



Exercise: Dice roll sum

- Write a method `diceSum` similar to `diceRoll`, but it also accepts a desired sum and prints only arrangements that add up to exactly that sum.

```
diceSum(2, 7);
```

```
[1, 6]  
[2, 5]  
[3, 4]  
[4, 3]  
[5, 2]  
[6, 1]
```

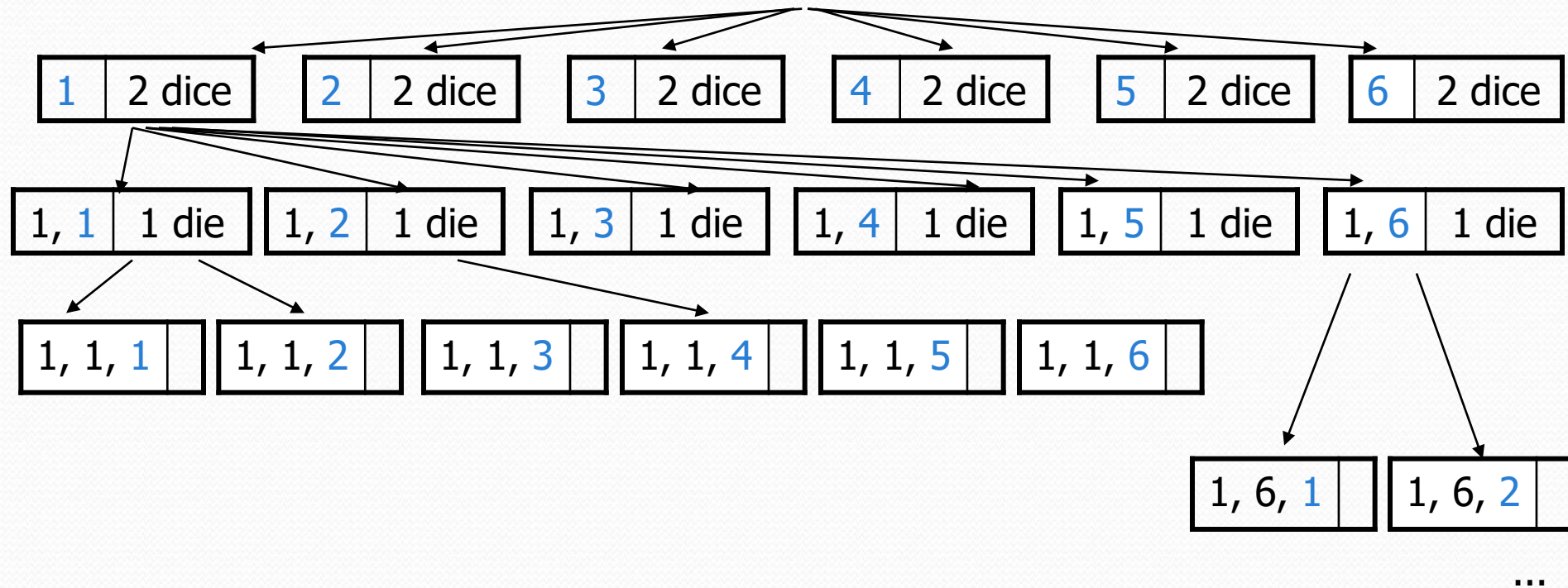


```
diceSum(3, 7);
```

```
[1, 1, 5]  
[1, 2, 4]  
[1, 3, 3]  
[1, 4, 2]  
[1, 5, 1]  
[2, 1, 4]  
[2, 2, 3]  
[2, 3, 2]  
[2, 4, 1]  
[3, 1, 3]  
[3, 2, 2]  
[3, 3, 1]  
[4, 1, 2]  
[4, 2, 1]  
[5, 1, 1]
```

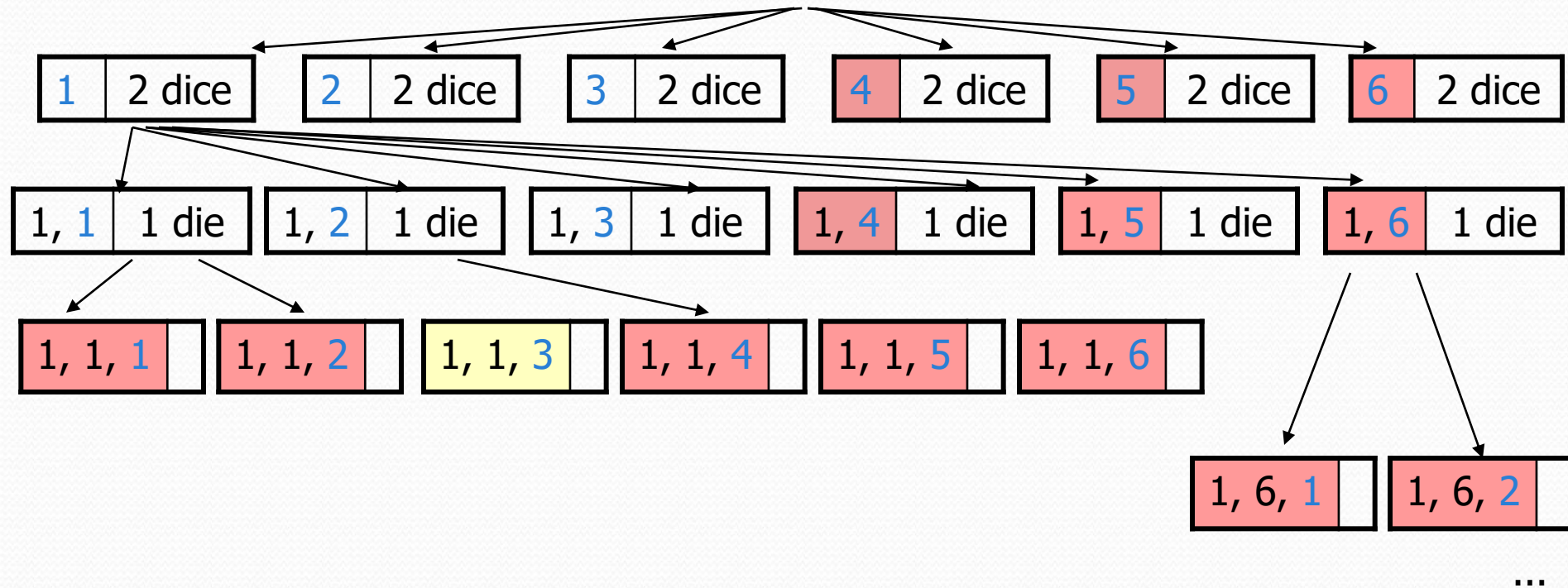
Consider all paths?

