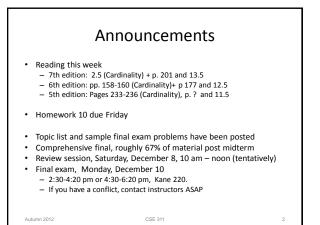
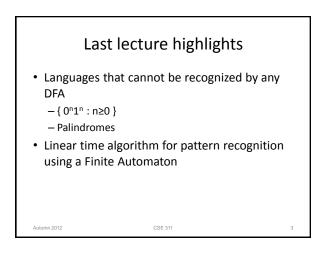
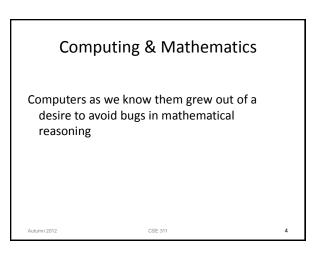
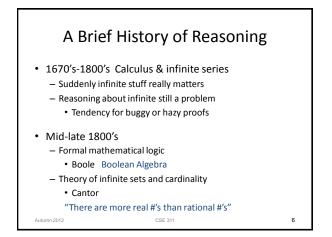
CSE	311 Foundations of Computing I	of
C	Lecture 28 Cardinality, Countability & Computability Autumn 2012	
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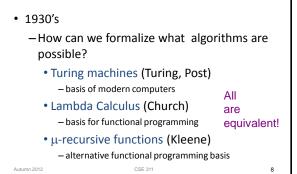


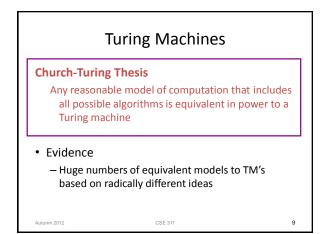
## A Brief History of Reasoning

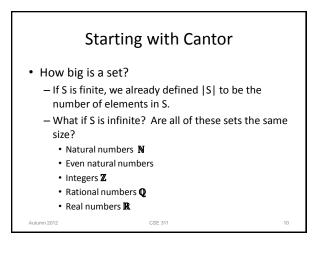
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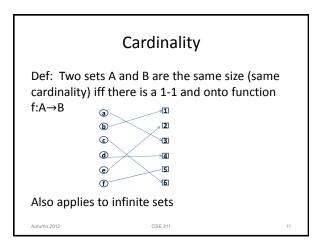
- Hilbert's famous speech outlines goal: mechanize all of mathematics 23 problems
- 1930's
  - Gödel, Turing show that Hilbert's program is impossible.
    - Gödel's Incompleteness Theorem
    - Undecidability of the Halting Problem
  - Both use ideas from Cantor's proof about reals & rationals

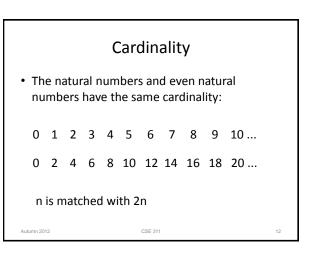
## A Brief History of Reasoning



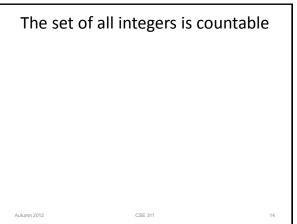


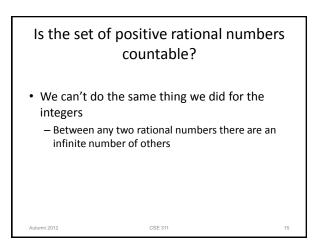


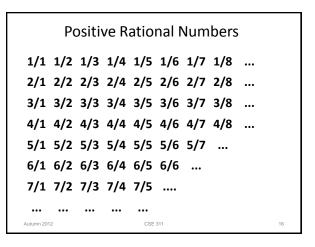




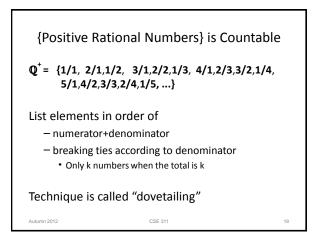
## CountabilityDefinition: A set is countable iff it is the same<br/>size as some subset of the natural numbersEquivalent: A set S is countable iff there is an<br/>onto function g: $\mathbb{N} \to S$ Equivalent: A set S is countable iff we can write<br/> $S=\{s_1, s_2, s_3, ...\}$

