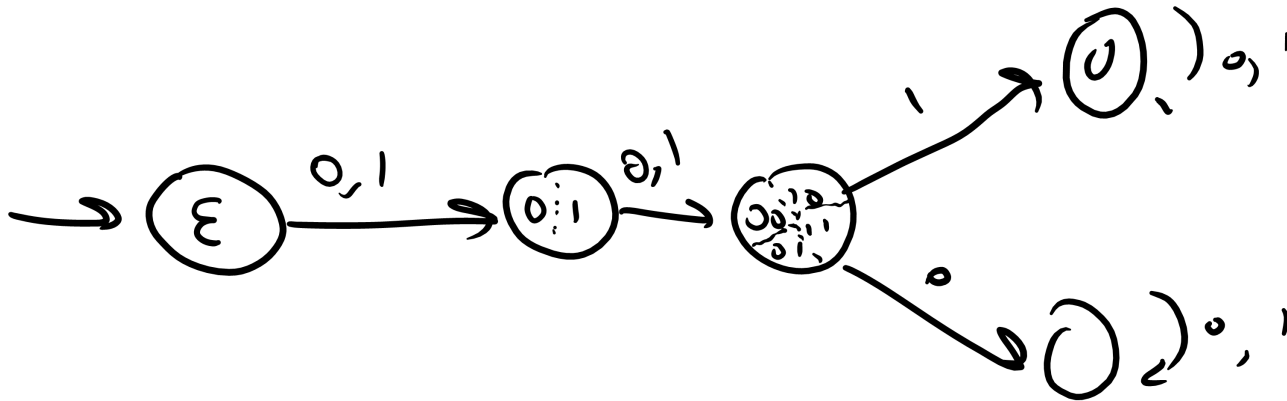
# Strings with an even number of 2's OR a mod 3 sum of 0

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FSM that accepts binary strings with a 1 three positions from the start

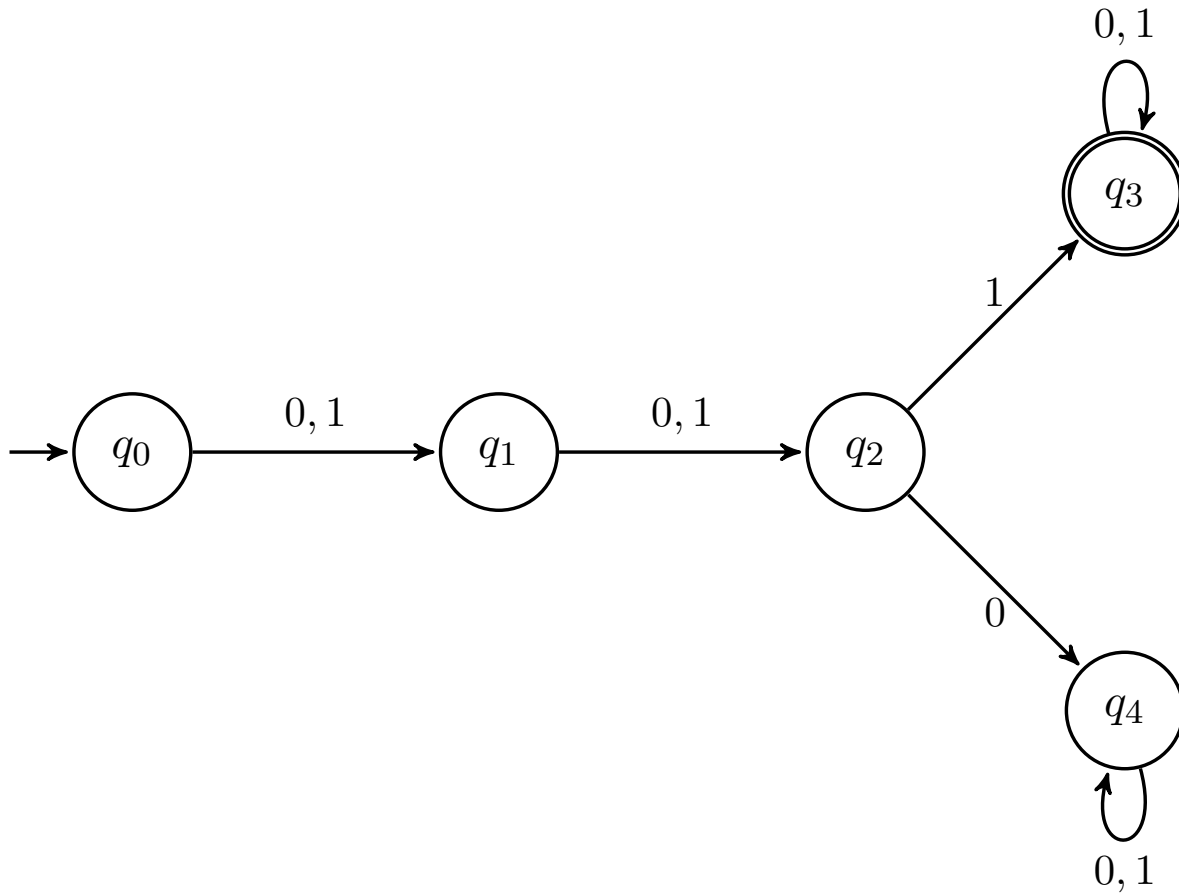
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# FSM that accepts binary strings with a 1 three positions from the start

