

# Lecture 14: Recursive Backtracking II

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07/27/22



# Reminders

- A3 Resubmission due Wednesday 7/27 @ 11:59pm
- A5 due Thursday 7/28 @ 11:59pm

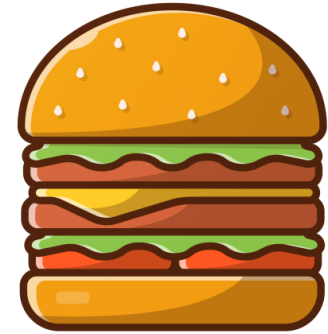
# Spend all your Husky card money!



Balance: \$3



\$1



\$2



\$3



\$5

chosen: 📞  
dollarsLeft: 3

Output:

chosen

Phone Number: 425-123-4567

chosen: 📞  
dollarsLeft: 3

\$1

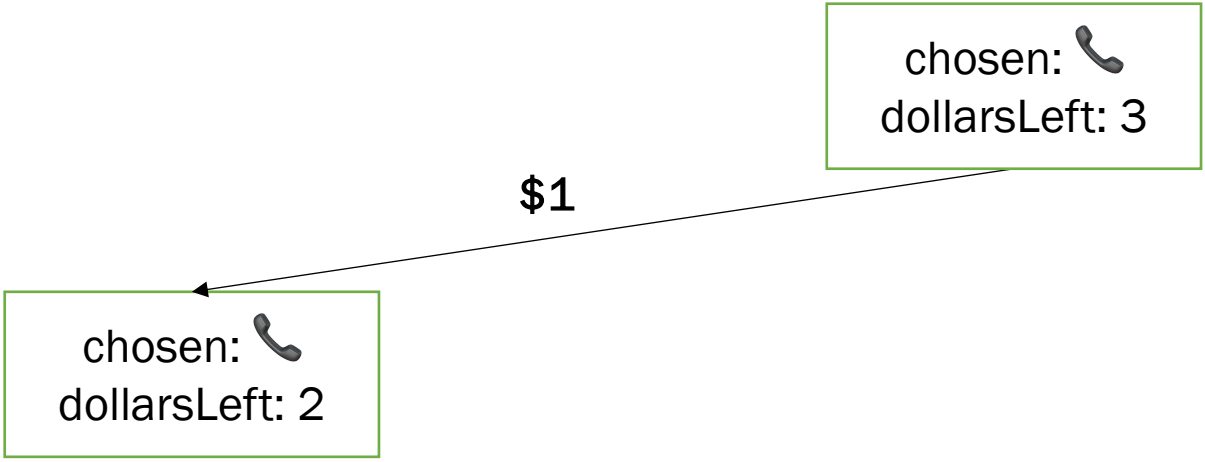


Output:

1

chosen

Phone Number: 425-123-4567

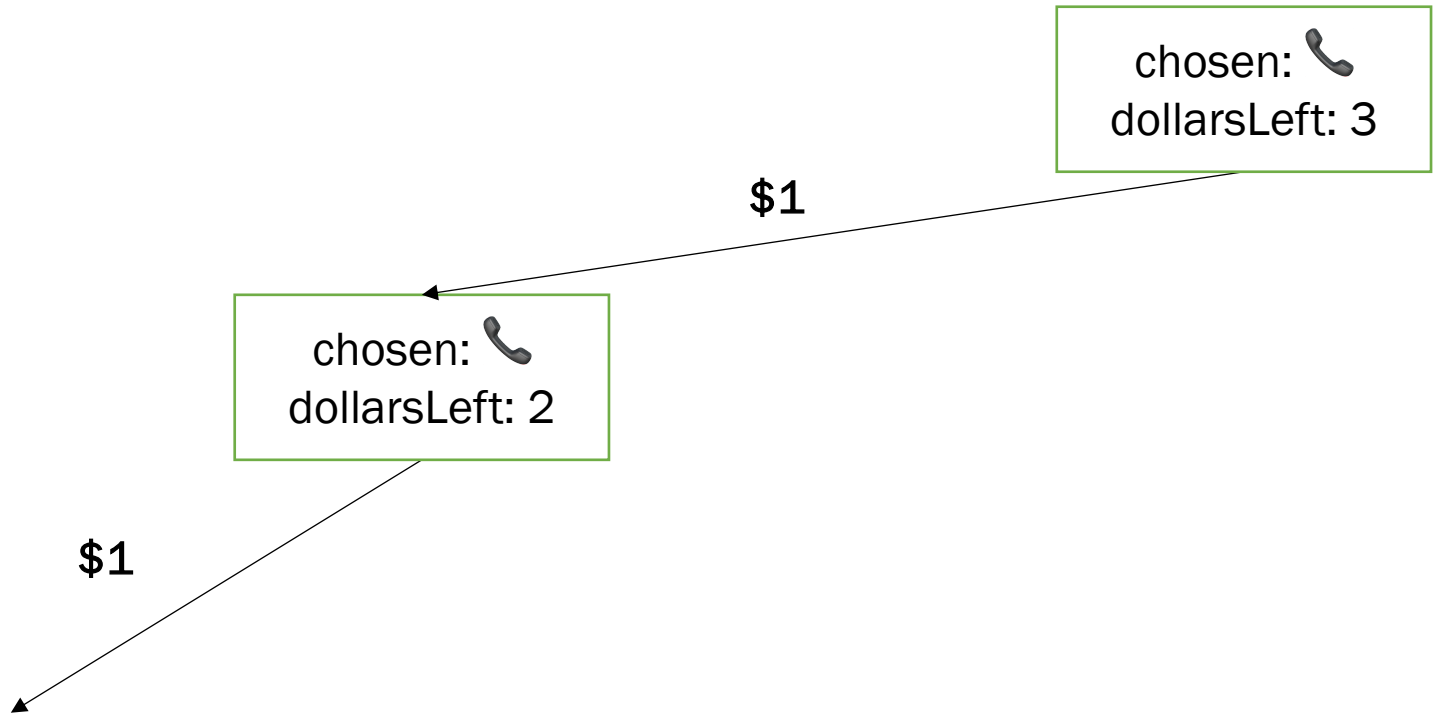


Output:

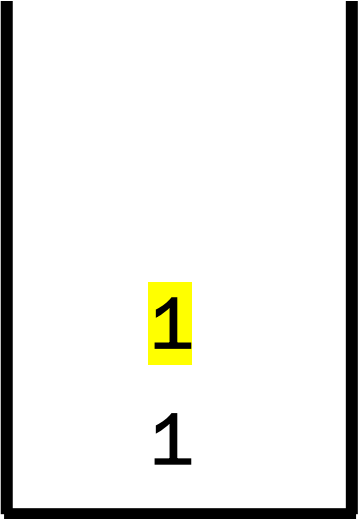
1

chosen

Phone Number: 425-123-4567

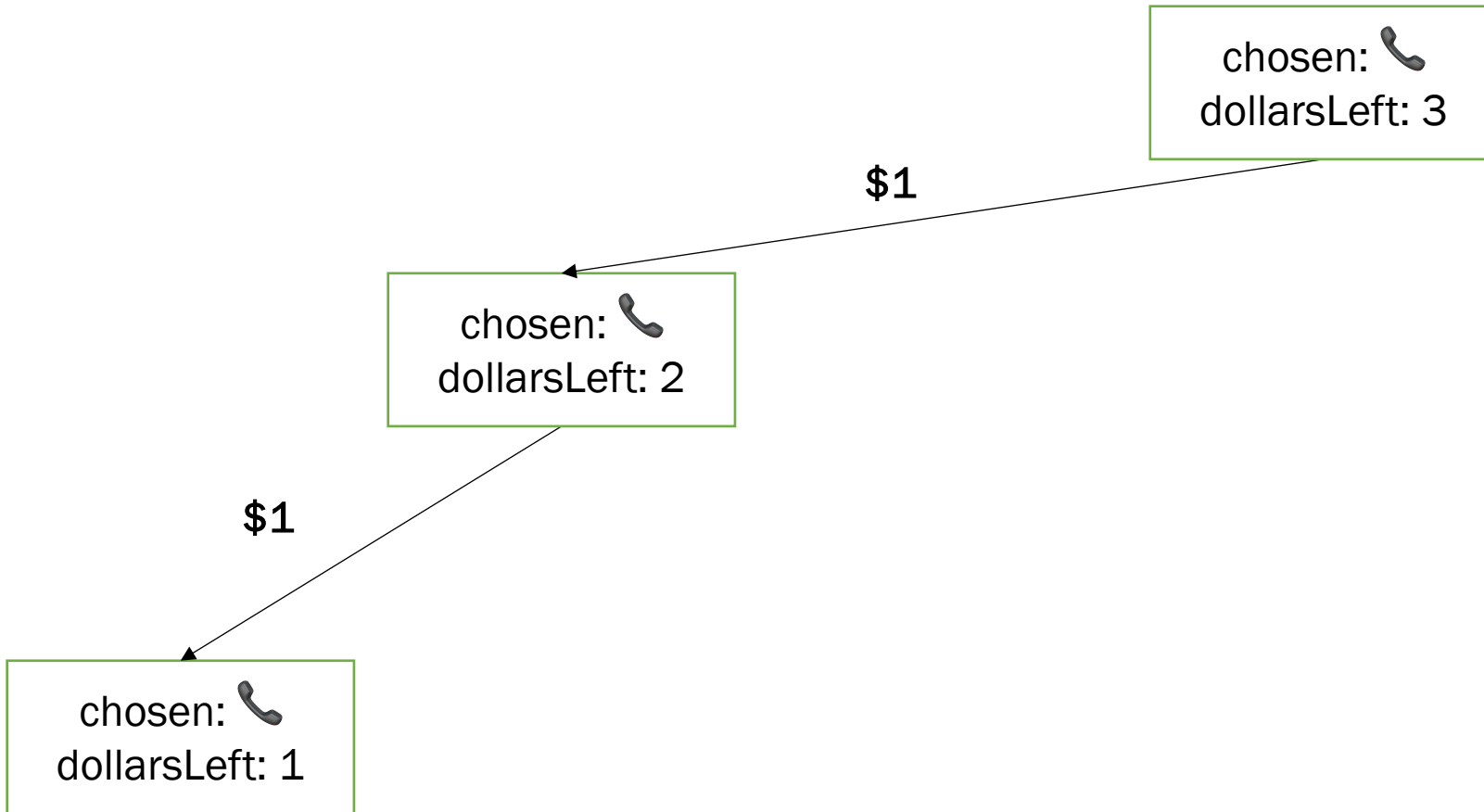


Output:



chosen

Phone Number: 425-123-4567



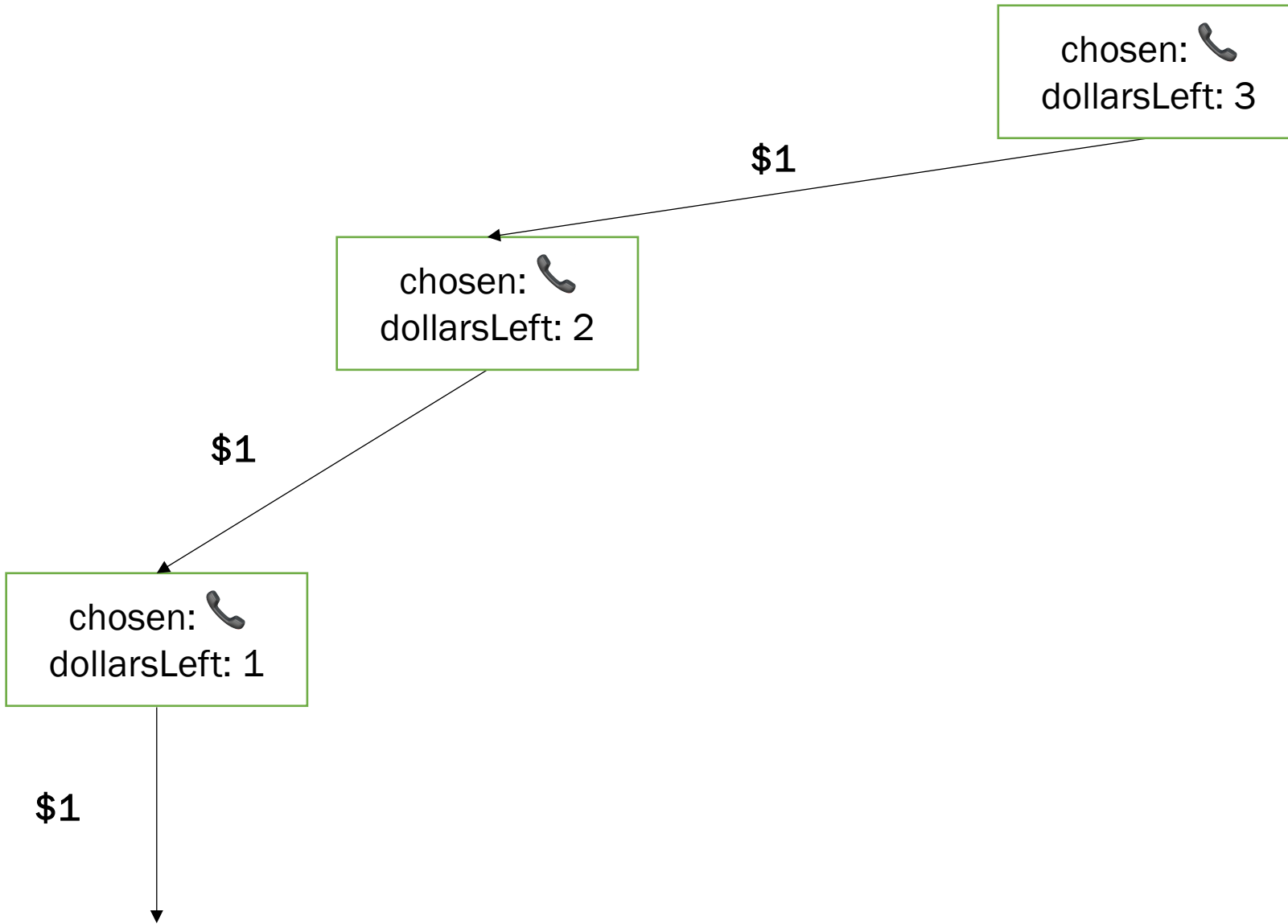
Output:

1  
1

chosen

Phone Number: 425-123-4567



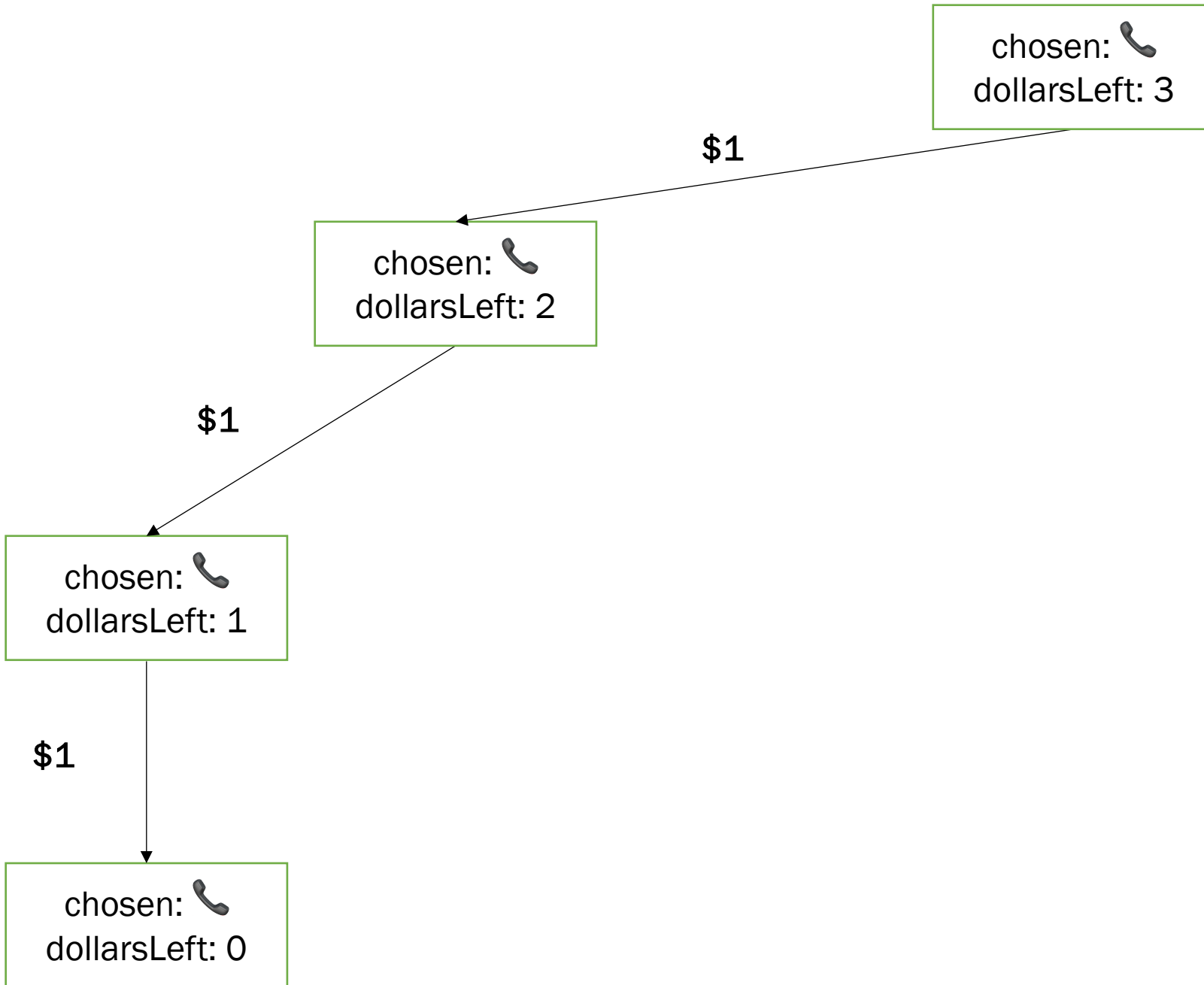


Output:

1  
1  
1

chosen

Phone Number: 425-123-4567

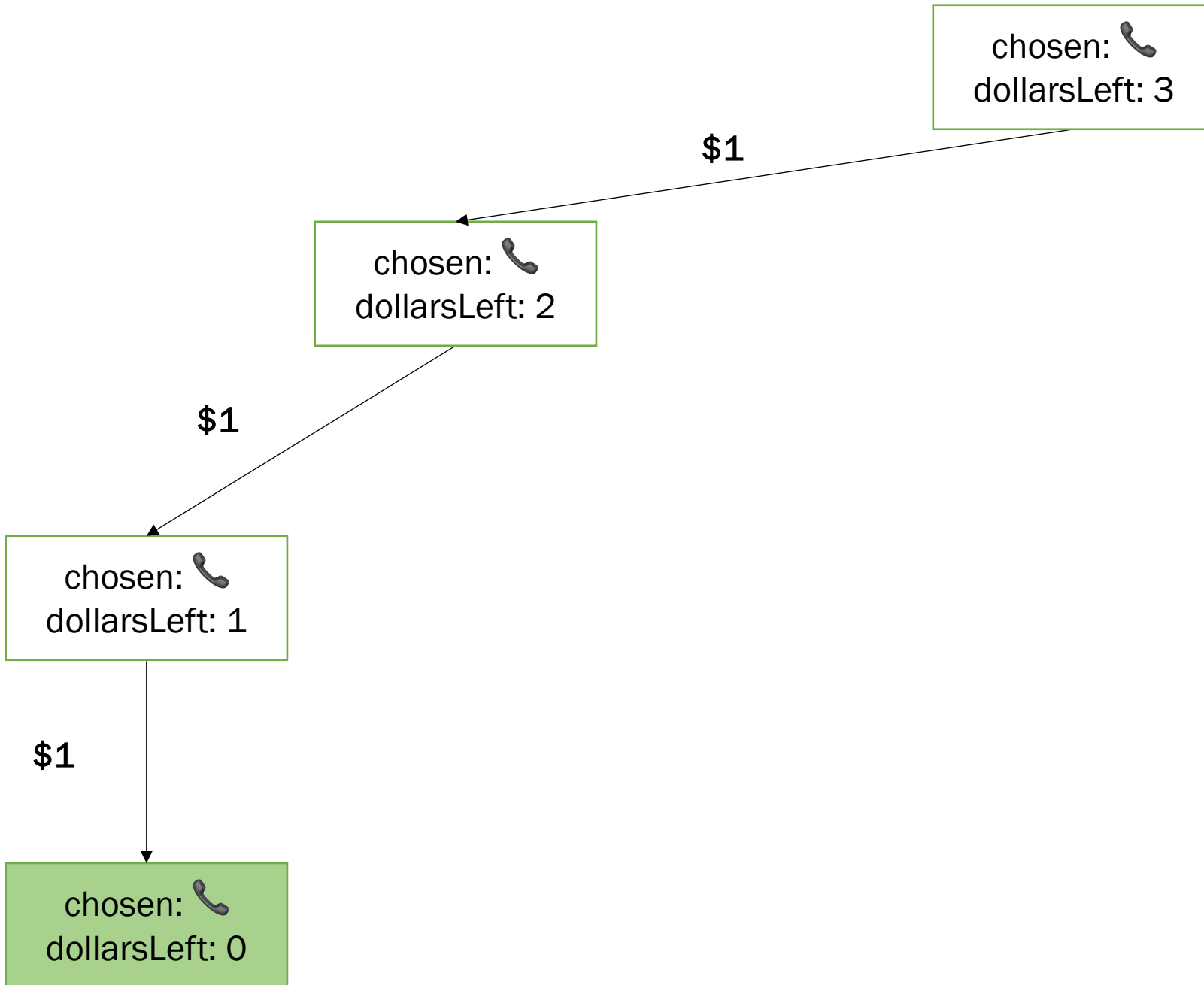


Output:

