# Building Java Programs 

Binary Trees

reading: 17.1 - 17.3


## Trees

- tree: A directed, acyclic structure of linked nodes.
- directed : Has one-way links between nodes.
- acyclic: No path wraps back around to the same node twice.
- binary tree: One where each node has at most two children.
- Recursive definition: A tree is either:
- empty (null), or
- a root node that contains:
- data,
- a left subtree, and
- a right subtree.
- (The left and/or right subtree could be empty.)



## Trees in computer science

－TreeMap and TreeSet implementations
－folders／files on a computer
－family genealogy；organizational charts
－AI：decision trees
－compilers：parse tree

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-a=(b+c) * d ;
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## Terminology

- node: an object containing a data value and left/right children
- root: topmost node of a tree
- leaf: a node that has no children
- branch: any internal node; neither the root nor a leaf
- parent: a node that refers to this one
- child: a node that this node refers to
- sibling: a node with a common parent
- subtree: the smaller tree of nodes on level 2 the left or right of the current node
- height: length of the longest path from the root to any node
- level or depth: length of the path
 from a root to a given node


## Recursive data structure

- Recursive definition: A tree is either:
- empty (null), or
- a root node that contains:
- data,
- a left tree, and
- a right tree



## A tree node for integers

- A basic tree node object stores data, refers to left/right
- Multiple nodes can be linked together into a larger tree



## IntTreeNode class

```
// An IntTreeNode object is one node in a binary tree of ints.
public class IntTreeNode {
    public int data; // data stored at this node
    public IntTreeNode left; // reference to left subtree
    public IntTreeNode right; // reference to right subtree
    // Constructs a leaf node with the given data.
    public IntTreeNode(int data) {
        this(data, null, null);
    }
    // Constructs a branch node with the given data and links.
    public IntTreeNode(int data, IntTreeNode left,
                        IntTreeNode right) {
        this.data = data;
        this.left = left;
        this.right = right;
    }
}
\begin{tabular}{|l|l|l|}
\hline left & data & right \\
\hline
\end{tabular}
```


## IntTree class

// An IntTree object represents an entire binary tree of ints.
public class IntTree \{
private IntTreeNode overallRoot; // null for an empty tree
methods

- Client code talks to the IntTree, not to the node objects inside it.
- Methods of the IntTree create and manipulate the nodes, their data and links between them.



## IntTree constructors

- For now, assume we have the following constructors:
public IntTree(IntTreeNode overallRoot)
public IntTree(int height)
- The 2nd constructor will create a tree and fill it with nodes with random data values overallRoot from 1-100 until it is full at the given height.

$$
\text { IntTree tree }=\text { new IntTree (3); }
$$



## Traversals

- traversal: An examination of the elements of a tree.
- A pattern used in many tree algorithms and methods
- Common orderings for traversals:
- pre-order: process root node, then its left/right subtrees
- in-order:
- post-order:
process left subtree, then root node, then right process left/right subtrees, then root node



## Traversal example



- pre-order: 174129698140
- in-order: 294161781940
- post-order: 296418140917


## Traversal trick

- To quickly generate a traversal:
- Trace a path around the tree.
- As you pass a node on the proper side, process it.
- pre-order: left side
- in-order: bottom
- post-order: right side

- pre-order: 174129698140
- in-order: 294161781940
- post-order: 296418140917


## Exercise

- Give pre-, in-, and post-order traversals for the following tree:



## Exercise

- Add a method print to the IntTree class that prints the elements of the tree, separated by spaces.
- A node's left subtree should be printed before it, and its right subtree should be printed after it.
- Example: tree.print();

294161781940


## Exercise solution

```
// An IntTree object represents an entire binary tree of ints.
public class IntTree {
    private IntTreeNode overallRoot; // null for an empty tree
    public void print() {
        print(overallRoot);
            System.out.println(); // end the line of output
    }
    private void print(IntTreeNode root) {
        // (base case is implicitly to do nothing on null)
        if (root != null) {
            // recursive case: print left, center, right
            print(overallRoot.left);
            System.out.print(overallRoot.data + " ");
            print(overallRoot.right);
    }
    }
}
```


## Template for tree methods

```
public class IntTree {
    private IntTreeNode overallRoot;
    ...
public type name (parameters) {
    name(overallRoot, parameters);
    }
    private type name(IntTreeNode root, parameters) {
    }
}
```

- Tree methods are often implemented recursively
- with a public/private pair
- the private version accepts the root node to process


## Exercise

- Add a method contains to the IntTree class that searches the tree for a given integer, returning true if it is found.

If an IntTree variable tree referred to the tree below, the following calls would have these results:

- tree.contains(87) true
- tree.contains (60) true
- tree.contains(63) false
- tree.contains(42) false



## Exercise solution

```
// Returns whether this tree contains the given integer.
public boolean contains(int value) {
        return contains(overallRoot, value);
}
private boolean contains(IntTreeNode node, int value) {
    if (node == null) {
        return false; // base case: not found here
    } else if (node.data == value) {
        return true; // base case: found here
    } else {
        // recursive case: search left/right subtrees
        return contains(node.left, value) ||
        contains(node.right, value);
    }
}
```


## Exercise

- Add a method named printSideways to the IntTree class that prints the tree in a sideways indented format, with right nodes above roots above left nodes, with each level 4 spaces more indented than the one above it.
- Example: Output from the tree below:
overall root



## Exercise solution

```
// Prints the tree in a sideways indented format.
public void printSideways() {
        printSideways(overallRoot, "");
}
private void printSideways(IntTreeNode root,
                                    String indent) {
    if (root != null) {
        printSideways(root.right, indent + " ");
        System.out.println(indent + root.data);
        printSideways(root.left, indent + " ");
    }
}
```