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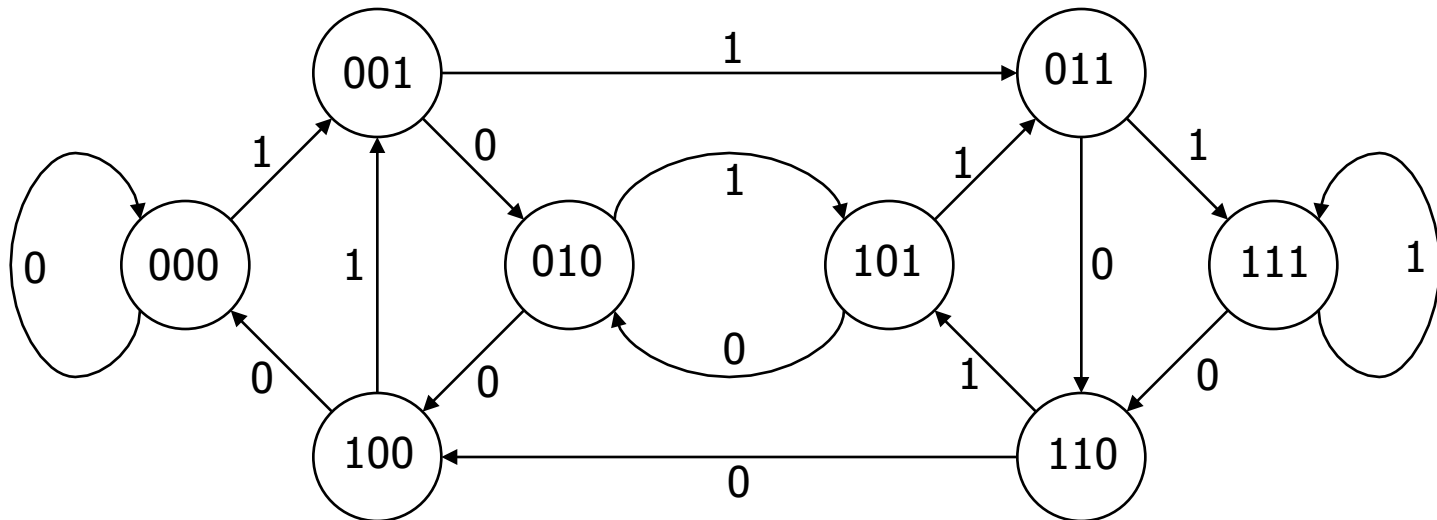
# 3 bit shift register

“Remember the last three bits”