1  
1  
1

chosen

Phone Number: 425-123-4567

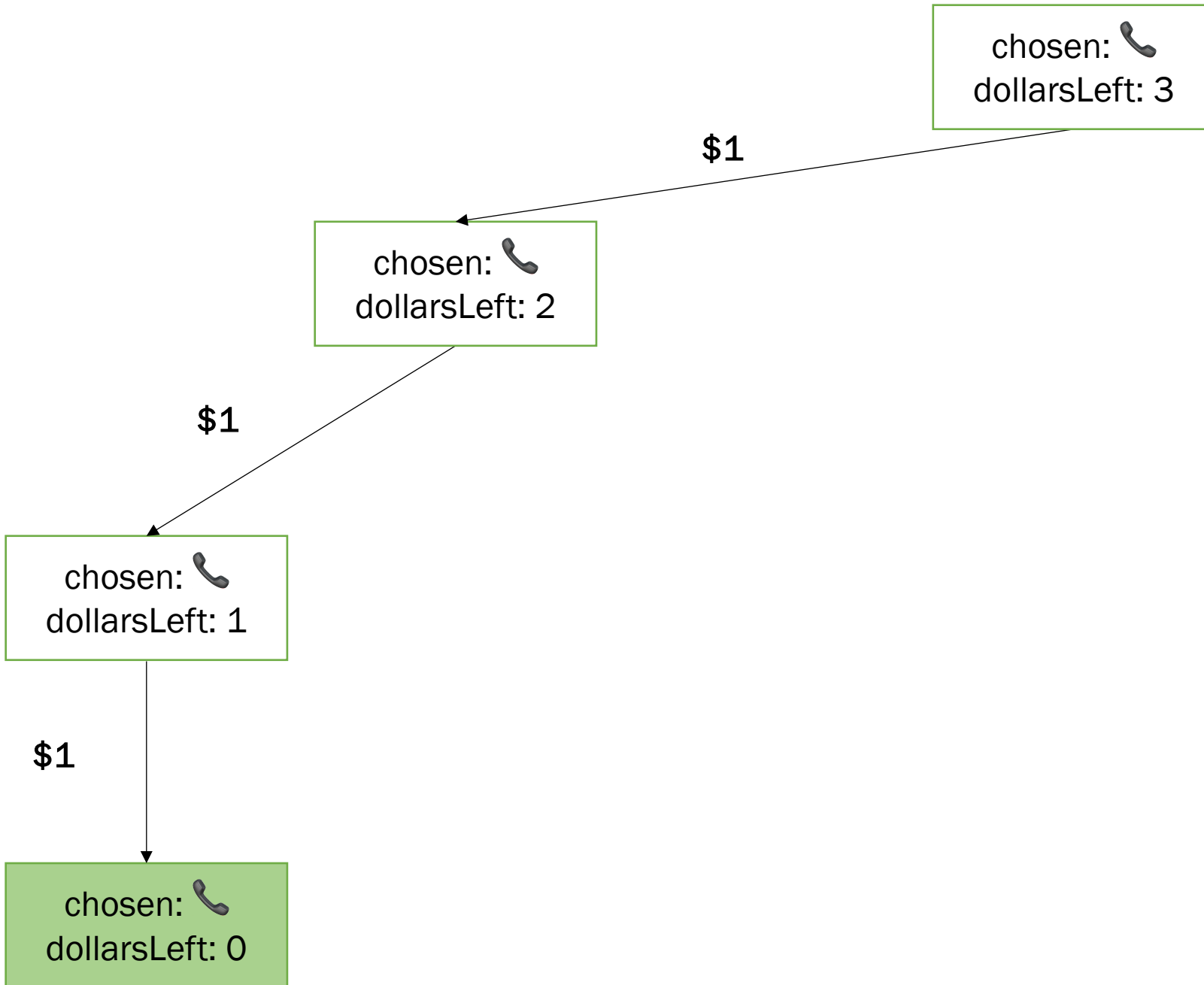


Output:

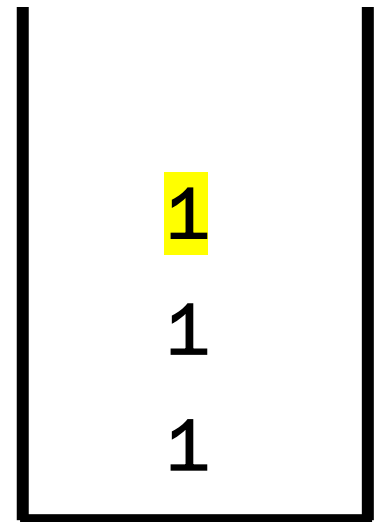
1  
1  
1

chosen

Phone Number: 425-123-4567

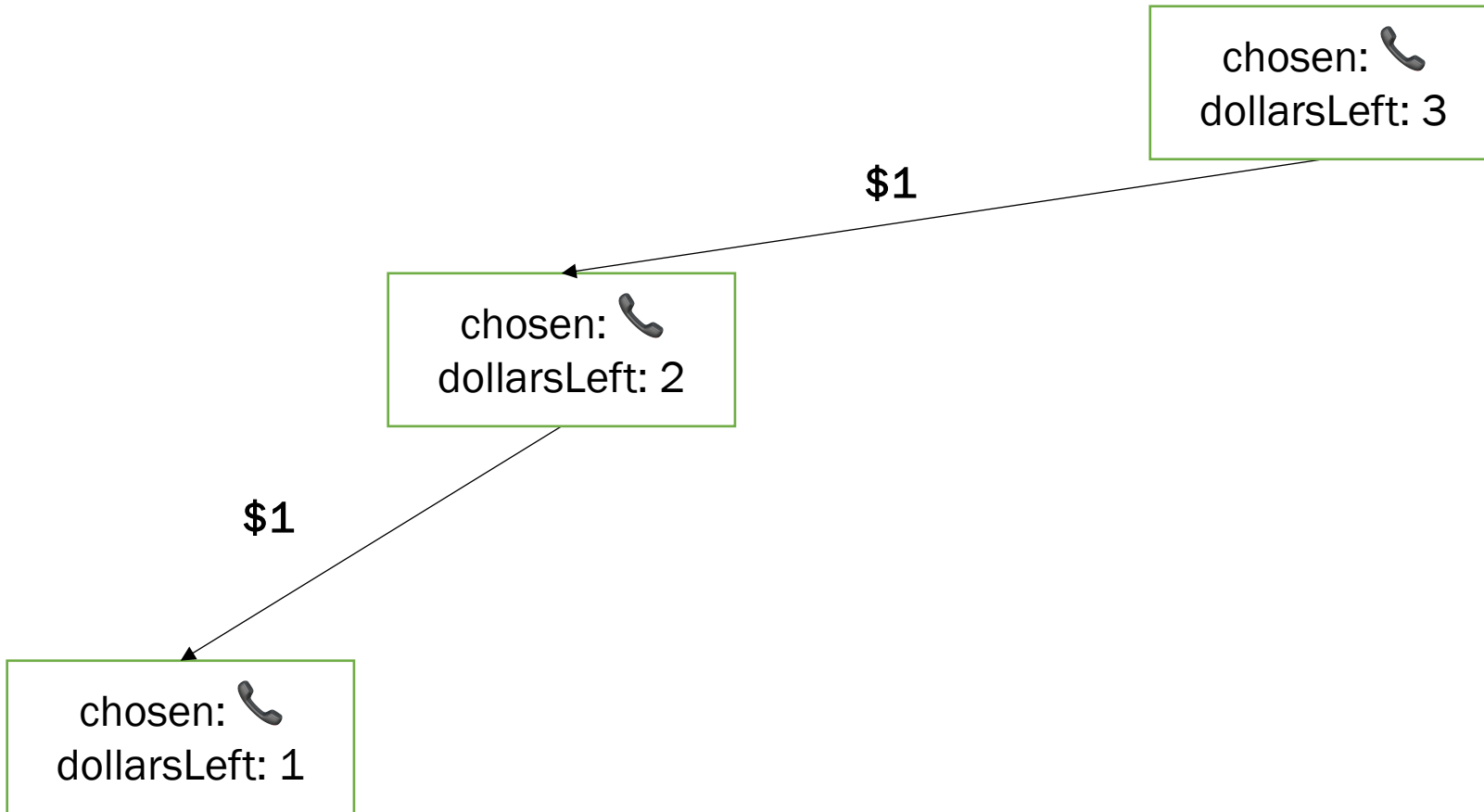


Output:  
[1, 1, 1]

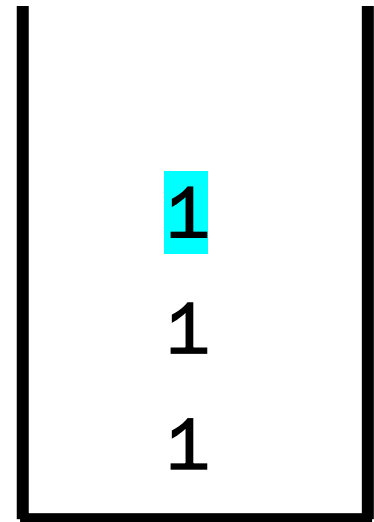


chosen

Phone Number: 425-123-4567

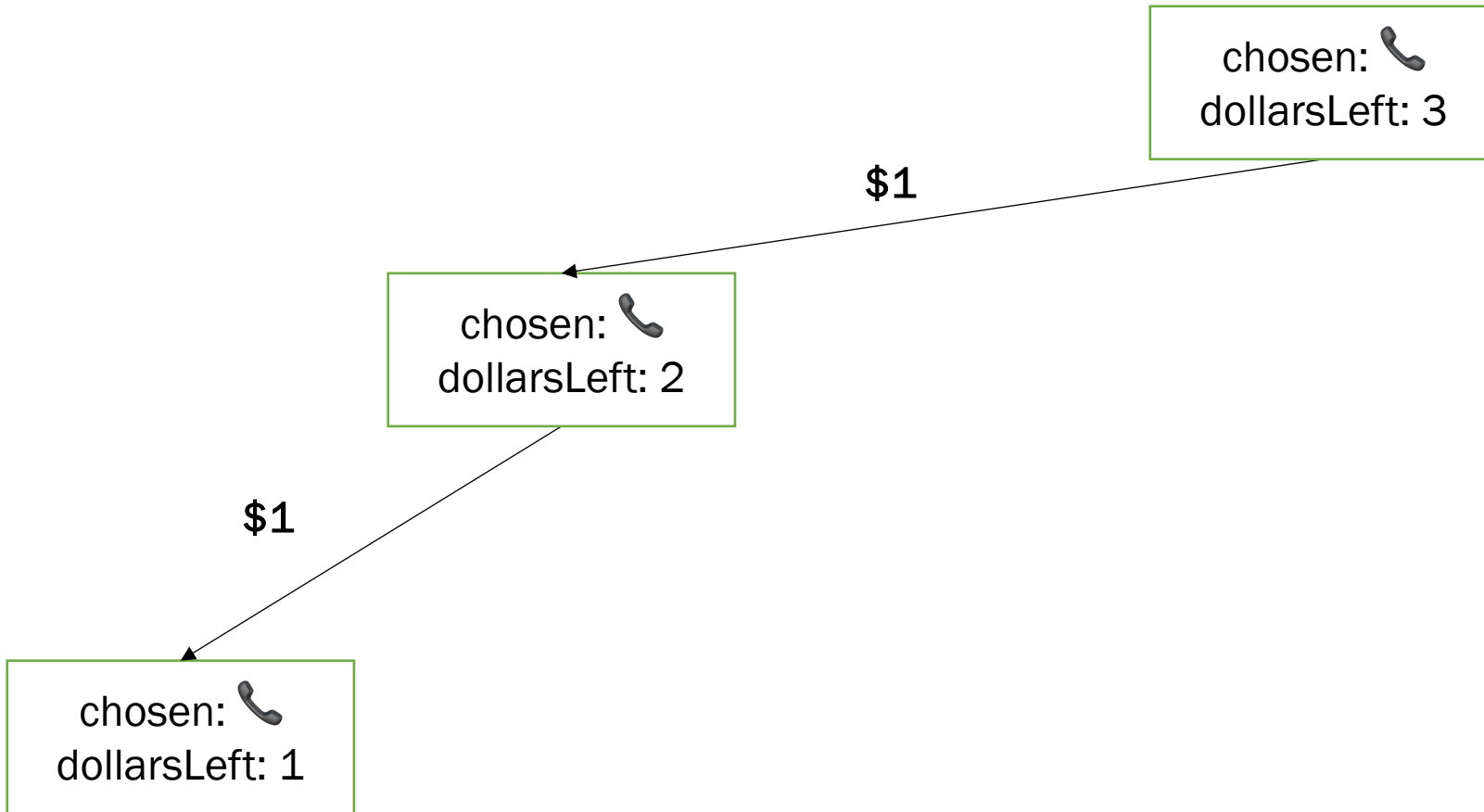


Output:  
[1, 1, 1]

