

# CSE 311 Foundations of Computing I

Lecture 21  
Finite State Machines  
Autumn 2011

## Announcements

- Reading assignments
  - 7<sup>th</sup> Edition, Sections 13.3 and 13.4
  - 6<sup>th</sup> Edition, Section 12.3 and 12.4
  - 5<sup>th</sup> Edition, Section 11.3 and 11.4
- HW 8 is on-line

## Last lecture highlights

Let  $R$  be a relation on a set  $A$ . There is a path of length  $n$  from  $a$  to  $b$  if and only if  $(a,b) \in R^n$

Let  $R$  be a relation on a set  $A$ . The connectivity relation  $R^*$  consists of the pairs  $(a,b)$  such that there is a path from  $a$  to  $b$  in  $R$ .

Transitive-Reflexive closure: Add the minimum possible number of edges to make the relation transitive and reflexive

The transitive-reflexive closure of a relation  $R$  is the connectivity relation  $R^*$

## Finite state machines

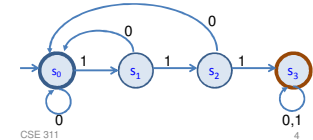
States

Transitions on inputs

Start state and final states

The language recognized by a machine is the set of strings that reach a final state

State	0	1
$s_0$	$s_0$	$s_1$
$s_1$	$s_0$	$s_2$
$s_2$	$s_0$	$s_3$
$s_3$	$s_3$	$s_3$



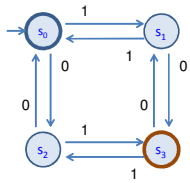
## Applications of Finite State Machines (a.k.a. Finite Automata)

- Implementation of regular expression matching in programs like **grep**
- Control structures for sequential logic in digital circuits
- Algorithms for communication and cache-coherence protocols
  - Each agent runs its own FSM
- Design specifications for reactive systems
  - Components are communicating FSMs

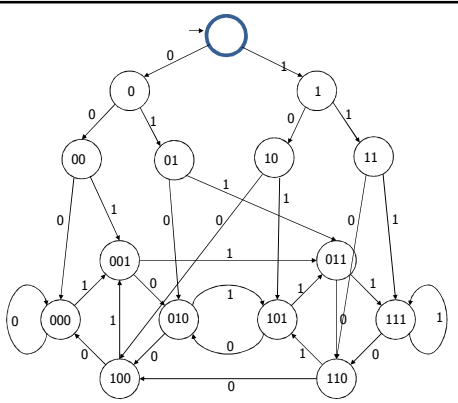
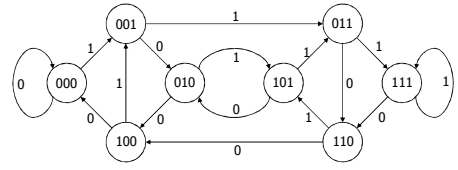
## Applications of Finite State Machines (a.k.a. Finite Automata)

- Formal verification of systems
  - Is an unsafe state reachable?
- Computer games
  - FSMs provide worlds to explore
- Minimization algorithms for FSMs can be extended to more general models used in
  - Text prediction
  - Speech recognition

What language does this machine recognize?



3 Bit Shift register

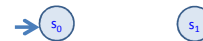


Design a DFA that accepts strings with a 1 three positions from the end

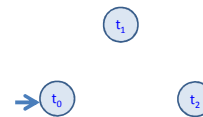
How does the size of a DFA to recognize "10<sup>th</sup> character is a 1" compare with the size of a DFA to recognize "10<sup>th</sup> character from the end is 1"?

Strings over  $\{0, 1, 2\}^*$

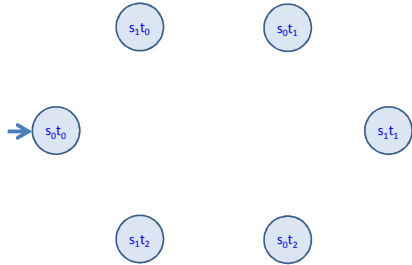
$M_1$ : Strings with an even number of 2's



$M_2$ : Strings where the sum of digits mod 3 is 0



## Recognize strings with an even number of 2's and a mod 3 sum of 0



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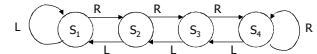
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## State machines with output

"Tug-of-war"

State	Input		Output
	L	R	
$s_1$	$s_1$	$s_2$	Beep
$s_2$	$s_1$	$s_3$	
$s_3$	$s_2$	$s_4$	
$s_4$	$s_3$	$s_4$	Beep



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## Vending Machine

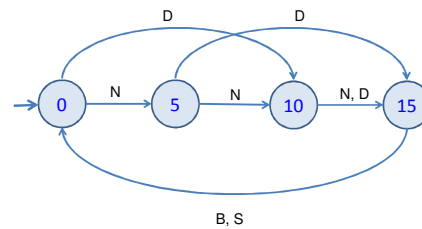
Enter 15 cents in dimes or nickels  
Press S or B for a candy bar



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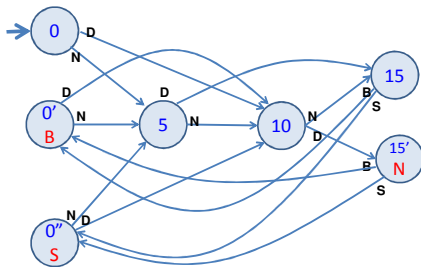
## Vending Machine, Version 1



Basic transitions on N (nickel), D (dime); B (butterfinger), S (snickers)

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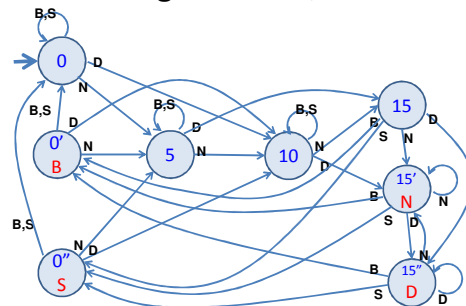
## Vending Machine, Version 2



Adding output to states: N – Nickel, S= Snickers, B – Butterfinger

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## Vending Machine, Final Version



Adding additional "unexpected" transitions:

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