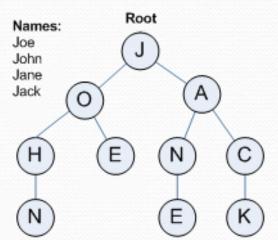
Building Java Programs

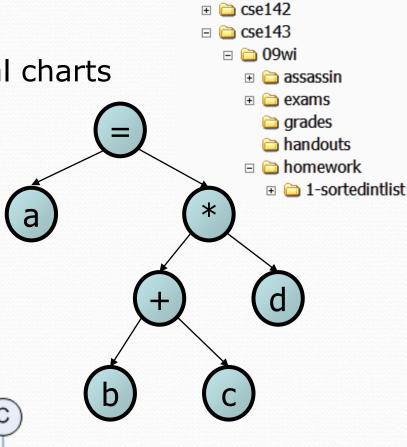
Binary Trees

reading: 17.1 - 17.3

Trees in computer science

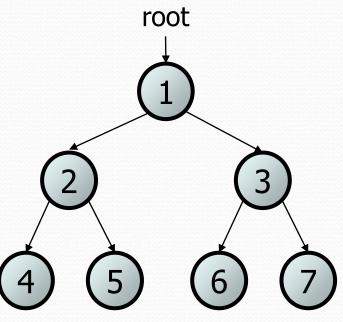
- TreeMap and TreeSet implementations
- folders/files on a computer
- family genealogy; organizational charts
- AI: decision trees
- compilers: parse tree
 - a = (b + c) * d;
- cell phone T9





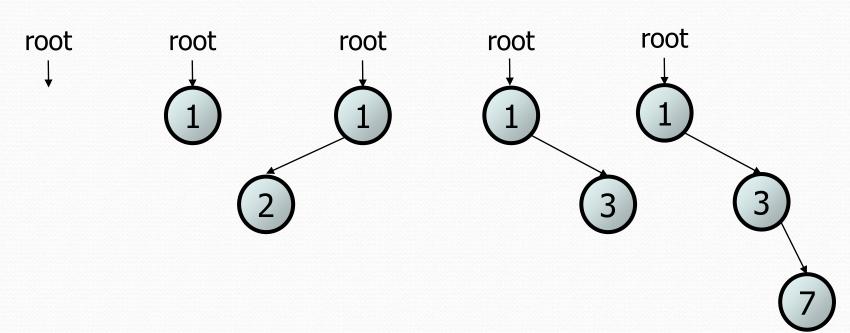
Trees

- tree: A directed, acyclic structure of linked nodes.
 - directed: Has one-way links between nodes.
 - acyclic: No path wraps back around to the same node twice.
- binary tree: One where each node has at most two children.
- Recursive definition: A tree is either:
 - empty (null), or
 - a root node that contains:
 - data,
 - a left subtree, and
 - a right subtree.
 - (The left and/or right subtree could be empty.)



Recursive data structure

- Recursive definition: A tree is either:
 - empty (null), or
 - a root node that contains:
 - data,
 - a left tree, and
 - a right tree

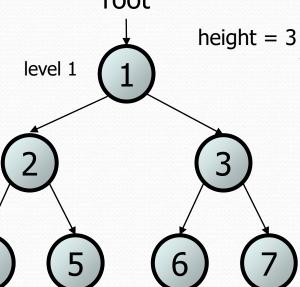


Terminology

- node: an object containing a data value and left/right children
 - root: topmost node of a tree
 - leaf: a node that has no children
 - branch: any internal node; neither the root nor a leaf root