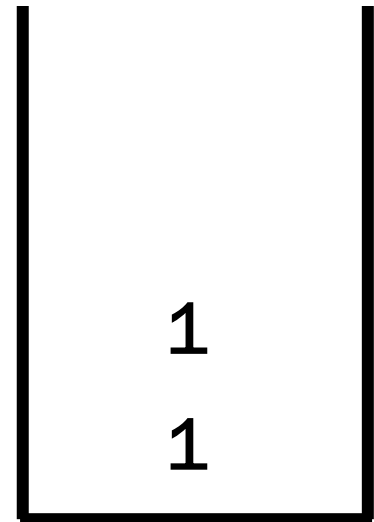


chosen

Phone Number: 425-123-4567

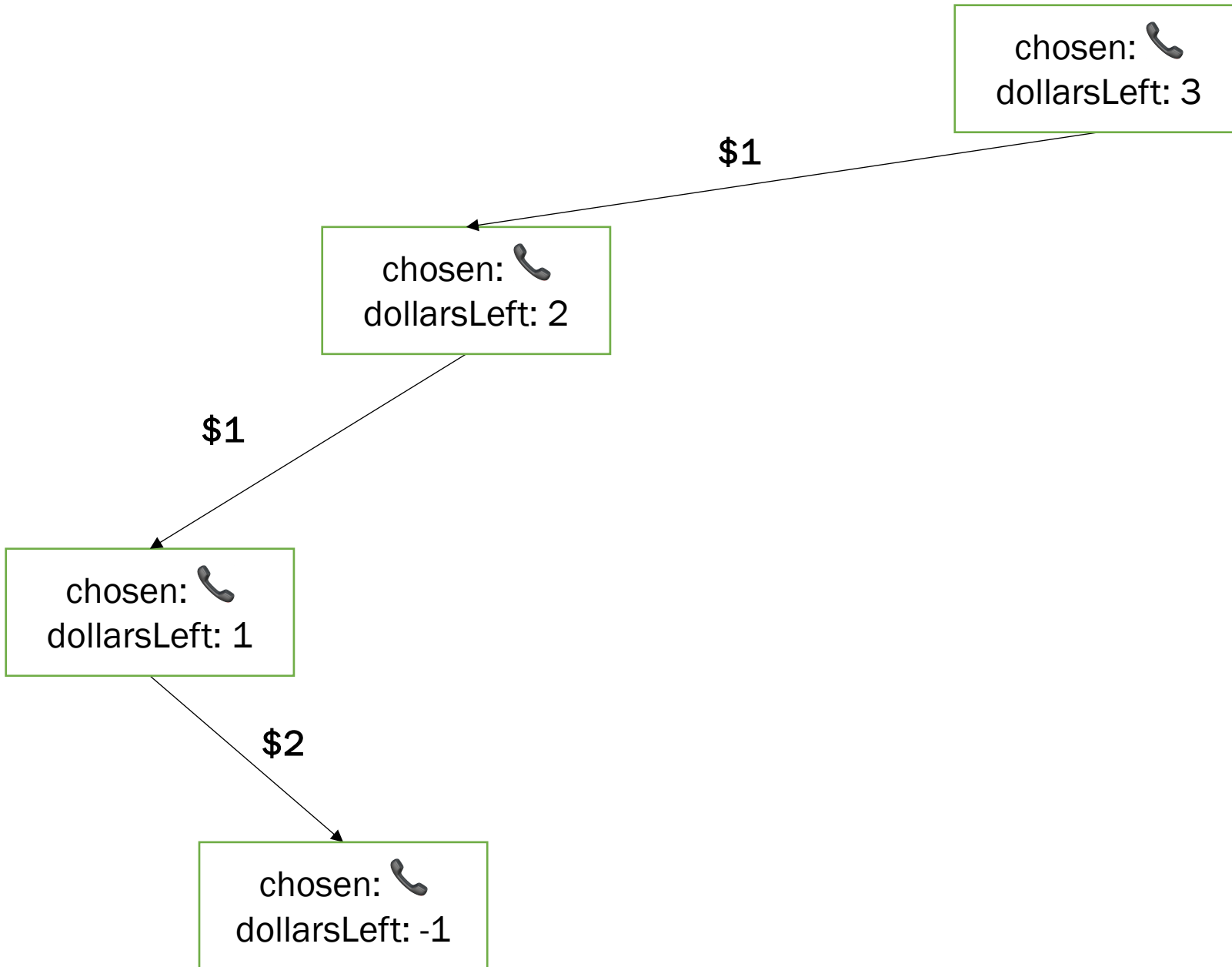


Output:  
[1, 1, 1]



chosen

Phone Number: 425-123-4567

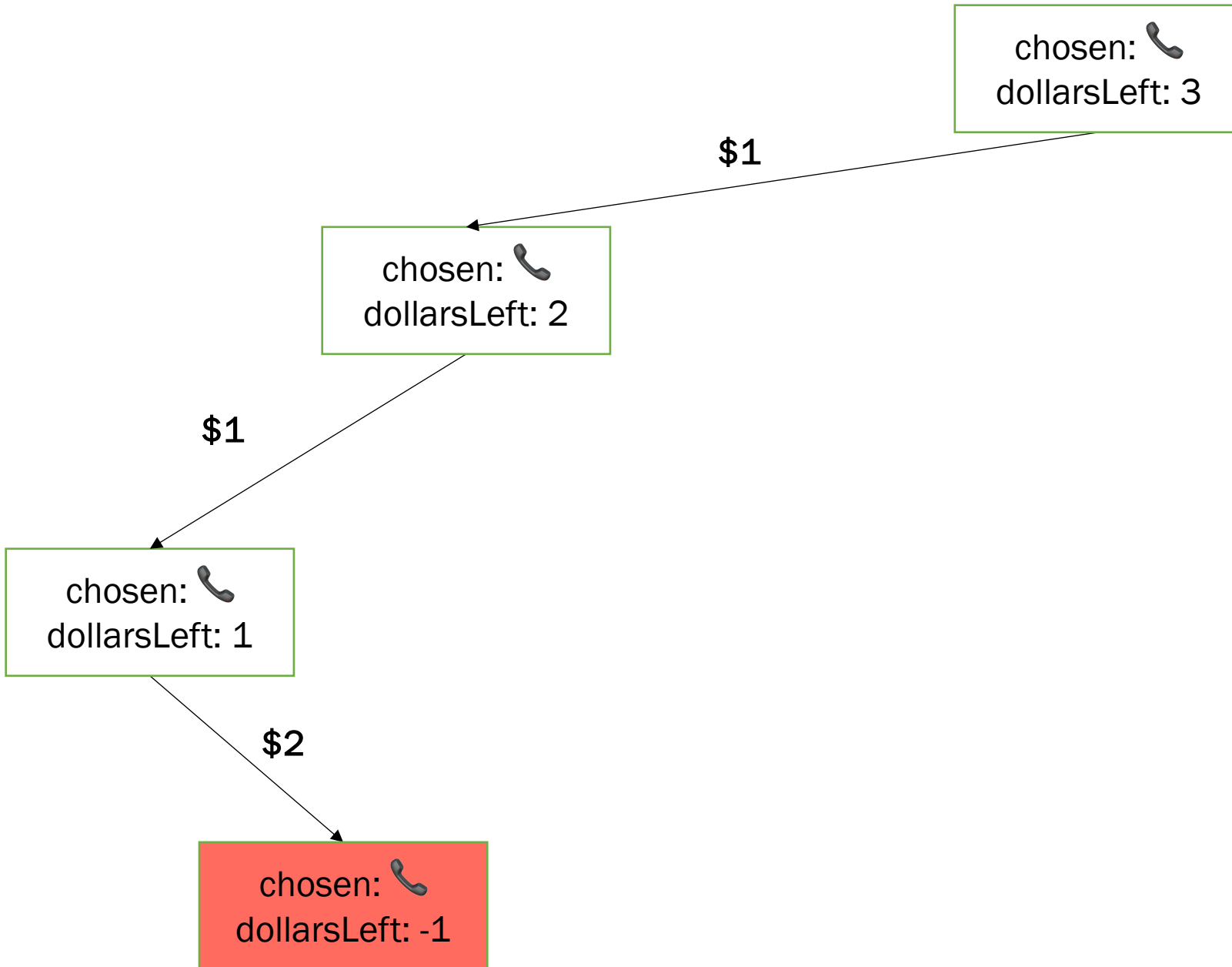


Output:  
[1, 1, 1]

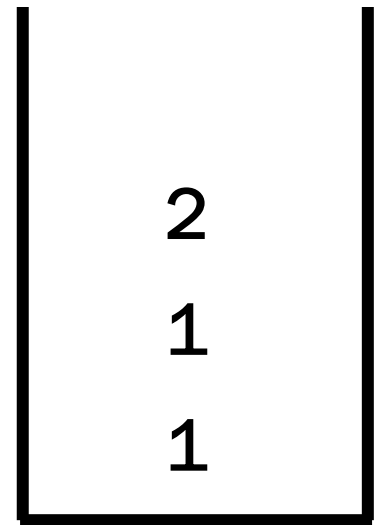
2  
1  
1

chosen

Phone Number: 425-123-4567



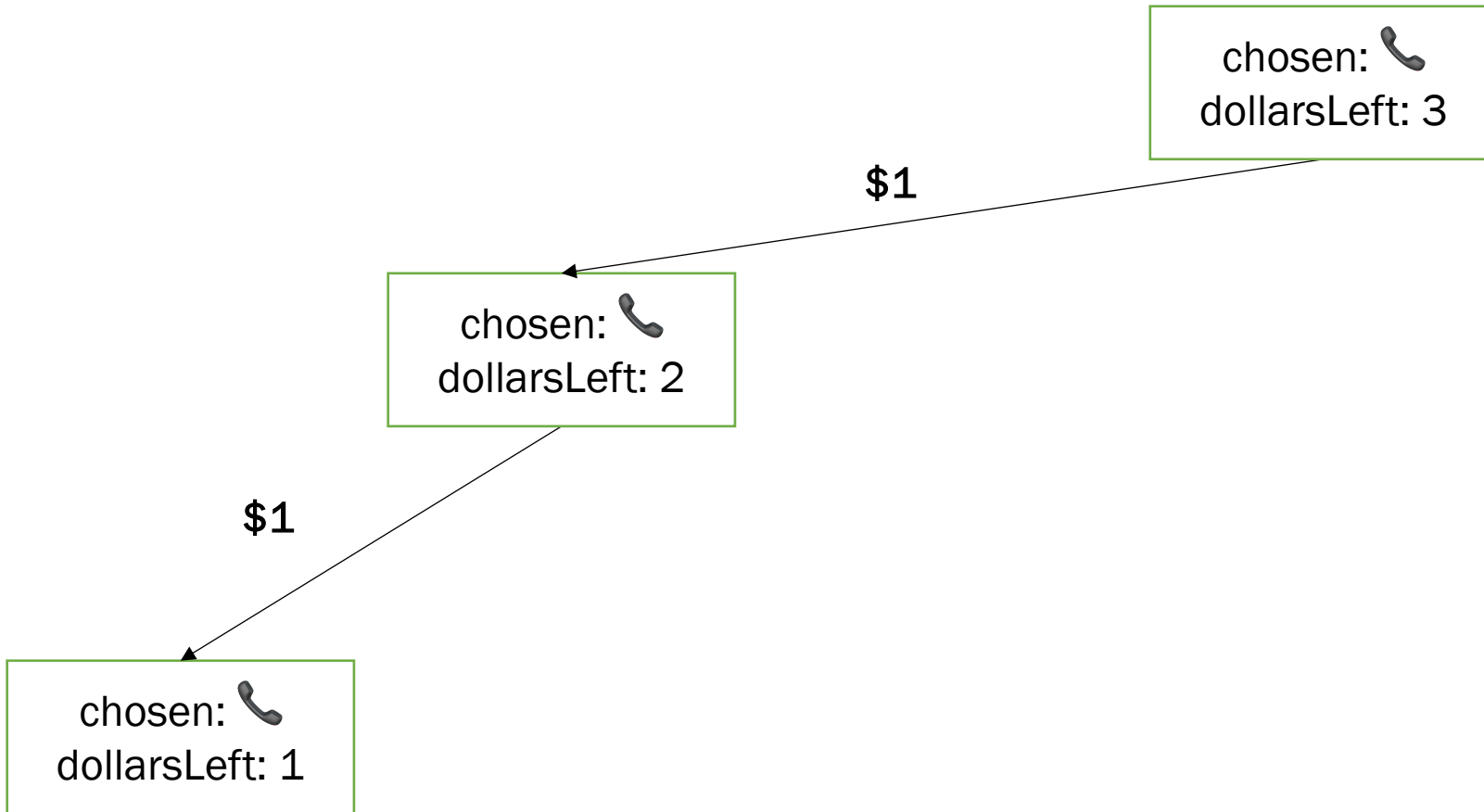
Output:  
[1, 1, 1]