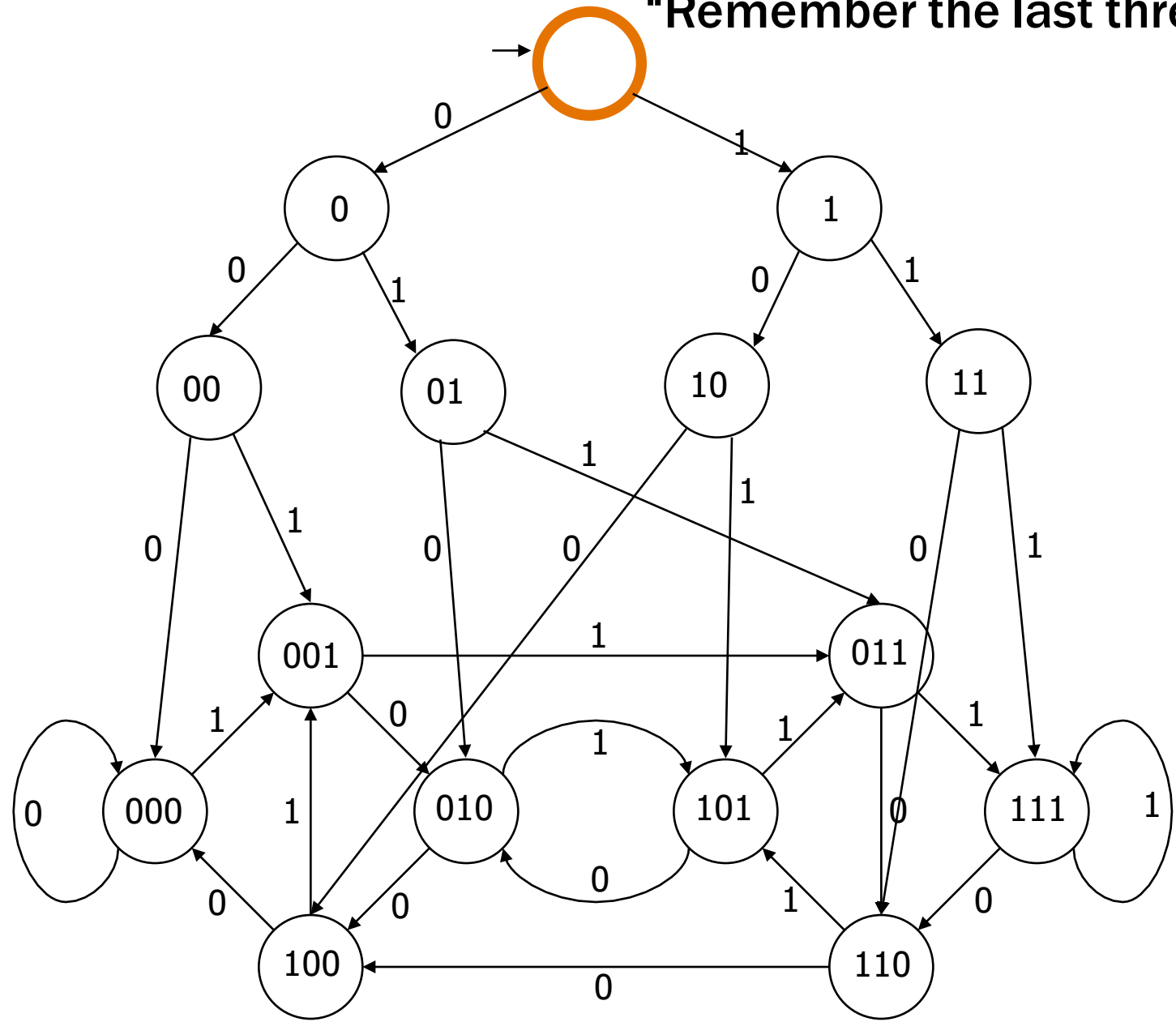
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# 3 bit shift register

“Remember the last three bits”