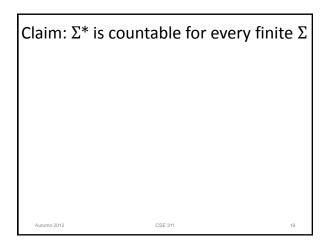


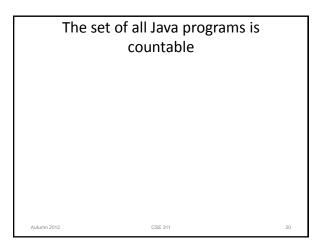


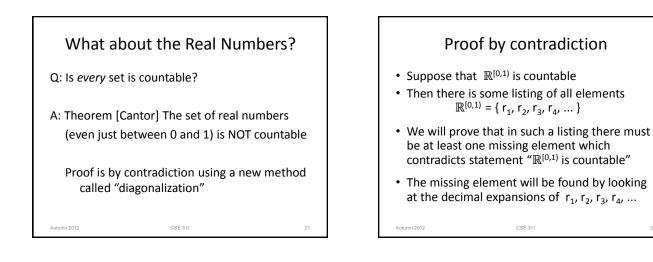


{Positive	e Rat	iona	l Nu	mbei	rs} is	Cou	ntabl	e
1/1 1/2	1/3	1/4	1/5	1/6	1/7	1/8		
2/1/2/2	2/3	2/4	2/5	2/5	2/7	2/8		
3/1 3/2	3/3	3/4	3/5	3/6	3/7	3/8		
4/1 4/2	4/3	4/4	4/5	4/6	4/7	4/8	•••	
5/1 5/2	5/3	5/4	5/5	5/6	5/7			
6/1 6/2	6/3	6/4	6/5	6/6				
7/1 7/2	7/3	7/4	7/5					
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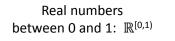


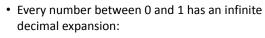






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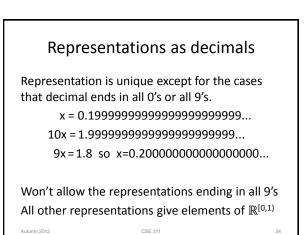




- 1/3 = 0.333333333333333333333333333...
- 1/7 = 0.14285714285714285714285...
- $\pi$  -3 = 0.14159265358979323846264...
  - 1/5 = 0.199999999999999999999999...

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		1	2	3	4	5	6	7	8	9	
<b>r</b> <sub>1</sub>	0.	5	0	0	0	0	0	0	0		
•1 r <sub>2</sub>	0.	3	3	3	3	3	3	3	3		
·2 r3	0.	1	4	2	8	5	7	1	4		
r <sub>4</sub>	0.	1	4	1	5	9	2	6	5		
r <sub>s</sub>	0.	1	2	1	2	2	1	2	2		
r <sub>6</sub>	0.	2	5	0	0	0	0	0	0		
r <sub>7</sub>	0.	7	1	8	2	8	1	8	2		
r <sub>8</sub>	0.	6	1	8	0	3	3	9	4		
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r <sub>3</sub>	0.	1	4	2	8	5	7	1	4		
r <sub>4</sub>	0.	1	4	1	5	9	2	6	5		
r <sub>5</sub>	0.	1	2	1	2	2	1	2	2		
r <sub>6</sub>	0.	2	5	0	0	0	0	0	0		
r <sub>7</sub>	0.	7	1	8	2	8	1	8	2		
r <sub>8</sub>	0.	6	1	8	0	3	3	9	4		
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