

# CSE 311: Foundations of Computing I

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## Inference Rules

Modus Ponens	$\frac{p, p \rightarrow q}{\therefore q}$
Direct Proof	$\frac{p \Rightarrow q}{\therefore p \rightarrow q}$
Elim $\wedge$	$\frac{p \wedge q}{\therefore p, q}$
Intro $\wedge$	$\frac{p, q}{\therefore p \wedge q}$
Elim $\vee$	$\frac{p \vee q, \neg p}{\therefore q}$
Intro $\vee$	$\frac{p}{\therefore p \vee q, q \vee p}$
Excluded Middle	$\overline{\therefore p \vee \neg p}$
Elim $\forall$	$\frac{\forall x P(x)}{\therefore P(a) \text{ for any } a}$
Intro $\forall$	$\frac{\text{Let } a \text{ be an arbitrary } \dots}{\therefore \forall x P(x)}$
Elim $\exists$	$\frac{\exists x P(x)}{\therefore P(c) \text{ for some special } c}$
Intro $\exists$	$\frac{P(c) \text{ for some } c}{\therefore \exists x P(x)}$