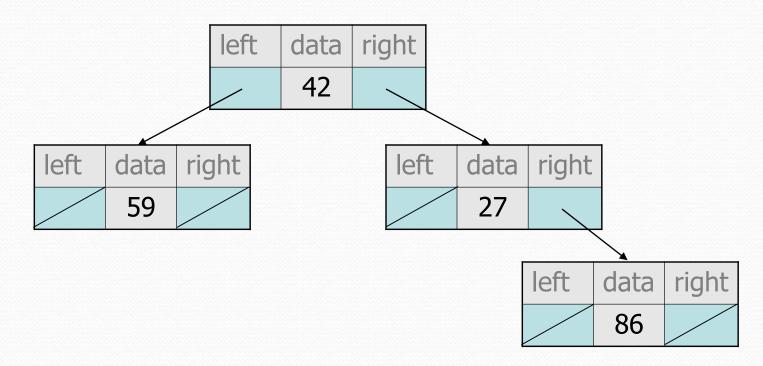
level 3 (4

- parent: a node that refers to this one
- child: a node that this node refers to
- **sibling**: a node with a common parent
- **subtree**: the smaller tree of nodes on level 2 the left or right of the current node
- height: length of the longest path from the root to any node
- level or depth: length of the path from a root to a given node



A tree node for integers

- A basic tree node object stores data, refers to left/right
 - Multiple nodes can be linked together into a larger tree



IntTreeNode class

```
// An IntTreeNode object is one node in a binary tree of ints.
public class IntTreeNode {
                        // data stored at this node
   public int data;
    public IntTreeNode left;  // reference to left subtree
    public IntTreeNode right; // reference to right subtree
    // Constructs a leaf node with the given data.
    public IntTreeNode(int data) {
        this (data, null, null);
    // Constructs a branch node with the given data and links.
    public IntTreeNode (int data, IntTreeNode left,
                                 IntTreeNode right) {
        this.data = data;
        this.left = left;
        this.right = right;
                                                           right
                                                 left
                                                      data
```

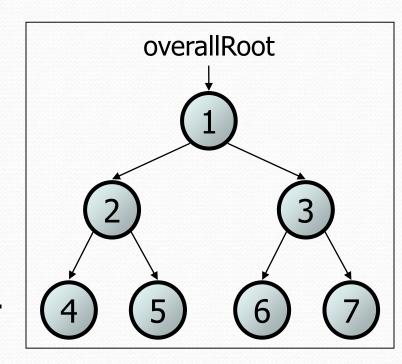
IntTree class

```
// An IntTree object represents an entire binary tree of ints.
public class IntTree {
    private IntTreeNode overallRoot; // null for an empty tree
```

methods

}

- Client code talks to the IntTree,
 not to the node objects inside it.
- Methods of the IntTree create and manipulate the nodes, their data and links between them.



Print IntTree

 We want to write a method that prints out the contents of an IntTree.

overallRoot

Here is the output we want

```
17 41 29 6 9 81 40

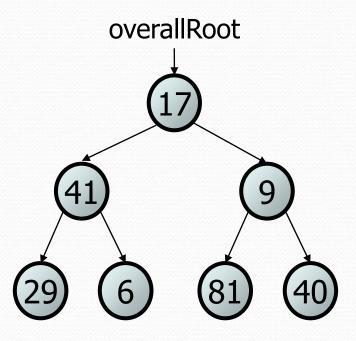
private void print(IntTreeNode root) {
   if (root != null) {
        System.out.print(root.data + " ");
        print(root.left);
        print(root.right);
   }
}
```

Traversals

- Orderings for traversals
 - pre-order: process root node, then its left/right subtrees
 - in-order: process left subtree, then root node, then right
 - post-order: process left/right subtrees, then root node

```
private void print(IntTreeNode root) {
    if (root != null) {
        System.out.print(root.data + " ");
        print(root.left);
        print(root.right);
    }
}
```