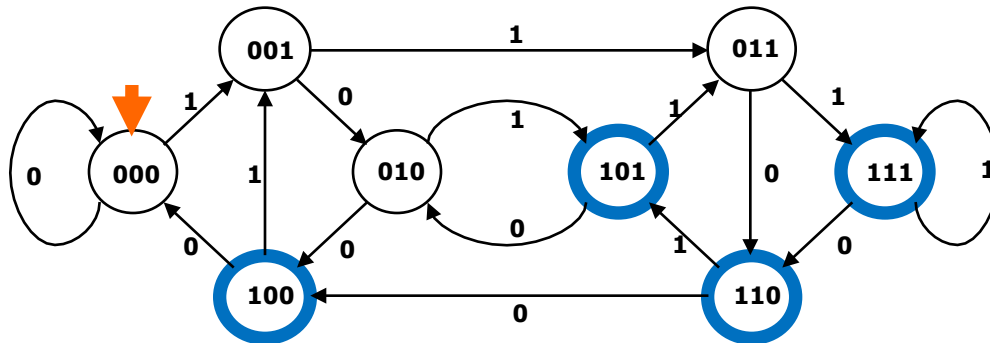
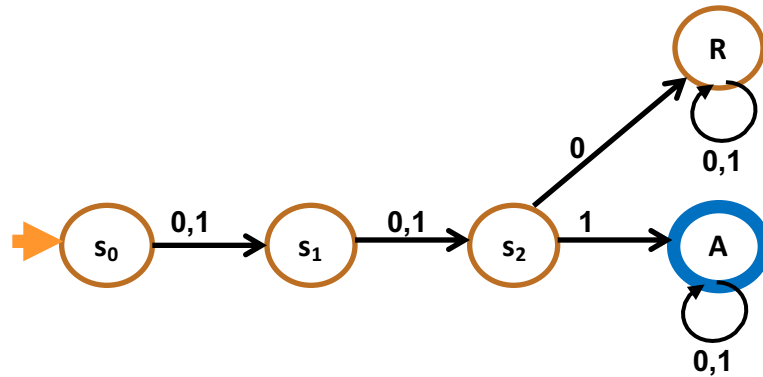


“Remember the last three bits”



# The beginning versus the end

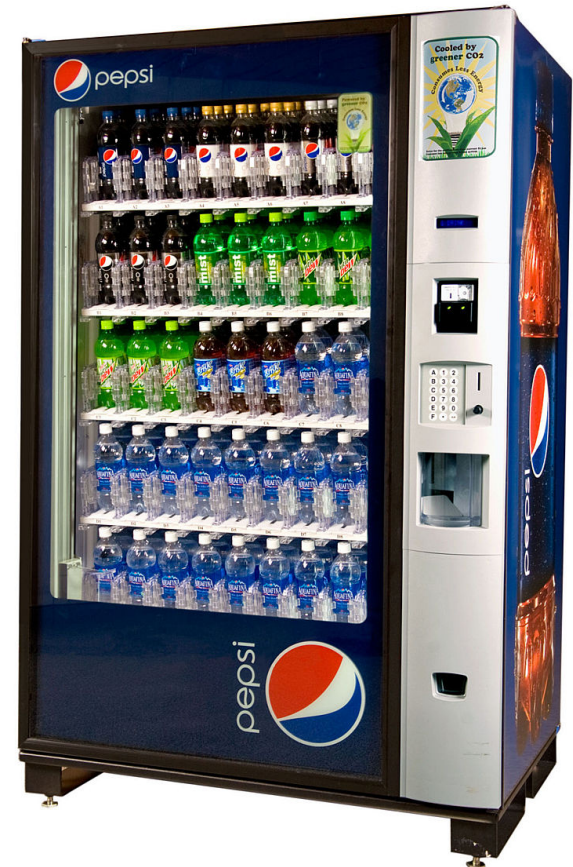
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# CSE 311: Foundations of Computing

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## Lecture 22: Finite State Machines with Output

