Building Java Programs

Chapter 13 binary search and complexity

reading: 13.1-13.2



Road Map <u>Java Language</u>

CS Concepts

- Client/Implementer
- Efficiency
- Recursion
- Regular Expressions
- Grammars
- Sorting
- Backtracking
- Hashing
- Huffman Compression

Data Structures

- Lists
- Stacks
- Queues
- Sets
- Maps
- Priority Queues

Exceptions

- Interfaces
- References
- Comparable
- Generics
- Inheritance/Polymorphism
- Abstract Classes

Java Collections

- Arrays
- ArrayList 🛠
- LinkedList 🛠
- Stack
- TreeSet / TreeMap
- HashSet / HashMap
- PriorityQueue

Sum this up for me

• Let's write a method to calculate the sum from 1 to some n public static int sum1(int n) {

```
int sum = 0;
for (int i = 1; i <= n; i++) {
    sum += i;
}
return sum;
}
```

```
Gauss also has a way of solving this
public static int sum2(int n) {
return n * (n + 1) / 2;
}
```

• Which one is more efficient?

Runtime Efficiency (13.2)

- efficiency: measure of computing resources used by code.
 - can be relative to speed (time), memory (space), etc.
 - most commonly refers to run time
- We want to be able to compare different algorithms to see which is more efficient

Efficiency Try 1

Let's time the methods!

n = 1	sum1	took	Oms,	sum2	took	Oms
n = 5	sum1	took	Oms,	sum2	took	0ms
n = 10	sum1	took	Oms,	sum2	took	0ms
n = 100	sum1	took	Oms,	sum2	took	0ms
n = 1,000	sum1	took	Oms,	sum2	took	0ms
n = 10,000,000	sum1	took	10ms,	sum2	took	0ms
n = 100,000,000	sum1	took	123ms,	sum2	took	0ms
n = 2, 147, 483, 647	sum1	took1	800ms,	sum2	took	0ms

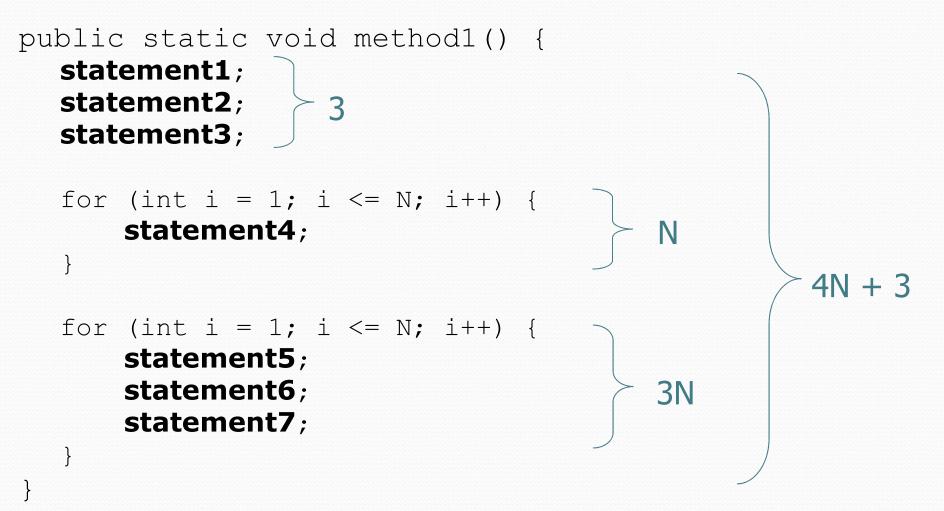
Downsides

- Different computers give different run times
- The same computer gives different results!!! D:<

Efficiency – Try 2

- Count number of "simple steps" our algorithm takes to run
- Assume the following:
 - Any single Java statement takes same amount of time to run.
 - int x = 5;
 - boolean b = (5 + 1 * 2) < 15 + 3;
 - System.out.println("Hello");
 - A loop's runtime, if the loop repeats N times, is N times the runtime of the statements in its body.
 - A method call's runtime is measured by the total runtime of the statements inside the method's body.

Efficiency examples



Efficiency examples 2

```
public static void method2() {
  for (int i = 1; i <= N; i++) {
      for (int j = 1; j <= N; j++) {
                                            N2
          statement1;
                                                   N^{2} + 4N
  for (int i = 1; i \le N; i++) {
      statement2;
      statement3;
                                            4N
      statement4;
      statement5;
```

How many statements will execute if N = 10? If N = 1000?

