

Recursive Backtracking Recursive Backtracking Recursive Backtracking

Outline Playing With Boolean Expressions

Definition (Recursive Backtracking)

Recursive Backtracking

Recursive Backtracking Strategy

If we found a solution, stop looking (e.g. return)

partial solutions and abandoning them if they don't work.

- Otherwise for each possible choice c...
 - Make the choice c
 - Recursively continue to make choices
 - Un-make the choice c (if we got back here, it means we need to continue looking)

Recursive Backtracking is an attempt to find solution(s) by building up

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Client vs. Implementor, again

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You may have noticed that many of the class examples I've been showing involve me using a class that I've already written. There are several reasons for this:

- Learning to read and use an API is a really important programming skill
- Switching between the client and implementor views is an important goal of this course
- The code I write is usually easy, but really tedious (so, it would be a waste of time to write in class)

Take-Away

Every time I print out an API for you, you should try to understand it from the comments. This will help you on the homework, on exams, and in any future programming endeavors.

BooleanExpression

Today's API is BooleanExpression.

What is a BooleanExpression?

The BooleanExpression class allows us to represent the conditions we write in if statements. For instance, to represent the following:

- 1 if (!(queue.size() > 0) && queue.peek() > 5) {
- 2 .. 3 }

We would do

new BooleanExpression("(!a && b)");

Notice that we use single letter variable names instead of queue.size() > 0. This is a simplification for implementation.

Evaluating BooleanExpression

Evaluating BooleanExpressions

Remember when we took (1+2) * 3 and evaluated it to 9 recursively? We can do a similar thing for BooleanExpressions: Consider the BooleanExpression from above:

"(!a && b)"

Suppose we know the following:

- a is true.
- b is false.

Who Sho

What does this expression evaluate to?

 $(\texttt{!a \&\& b}) \longrightarrow (\texttt{!true \&\& false}) \longrightarrow (\texttt{false \&\& false}) \longrightarrow \texttt{false}$

Suppose we wanted to write a method:

public static boolean evaluate(BooleanExpression e, ??? assn)

where assn represents the truth values of the variables.

What type would assn be? It's a mapping from variables to truth values.

Evaluating BooleanExpression Okay, so, we have: public static boolean evaluate(BooleanExpression e, Map<String, Boolean> assignments) Consider the following case: evaluate return value? 🔳 e is a && b assignments map is {a=true}. What should evaluate return? We can't answer the question. What seems like a good idea? null. So, we change the return type to Boolean.

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Uh Oh... How can we try assignments?

We don't have a way of passing assignments through to the function. How can we fix this?

public/private pair!

Public/Private Recursive Pair

public static void canBeTrue(BooleanExpression b)

private static void canBeTrue(BooleanExpression b, Map<String, Boolean> m)

canBeTrue Solution



BTW, Why does this problem matter?

Solving canBeTrue quickly is the $\ensuremath{\mbox{most}}$ important open problem in Computer Science.

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- If you solve this problem in $\mathcal{O}(n^k)$ time for any k, the following happen: You get one million dollars.
 - You get a PhD.
 - You get a PhD.
 - \blacksquare You become the most famous Computer Scientist, pretty much ever
 - You break all banks, credit cards, website encryption, etc.