# CSE 311 Foundations of Computing I

Lecture 22
Finite State Machines: Output and Minimization
Autumn 2011

Autumn 2011 CSE 311

#### **Announcements**

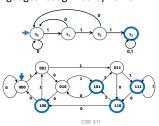
- Reading assignments
  - 7<sup>th</sup> Edition, Sections 13.3 and 13.4
  - 6<sup>th</sup> Edition, Section 12.3 and 12.4
  - -5<sup>th</sup> Edition, Section 11.3 and 11.4

utumn 2011 CSE 311

## Last lecture highlights

Finite state machines

- States, transitions, start state, final states
- Languages recognized by FSMs



Last lecture highlights

- Combining FSMs to check two properties at once

• New states record states of both FSMs

Output

Description

# State Machines with Output SNIFICES Vending Machine

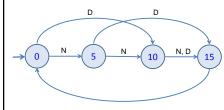
Enter 15 cents in dimes or nickels Press S or B for a candy bar

Autumn 2011



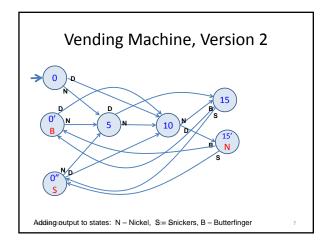
CSE 311

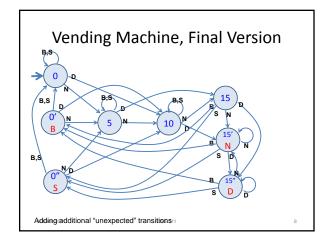
## Vending Machine, Version 1



B, S

Basic transitions on N (nickel), D (dime),  $^3B$  (butterfinger), S (snickers)





### State Minimization

- Many different FSMs (DFAs) for the same problem
- Take a given FSM and try to reduce its state set by combining states
  - Algorithm will always produce the unique minimal equivalent machine (up to renaming of states) but we won't prove this

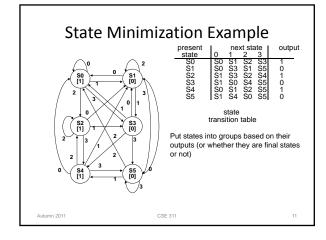
Autumn 2011 CSE 311 9

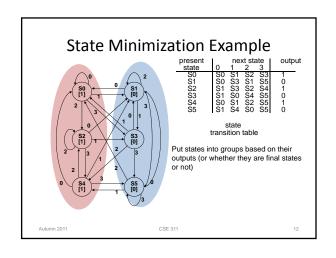
### State minimization algorithm

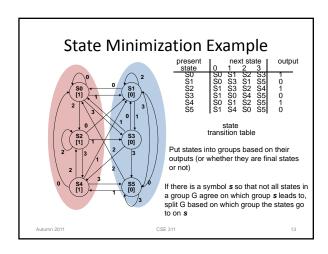
- 1. Put states into groups based on their outputs (or whether they are final states or not)
- 2. Repeat the following until no change happens
  - a. If there is a symbol s so that not all states in a group G agree on which group s leads to, split G into smaller groups based on which group the states go to on s

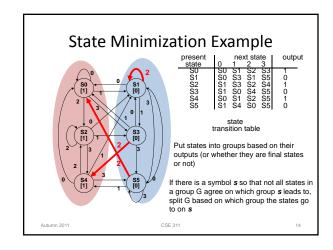
Automo 2011

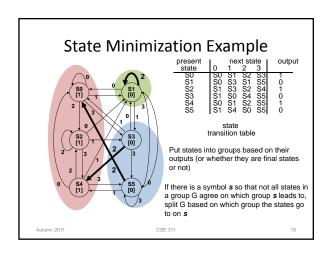
CSL > 10

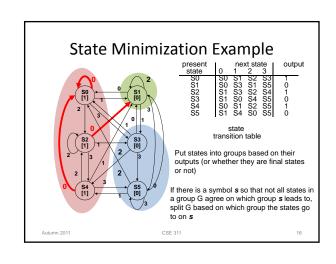


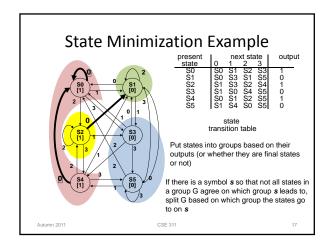


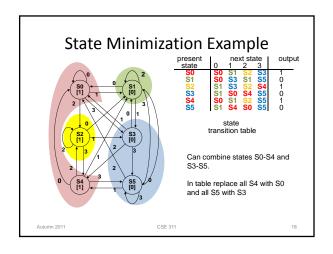


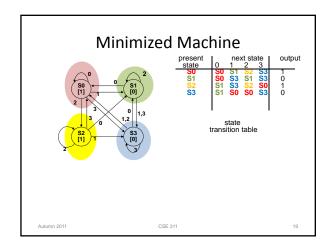


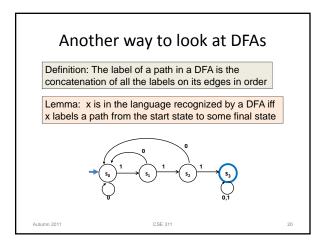










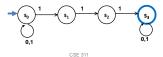


### Nondeterministic Finite Automaton (NFA)

- Graph with start state, final states, edges labeled by symbols (like DFA) but
  - Not required to have exactly 1 edge out of each state labeled by each symbol - can have 0 or >1
  - Also can have edges labeled by empty string  $\pmb{\lambda}$

Autumn 2011

 Definition: x is in the language recognized by an NFA iff x labels a path from the start state to some final state



Design an NFA to recognize the set of binary strings that contain 111 or have an even # of 1's

CSE 311

Autumn 2011