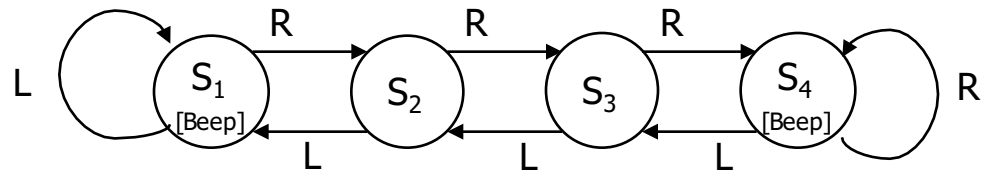


# State Machines with Output

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State	Input		Output
	L	R	
$S_1$	$S_1$	$S_2$	Beep
$S_2$	$S_1$	$S_3$	
$S_3$	$S_2$	$S_4$	
$S_4$	$S_3$	$S_4$	Beep

“Tug-of-war”





# Vending Machine



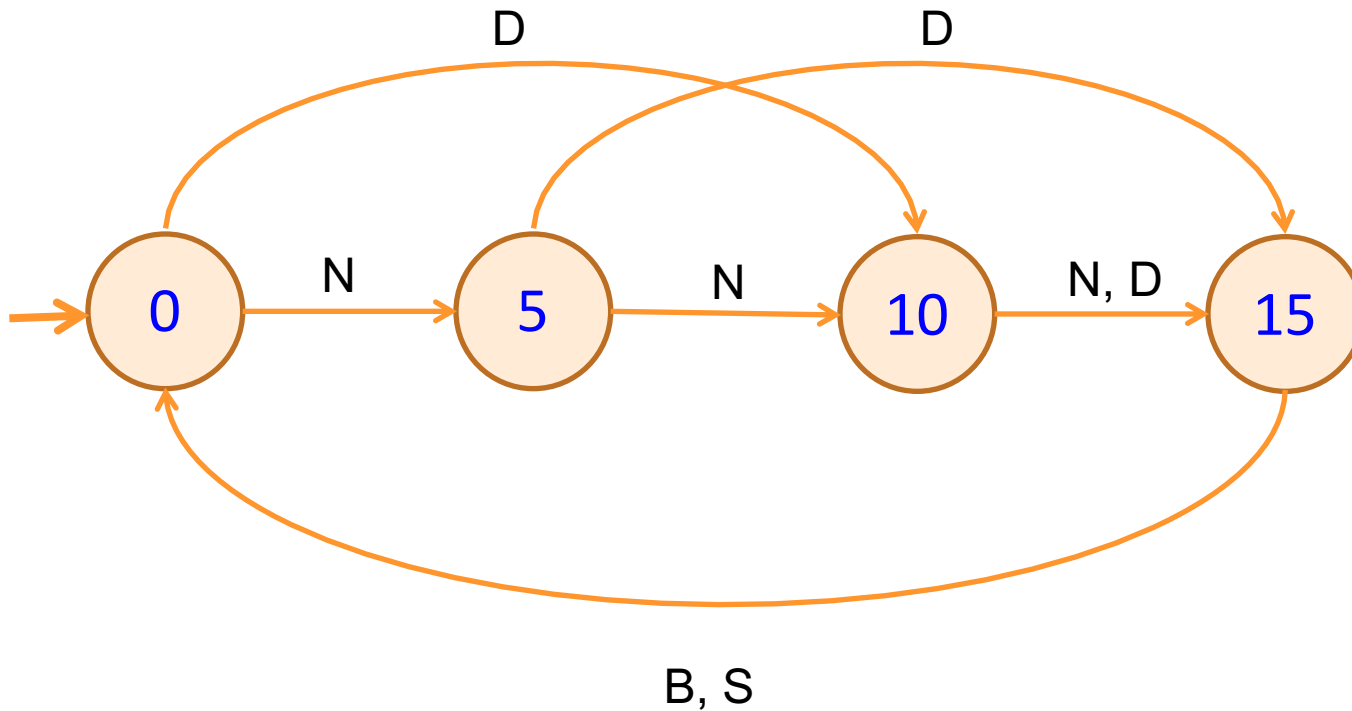
Enter 15 cents in dimes or nickels  
Press S or B for a candy bar