chosen	available	desired sum
-	3 dice	5



New decision tree

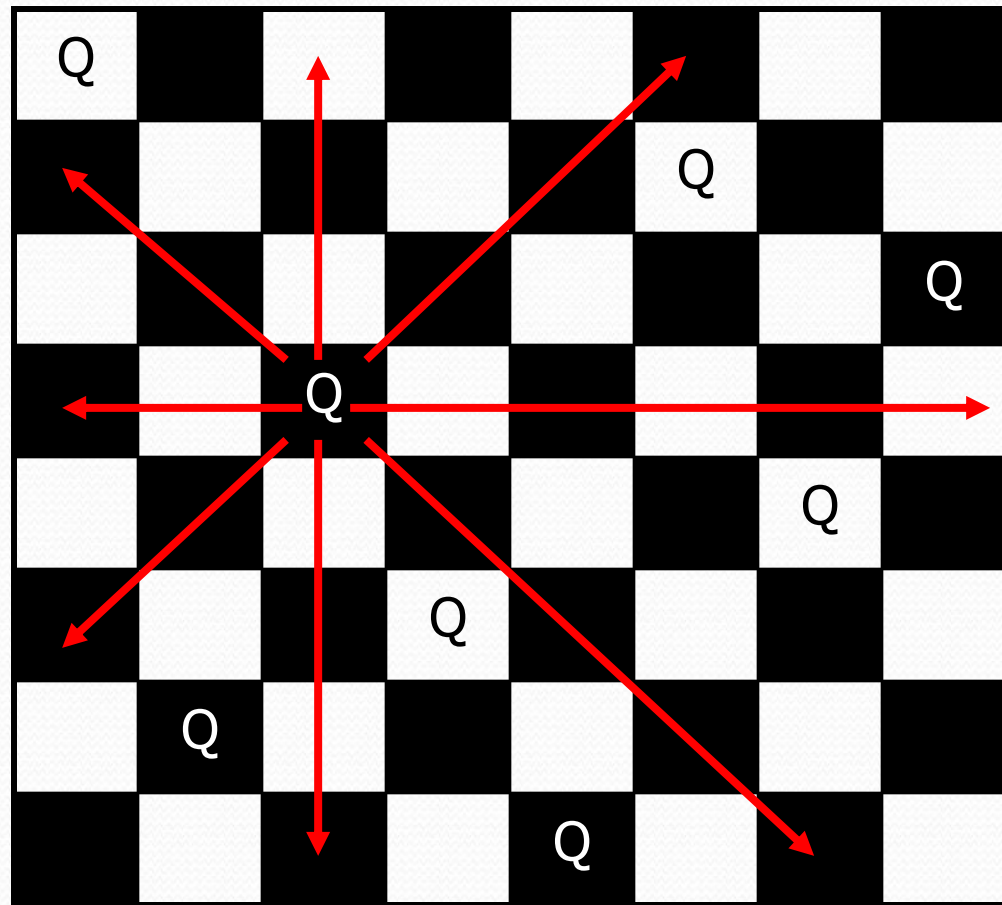
chosen	available	desired sum
-	3 dice	5



The "8 Queens" problem

- Consider the problem of trying to place 8 queens on a chess board such that no queen can attack another queen.

- What are the "choices"?
- How do we "make" or "un-make" a choice?
- How do we know when to stop?



Naive algorithm

• for (each square on board):

- Place a queen there.
- Try to place the rest of the queens.
- Un-place the queen.

- How large is the solution space for this algorithm?
 - $64 * 63 * 62 * \dots$

	1	2	3	4	5	6	7	8
1	Q
2
3	...							
4								
5								
6								
7								
8								

Better algorithm idea

- Observation: In a working solution, exactly 1 queen must appear in each row and in each column.

- Redefine a "choice" to be valid placement of a queen in a particular column.

- How large is the solution space now?

- $8 * 8 * 8 * \dots$

	1	2	3	4	5	6	7	8
1	Q					
2						
3		Q	...					
4			...					
5			Q					
6								
7								
8								

Exercise

- Suppose we have a `Board` class with these methods:

Method/Constructor	Description
<code>public Board(int size)</code>	construct empty board
<code>public boolean isSafe(int row, int column)</code>	true if queen can be safely placed here
<code>public void place(int row, int column)</code>	place queen here
<code>public void remove(int row, int column)</code>	remove queen from here
<code>public String toString()</code>	text display of board

- Write a method `solveQueens` that accepts a `Board` as a parameter and tries to place 8 queens on it safely.