• pre-order: 17 41 29 6 9 81 40

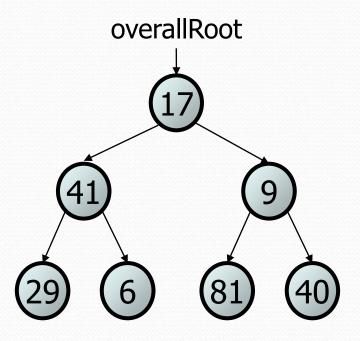


Traversals

- Orderings for traversals
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```
private void print(IntTreeNode root) {
    if (root != null) {
        print(root.left);
        System.out.print(root.data + " ");
        print(root.right);
    }
}
```

• in-order: 29 41 6 17 81 9 40

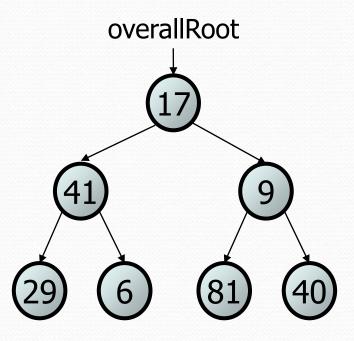


Traversals

- Orderings for traversals
 - pre-order: process root node, then its left/right subtrees
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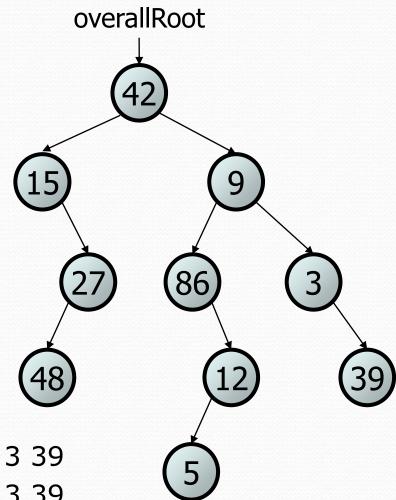
```
private void print(IntTreeNode root) {
    if (root != null) {
        print(root.left);
        print(root.right);
        System.out.print(root.data + " ");
    }
}
```

• post-order: 29 6 41 81 40 9 17



Exercise

 Give pre-, in-, and post-order traversals for the following tree:



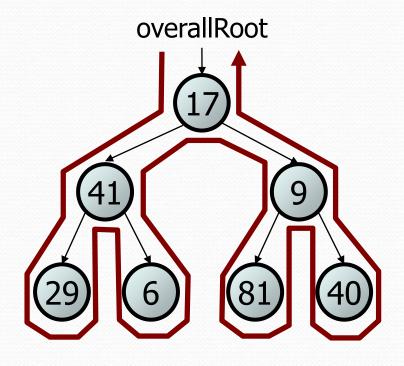
- pre: 42 15 27 48 9 86 12 5 3 39

- in: 15 48 27 42 86 5 12 9 3 39

- post: 48 27 15 5 12 86 39 3 42

Traversal trick

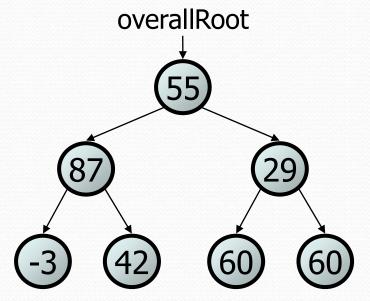
- To quickly generate a traversal:
 - Trace a path around the tree.
 - As you pass a node on the proper side, process it.
 - pre-order: left side
 - in-order: bottom
 - post-order: right side



- pre-order: 17 41 29 6 9 81 40
- in-order: 29 41 6 17 81 9 40
- post-order: 29 6 41 81 40 9 17

Exercise

- Add a method contains to the IntTree class that searches the tree for a given integer, returning true if it is found.
 - If an IntTree variable tree referred to the tree below, the following calls would have these results:
 - tree.contains(87) \rightarrow true
 - tree.contains(60) \rightarrow true
 - tree.contains(63) \rightarrow false
 - tree.contains(42) \rightarrow false



Exercise solution

```
// Returns whether this tree contains the given integer.
public boolean contains(int value) {
    return contains (overallRoot, value);
private boolean contains(IntTreeNode node, int value) {
    if (node == null) {
        return false; // base case: not found here
    } else if (node.data == value) {
        return true; // base case: found here
    } else {
        // recursive case: search left/right subtrees
        return contains (node.left, value) | |
               contains(node.right, value);
```

Template for tree methods

```
public class IntTree {
    private IntTreeNode overallRoot;
    ...

public type name(parameters) {
        name(overallRoot, parameters);
    }

private type name(IntTreeNode root, parameters) {
        ...
    }
}
```

- Tree methods are often implemented recursively
 - with a public/private pair
 - the private version accepts the root node to process