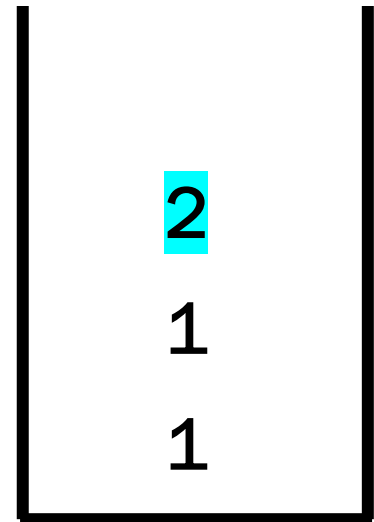
chosen

Phone Number: 425-123-4567



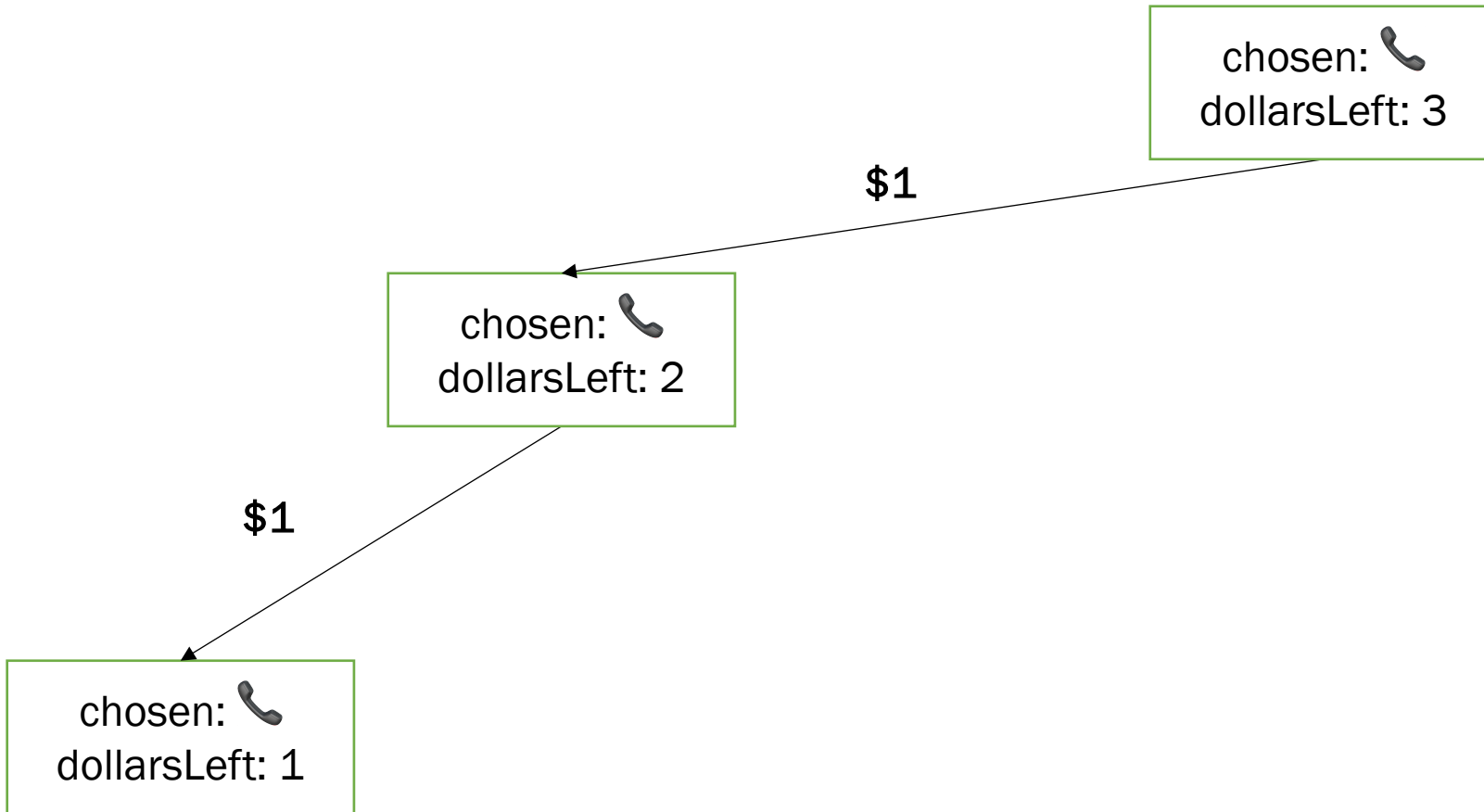


Output:  
[1, 1, 1]

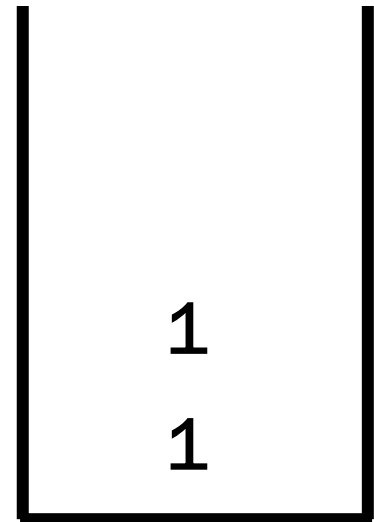


chosen

Phone Number: 425-123-4567

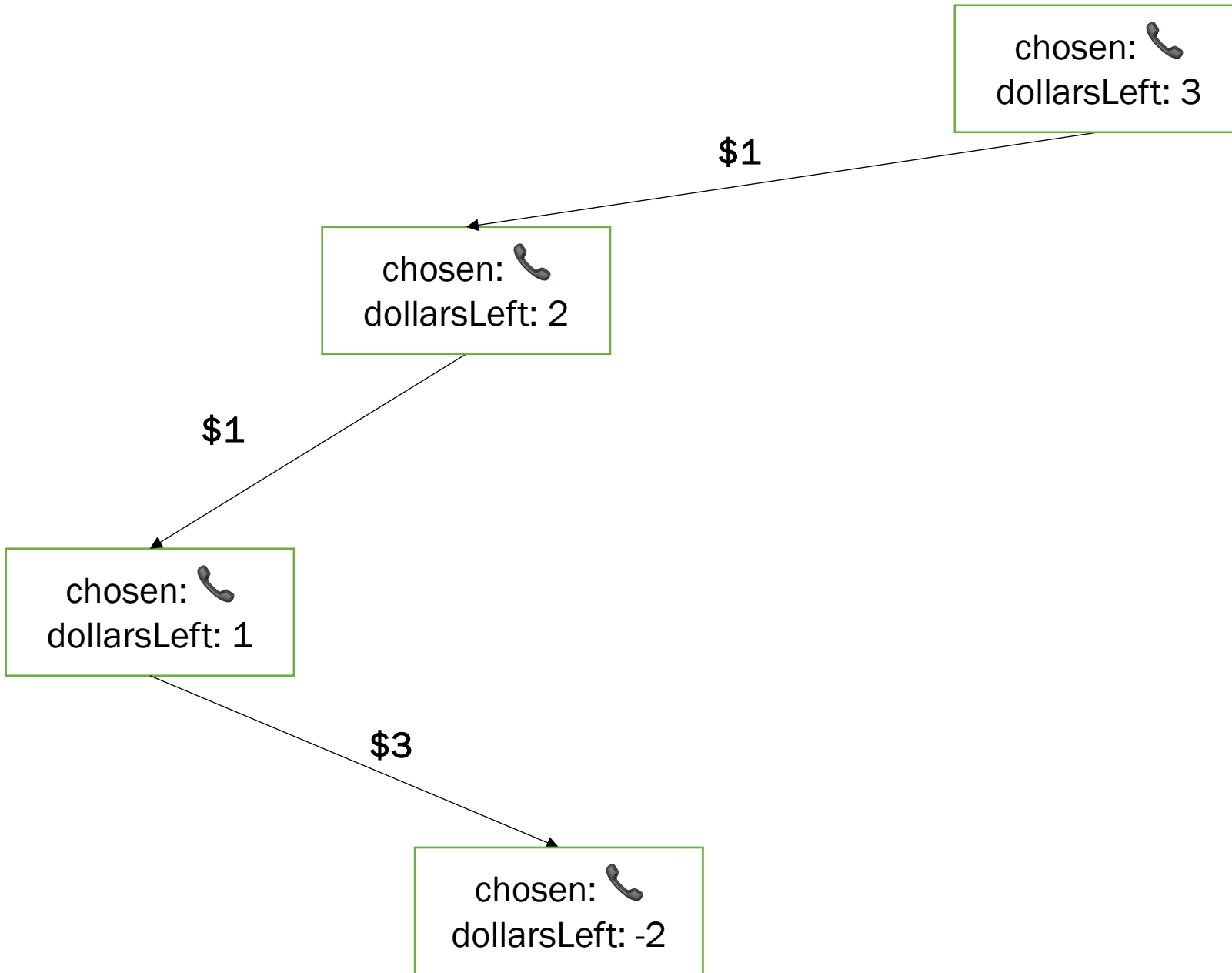


Output:  
[1, 1, 1]