# Vending Machine, v0.1

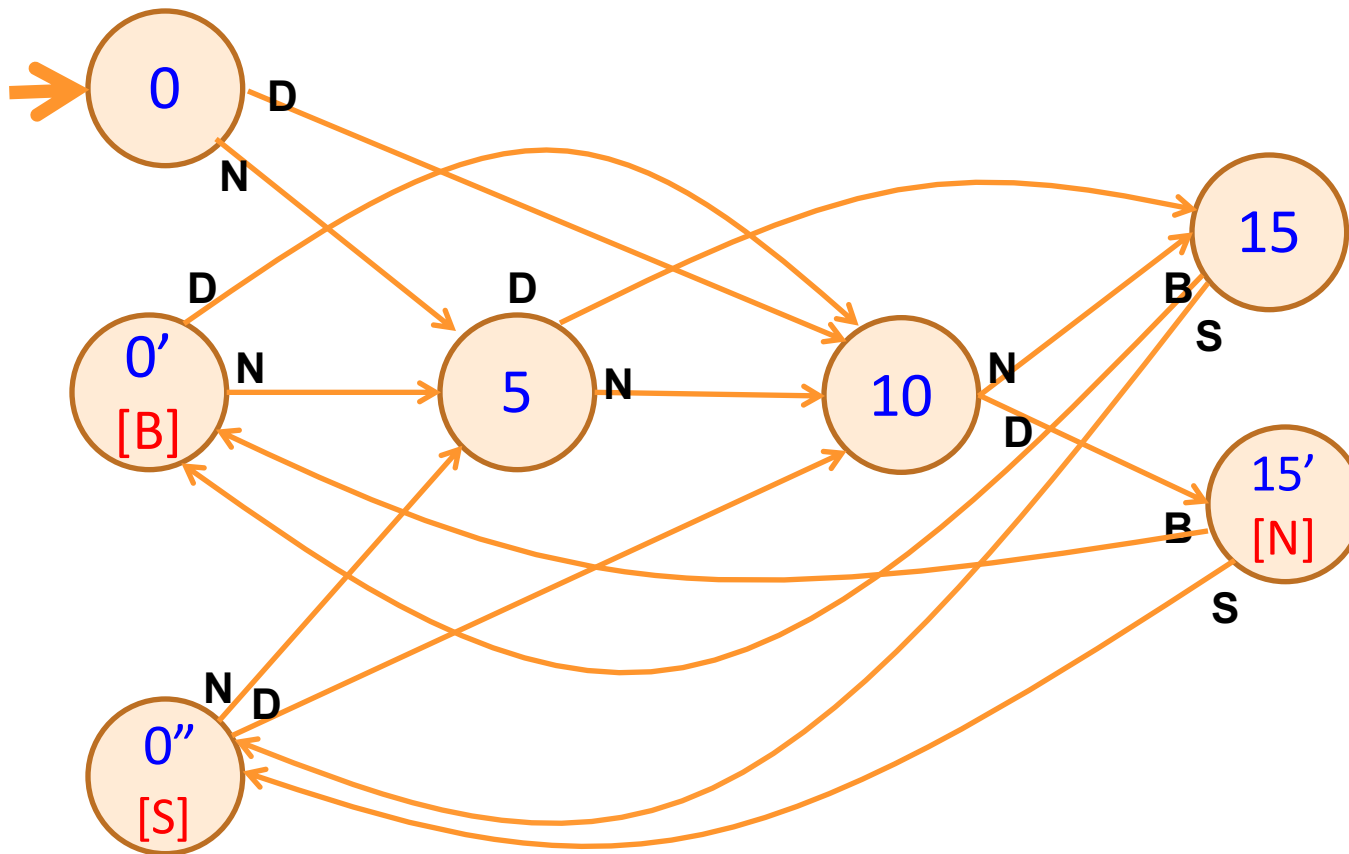
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Basic transitions on N (nickel), D (dime), B (butterfinger), S (snickers)

