CSE311: Quiz Section, 10/13/2011

Reminder about homework:

Be sure to read the homework questions VERY carefully. Apparently people lost points on homework 1 by not quite answering the question that was asked.

Answers: I won't be posting any answers for this worksheet, because I've taken all of the problems (except the first one) from odd-numbered problems in the text book, which means the answers are in the back of the book. I've given you the problem numbers for the 6th and 7th editions. (Sorry, I don't have access to a 5th edition.) Please note that where the a) b) c) enumeration don't match up, I've put the original letter at the end of the item.

- 1. Translate English to logical expressions, varying domains
 - For each one of these, translate twice: once with a domain of all students in the class and once with a domain of all people.
 - (a) Someone in the class is a rodeo clown.
 - (b) Everyone in the class is a secret agent.
- 2. Logical equivalence with quantifiers.

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7th edition: 1.4: 43; 6th edition: 1.3: 43
Is \forall x(P(x) \to Q(x)) logically equivalent to \forall x P(x) \to \forall x Q(x)? Justify your answer.
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3. Translate English to logical expressions with nested quantifiers.

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7th edition: 1.5: 9; 6th edition: 1.4: 9
Let L(x,y) be the statement "x loves y"
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- (a) There is somebody whom everybody loves (c)
- (b) Nobody loves everybody (d)
- (c) There is exactly one person whom everybody loves. (g)
- (d) Everyone loves himself or herself. (i)
- (e) There is someone who loves no one besides himself or herself. (j)
- 4. Translate nested quantifiers into English

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7th edition: 1.5: 25; 6th edition: 1.4: 25
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For all of these the domain is all real numbers...

- (a) $\exists x \forall y (xy = y)$ (a)
- (b) $\exists x \exists y ((x^2 > y) \land (x < y))$ (c)
- (c) $\forall x \forall y \exists z (x + y = z)$ (d)
- 5. Negating quantifiers

7th edition: 1.5: 33; 6th edition: 1.4: 33

Move the negations to appear only within predicates (that is, no negation is outside a quantifier or an expression involving logical connectives).

- (a) $\neg \forall y \forall x (P(x,y) \lor Q(x,y))$ (c)
- (b) $\neg(\exists x \exists y \neg P(x,y) \land \forall x \forall y Q(x,y))$ (d)
- 6. Using inference rules and equivalences to prove that given premises imply a conclusion

7th edition: 1.6: Examples 6 and 7; 6th edition: 1.5: Examples 6 and 7 Show that the given premises imply the conclusion

- (a) Premises: $\neg p \land q, r \rightarrow p, \neg r \rightarrow s, s \rightarrow t$ Conclusion: t
- (b) Premises: $p \to q, \neg p \to r, r \to s$ Conclusion: $\neg q \to s$
- 7. Use inference rules with quantified premises and conclusions

7th edition: 1.6: 27, 29; 6th edition: 1.5: 27, 29

- (a) Premises: $\forall x (P(x) \to (Q(x) \land S(x))), \forall x (P(x) \land R(x))$ Conclusion: $\forall x (R(x) \land S(x))$
- (b) Premises: $\forall x(P(x) \lor Q(x)), \ \forall x(\neg Q(x) \lor S(x)), \ \forall x(R(x) \to \neg S(x)), \ \exists x \neg P(x)$

Conclusion: $\exists x \neg R(x)$