chosen

Phone Number: 425-123-4567

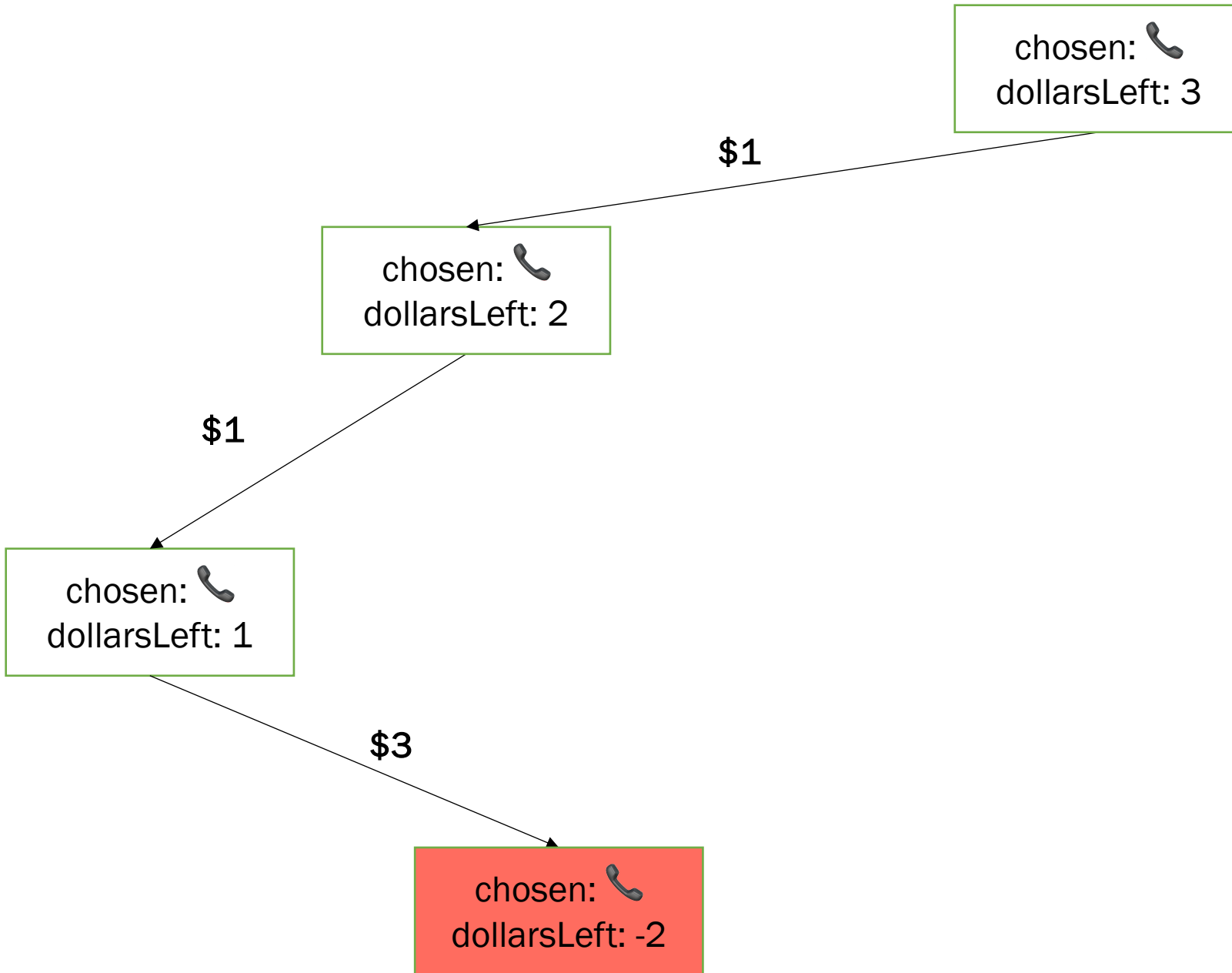


Output:  
[1, 1, 1]

3  
1  
1

chosen

Phone Number: 425-123-4567

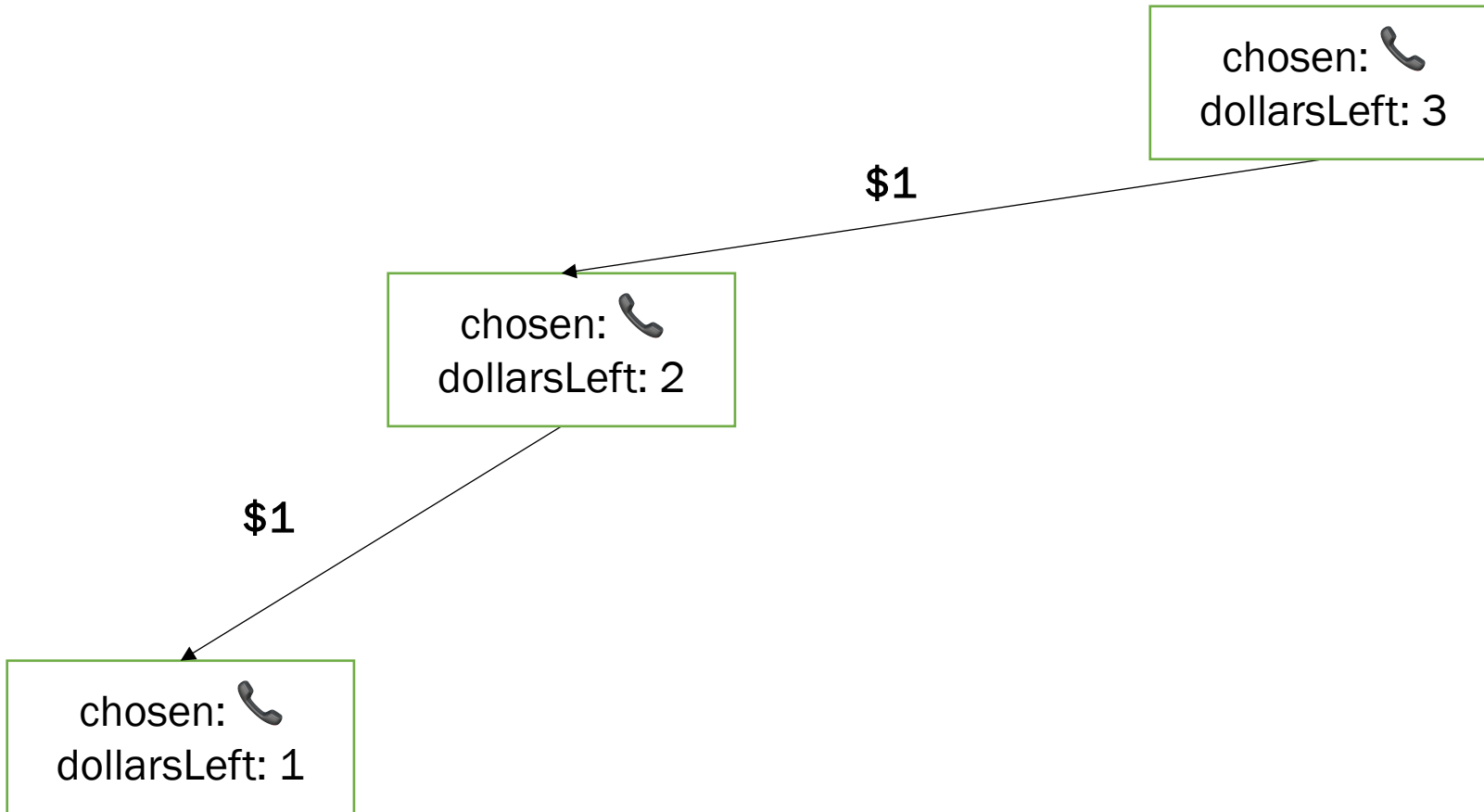


Output:  
[1, 1, 1]

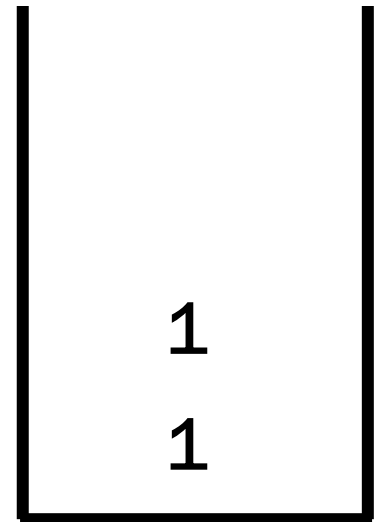
3  
1  
1

chosen

Phone Number: 425-123-4567

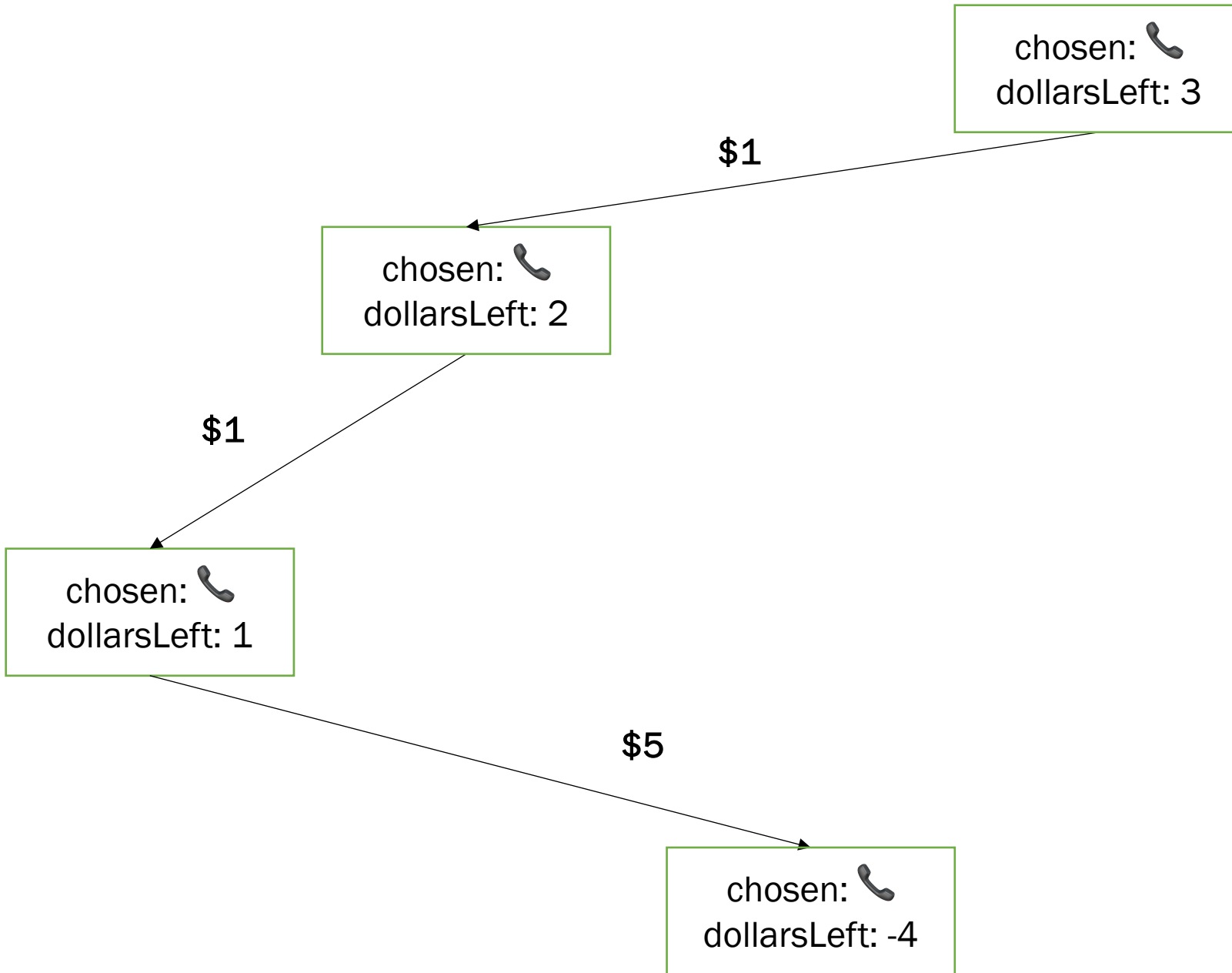


Output:  
[1, 1, 1]