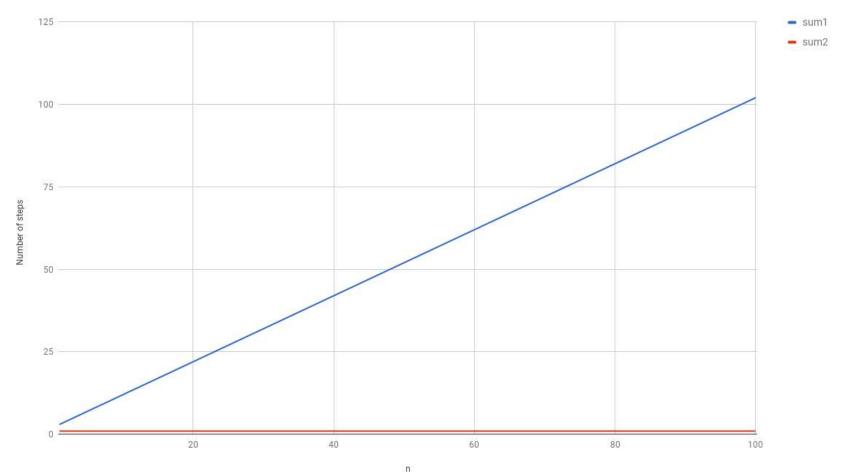
Sum this up for me

 Let's write a method to calculate the sum from 1 to some n public static int sum1(int n) { int sum = 0; $\}$ 1 for (int i = 1; i <= n; i++) { Ν N + 2sum += i; return sum; $\}$ 1 } Gauss also has a way of solving this public static int sum2(int n) { return n * (n + 1) / 2; $\}$ 1 }

• Which one is more efficient?

Visualizing Difference

Comparing sum1 and sum2



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Algorithm growth rates (13.2)

- We measure runtime in proportion to the input data size, N.
 - growth rate: Change in runtime as N changes.
- Say an algorithm runs 0.4N³ + 25N² + 8N + 17 statements.
 - Consider the runtime when N is *extremely large* .
 - We ignore constants like 25 because they are tiny next to N.
 - The highest-order term (N³) dominates the overall runtime.

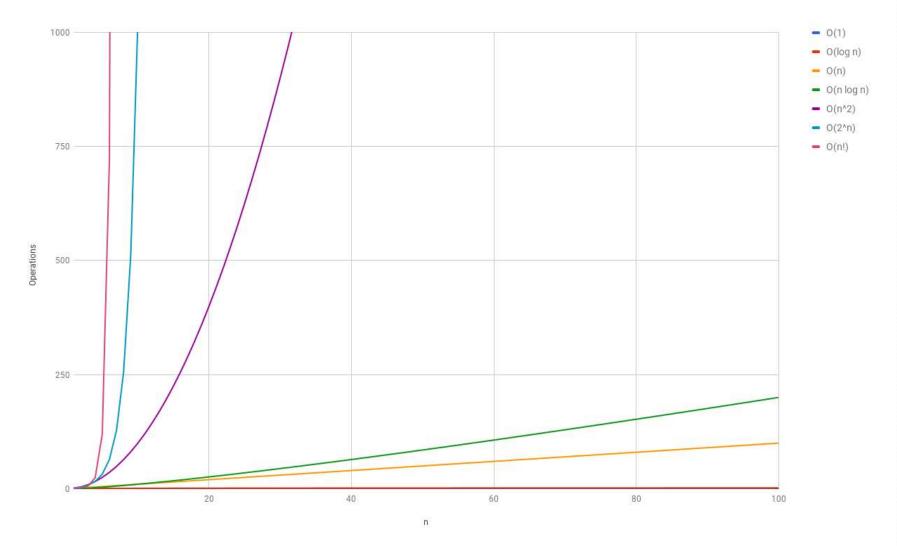
- We say that this algorithm runs "on the order of" N³.
- or **O(N³)** for short ("**Big-Oh** of N cubed")

Complexity classes

 complexity class: A category of algorithm efficiency based on the algorithm's relationship to the input size N.