# Vending Machine, v0.2

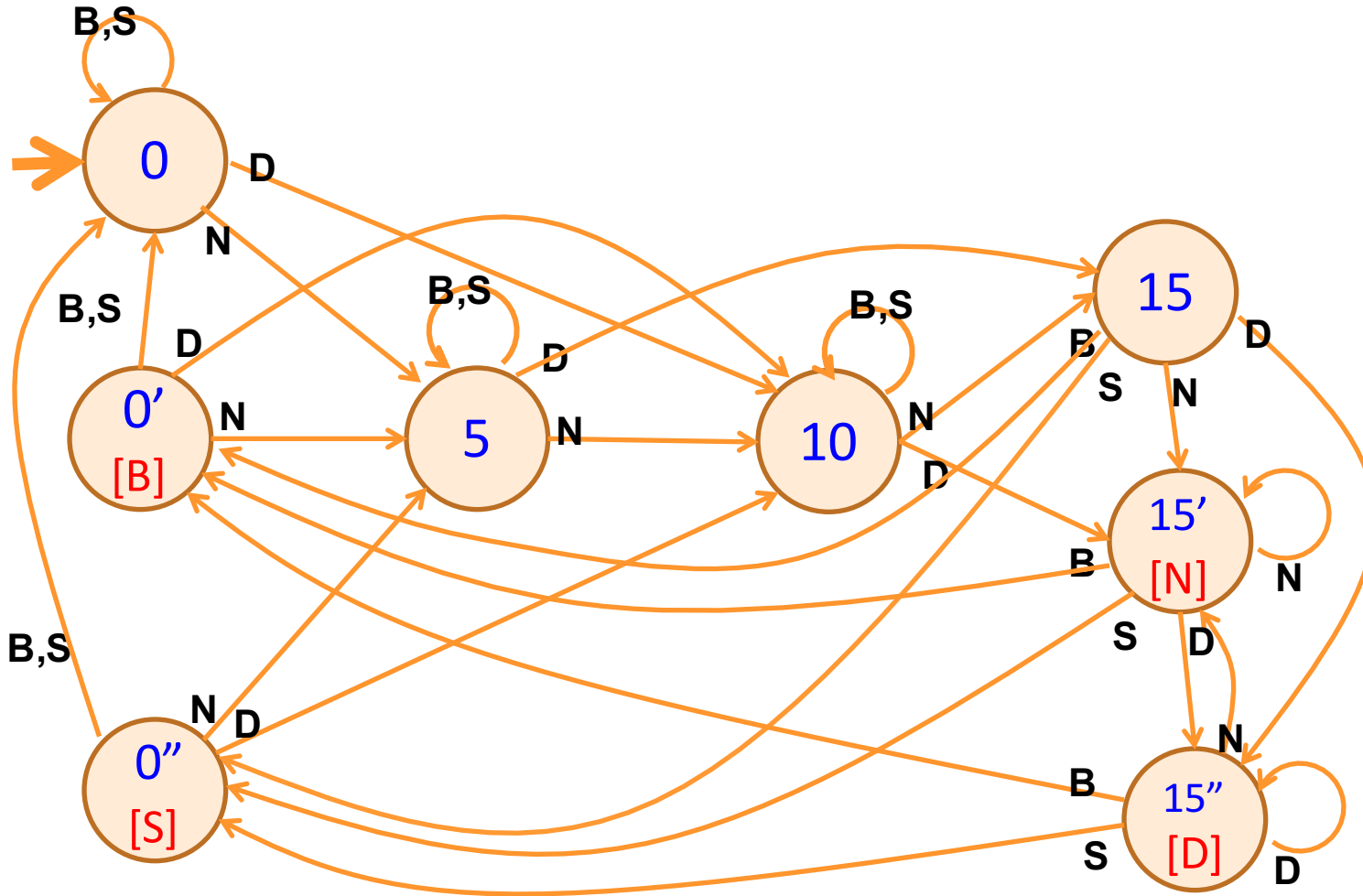
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Adding output to states: N – Nickel, S – Snickers, B – Butterfinger

# Vending Machine, v1.0

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Adding additional “unexpected” transitions