chosen

Phone Number: 425-123-4567

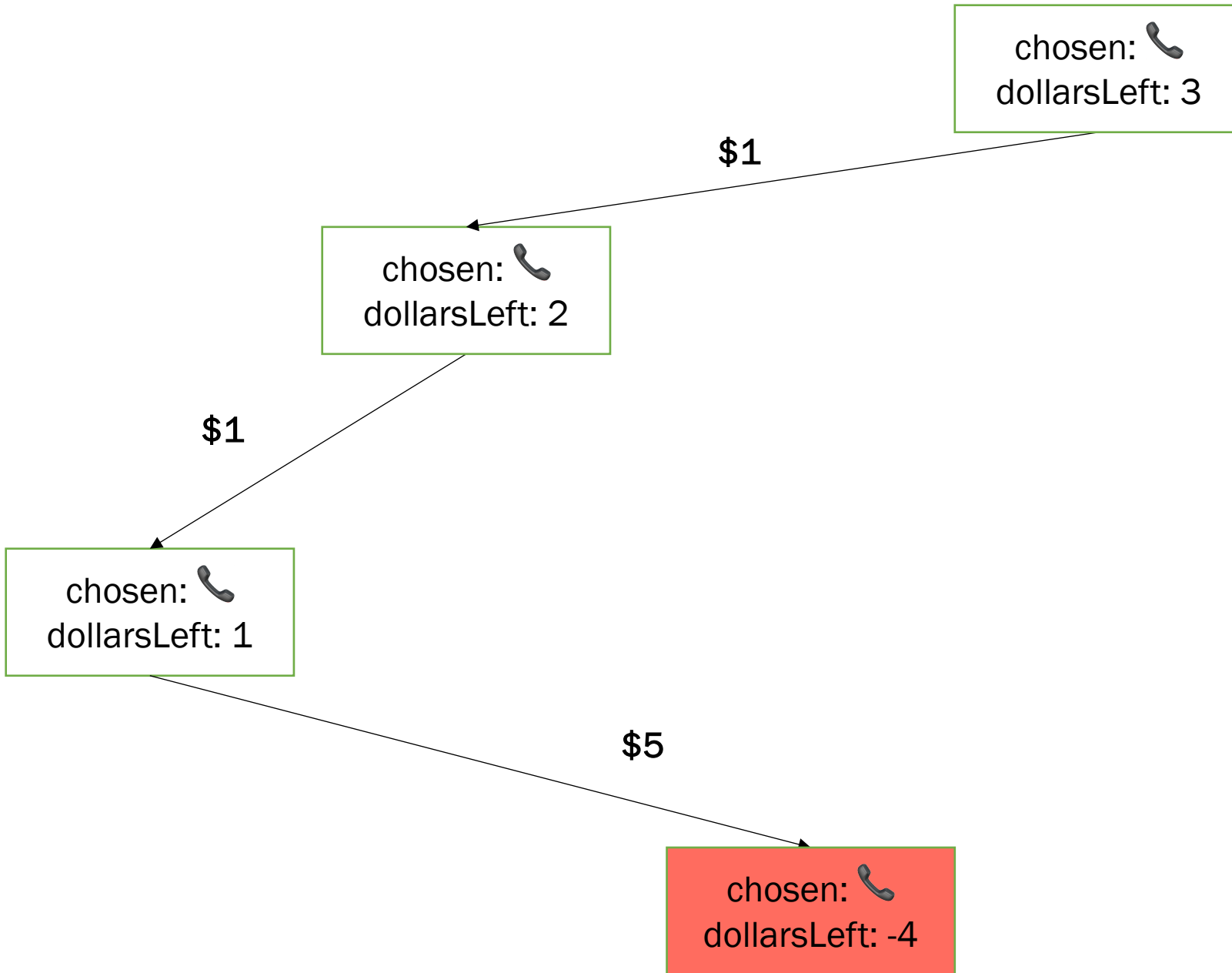


Output:  
[1, 1, 1]

5  
1  
1

chosen

Phone Number: 425-123-4567

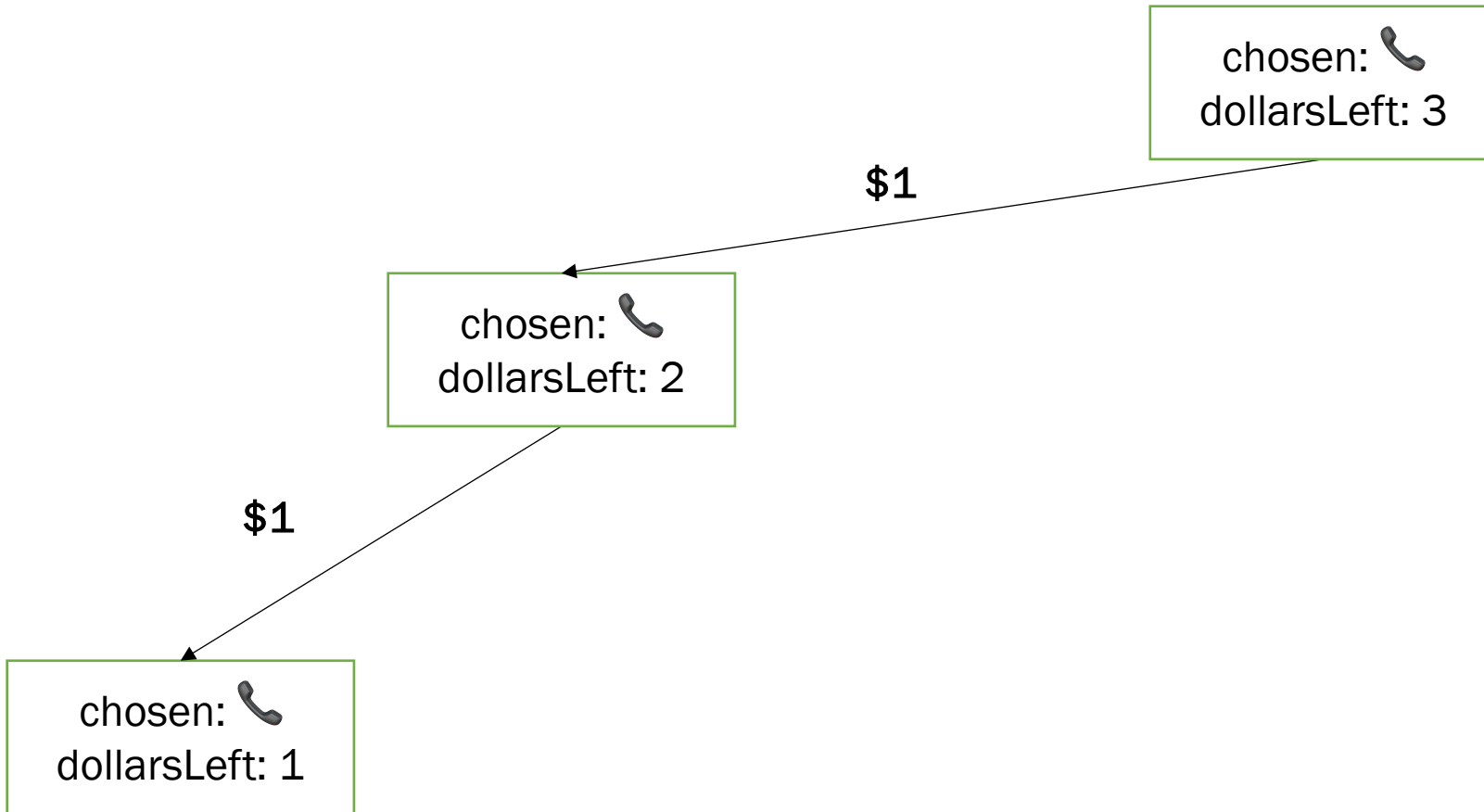


Output:  
[1, 1, 1]

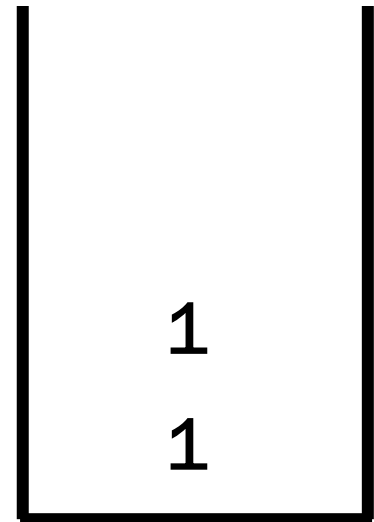
5  
1  
1

chosen

Phone Number: 425-123-4567



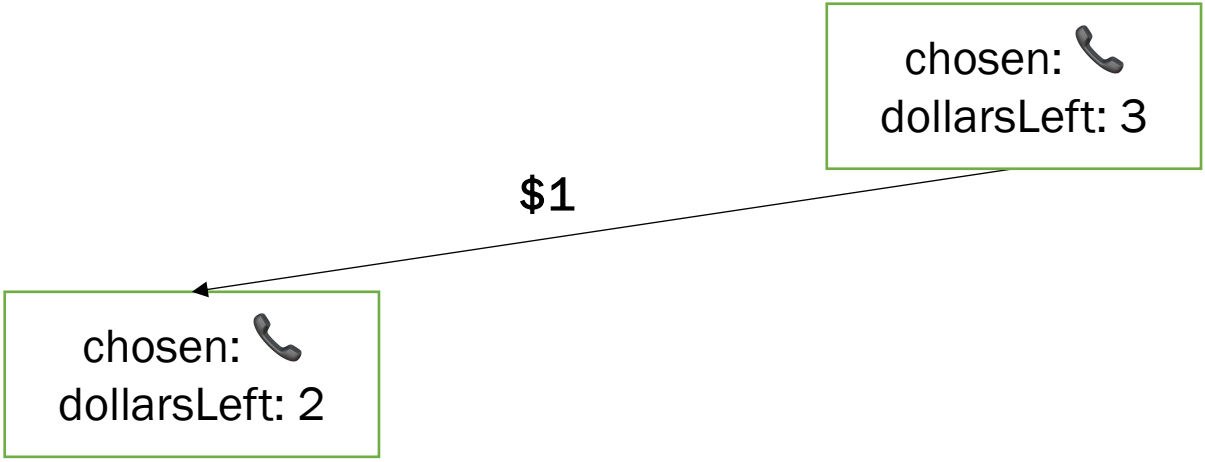
Output:  
[1, 1, 1]



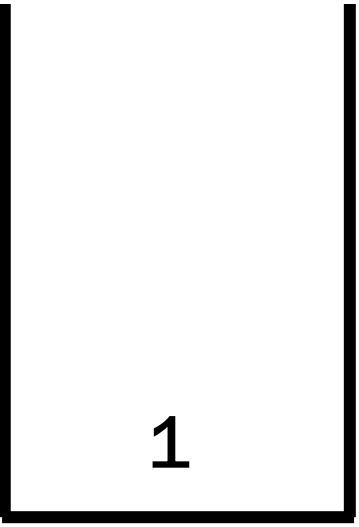
chosen

Phone Number: 425-123-4567



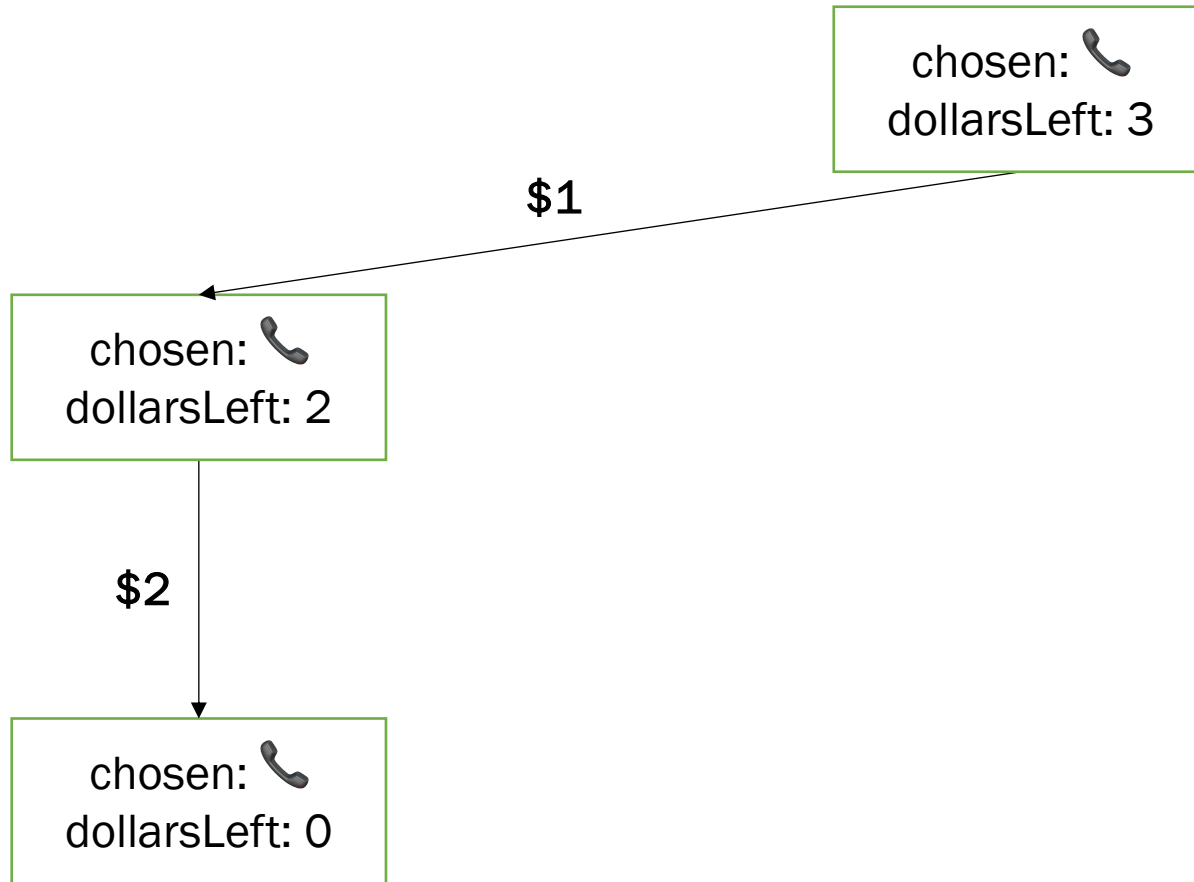


Output:  
[1, 1, 1]