Class	Big-Oh	If you double N,	Example
constant	O(1)	unchanged	10ms
logarithmic	O(log ₂ N)	increases slightly	175ms
linear	O(N)	doubles	3.2 sec
log-linear	O(N log ₂ N)	slightly more than doubles	6 sec
quadratic	O(N ²)	quadruples	1 min 42 sec
cubic	O(N ³)	multiplies by 8	55 min
		•••	
exponential	O(2 ^N)	multiplies drastically	5 * 10 ⁶¹ years

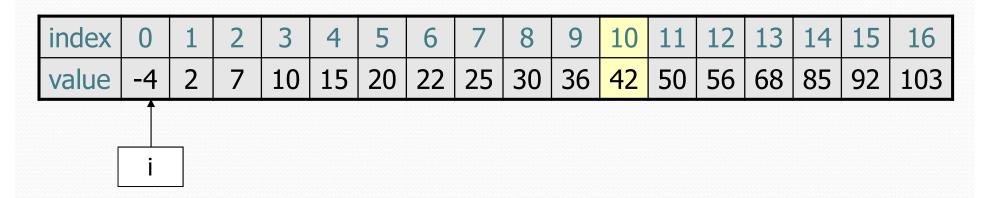
Complexity classes



http://recursive-design.com/blog/2010/12/07/comp-sci-101-big-o-notation/ - post about a Google interview 14

Sequential search

- sequential search: Locates a target value in an array / list by examining each element from start to finish. Used in indexOf.
 - How many elements will it need to examine?
 - Example: Searching the array below for the value **42**:



• The array is sorted. Could we take advantage of this?

Sequential search

• What is its complexity class?

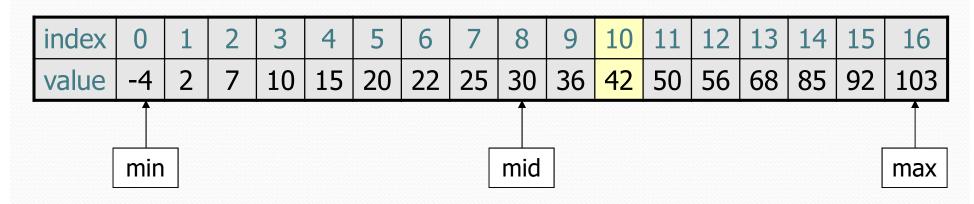
```
public int indexOf(int value) {
    for (int i = 0; i < size; i++) {
        if (elementData[i] == value) {
            return i;
        }
    }
    return -1; // not found
}</pre>
```

index	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
value	-4	2	7	10	15	20	22	25	30	36	42	50	56	68	85	92	103

- On average, "only" N/2 elements are visited
 - 1/2 is a constant that can be ignored

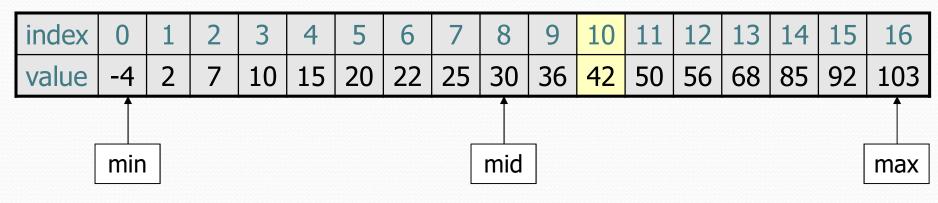
Binary search (13.1)

- binary search: Locates a target value in a sorted array or list by successively eliminating half of the array from consideration.
 - How many elements will it need to examine?
 - Example: Searching the array below for the value **42**:



Binary search

- binary search successively eliminates half of the elements.
 - Algorithm: Examine the middle element of the array.
 - If it is too big, eliminate the right half of the array and repeat.
 - If it is too small, eliminate the left half of the array and repeat.
 - Else it is the value we're searching for, so stop.
 - Which indexes does the algorithm examine to find value **42**?
 - What is the runtime complexity class of binary search?



Binary search runtime

 For an array of size N, it eliminates ¹/₂ until 1 element remains.

N, N/2, N/4, N/8, ..., 4, 2, 1

How many divisions does it take?

• Think of it from the other direction:

- How many times do I have to multiply by 2 to reach N?
 1, 2, 4, 8, ..., N/4, N/2, N
- Call this number of multiplications "x".

 $2^{\times} = N$ **x** = log₂ N

Binary search is in the logarithmic complexity class.

Collection efficiency

• Efficiency of our Java's ArrayList and LinkedList methods:

Method	ArrayList	LinkedList
add	O(1)*	O(1)
add(index, value)	O(N)	O(N)
indexOf	O(N)	O(N)
get	O(1)	O(N)
remove	O(N)	O(N)
set	O(1)	O(N)
size	O(1)	O(1)

* Most of the time!