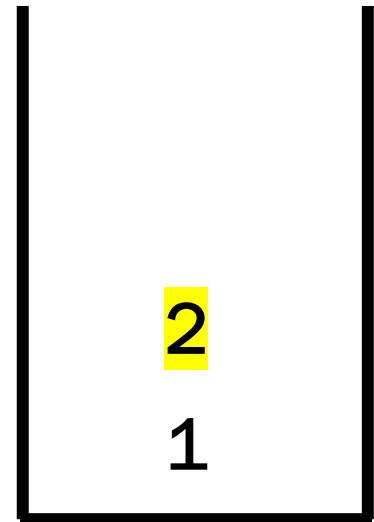


chosen

Phone Number: 425-123-4567

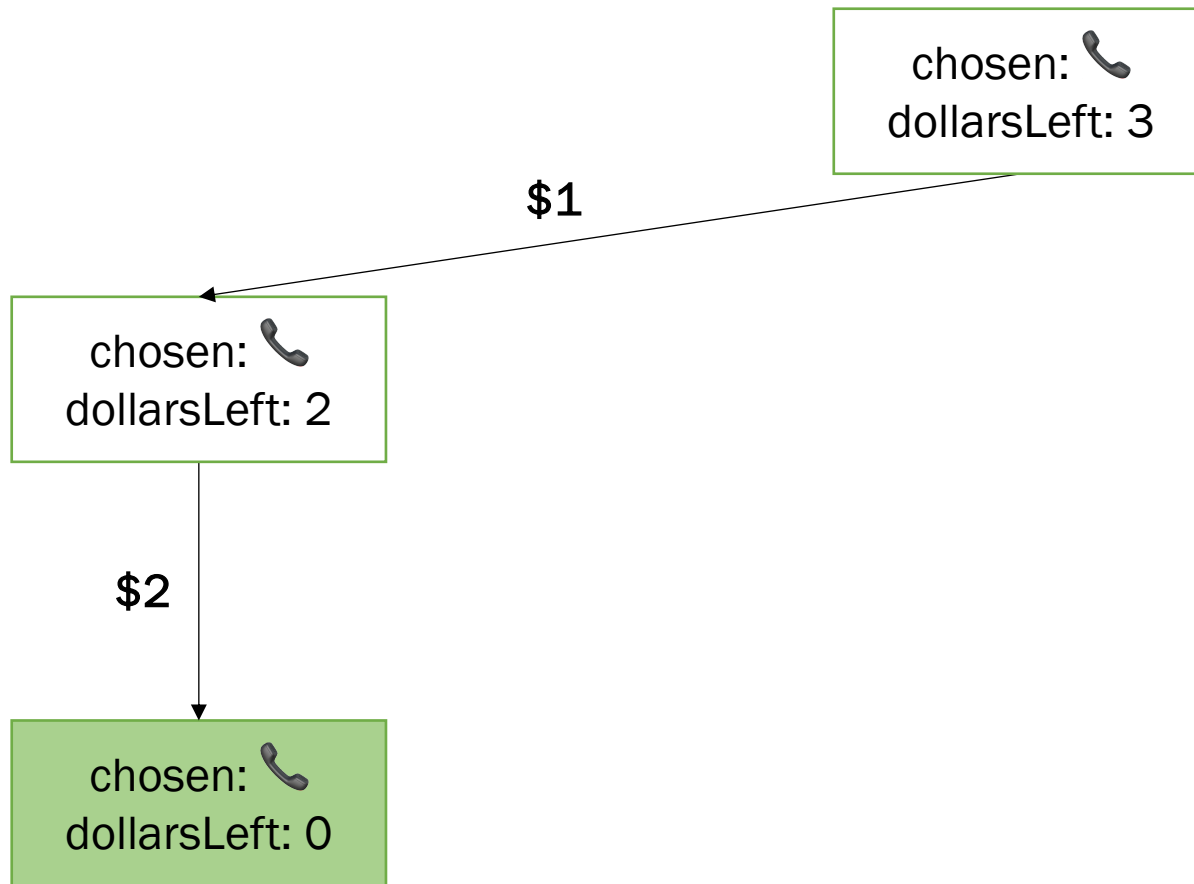


Output:  
[1, 1, 1]

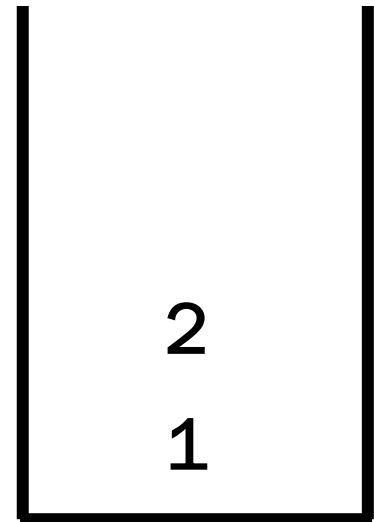


chosen

Phone Number: 425-123-4567



Output:  
[1, 1, 1]  
[1, 2]



chosen

Phone Number: 425-123-4567

chosen: 📞  
dollarsLeft: 3

\$1

\$2

\$3

\$5

chosen: 📞  
dollarsLeft: 2

chosen: 📞  
dollarsLeft: 1

chosen: 📞  
dollarsLeft: 0

chosen: 📞  
dollarsLeft: -2

\$1

\$2

\$3

\$5

\$1

\$2

\$3

\$5

chosen: 📞  
dollarsLeft: 1

chosen: 📞  
dollarsLeft: 0

chosen: 📞  
dollarsLeft: -1

chosen: 📞  
dollarsLeft: -3

chosen: 📞  
dollarsLeft: 0

chosen: 📞  
dollarsLeft: -1

chosen: 📞  
dollarsLeft: -2

chosen: 📞  
dollarsLeft: -4

\$1

chosen: 📞  
dollarsLeft: 0

chosen: 📞  
dollarsLeft: 3

\$1

\$2

\$3

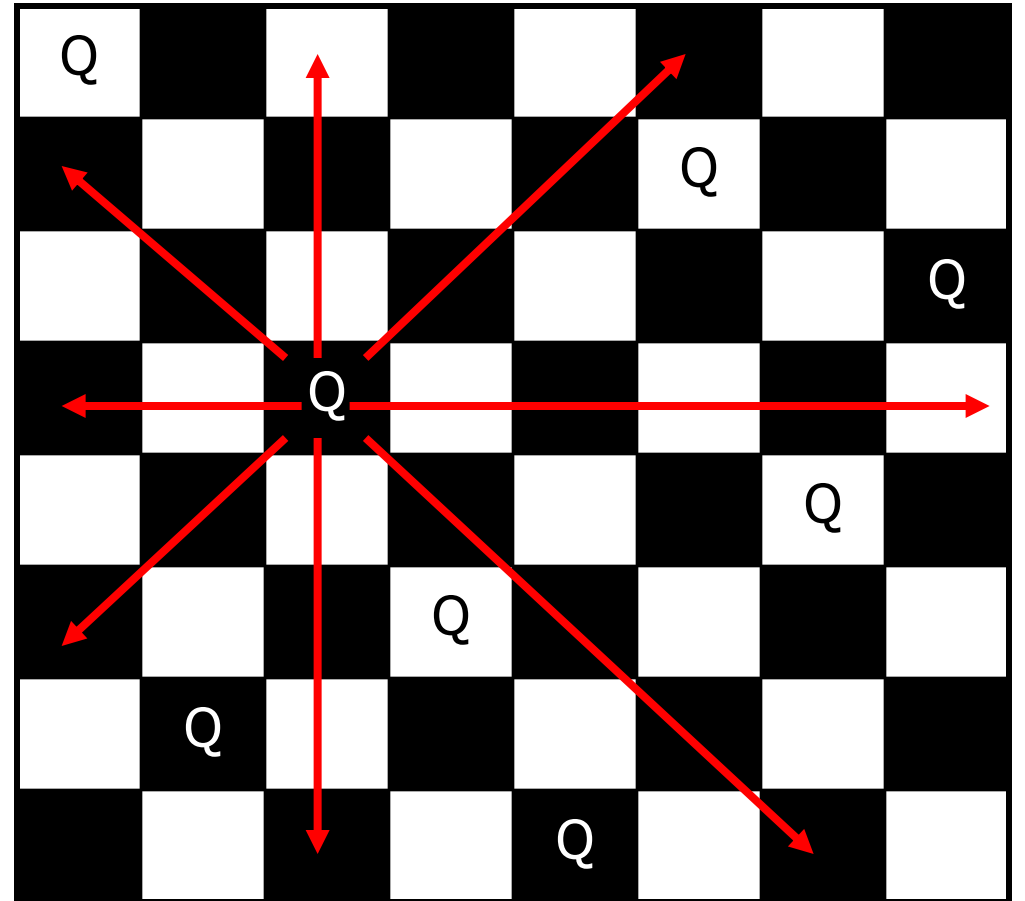
\$5

chosen: 📞  
dollarsLeft: -4

chosen: 📞  
dollarsLeft: 0

# The "8 Queens" problem

- Consider the problem of trying to place 8 queens on a chess board such that no queen can attack another queen.
  - What are the "choices"?
  - How do we "make" or "un-make" a choice?
  - How do we know when to stop?



# Naive algorithm

- for (each square on board):
  - Place a queen there.
  - Try to place the rest of the queens.
  - Un-place the queen.

	1	2	3	4	5	6	7	8
1	Q	...	...	...	...	...	...	...
2	...	...	...	...	...	...	...	...
3	...							
4								
5								
6								
7								
8								

# Better algorithm idea

- Observation: In a working solution, exactly 1 queen must appear in each column.
  - Redefine a "choice" to be valid placement of a queen in a particular column.

	1	2	3	4	5	6	7	8
1	Q	...	...					
2		...	...					
3		Q	...					
4			...					
5			Q					
6								
7								
8								



# solve

- Write a method `solve` that accepts a `Board` as a parameter and prints out all the ways to place `n` queens on it.

# Board class

	1	2	3	4	5	6	7	8
1	Q	...	...	...	...	...	...	...
2	...	...	...	...	...	...	...	...
3	...							
4								
5								
6								
7								
8								