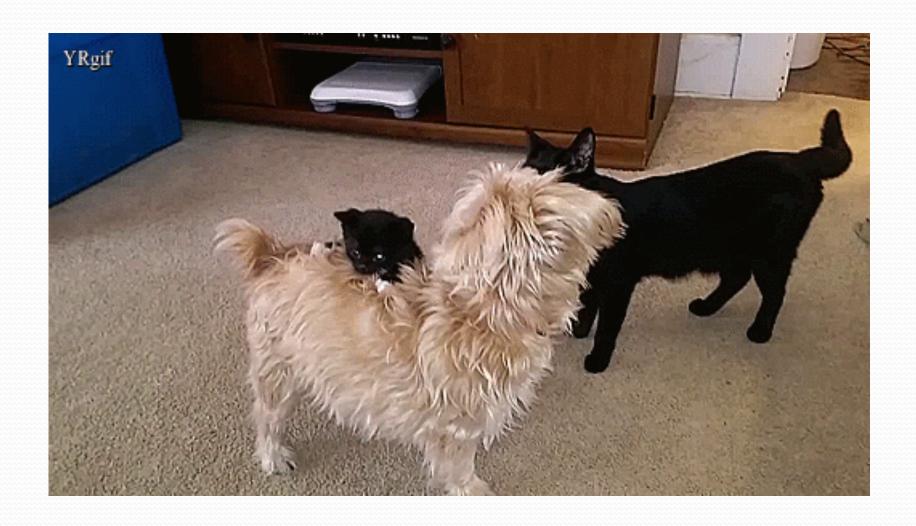
Building Java Programs

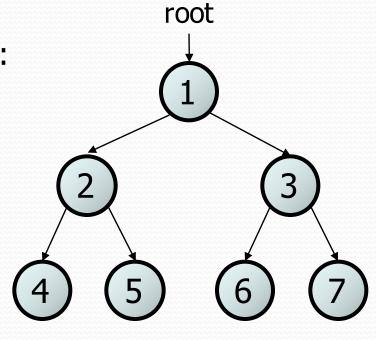
Binary Trees

reading: 17.1 - 17.3



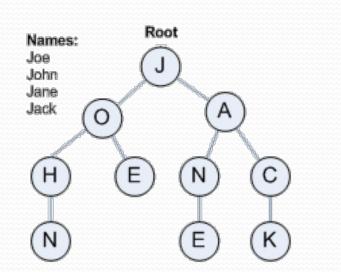
Trees

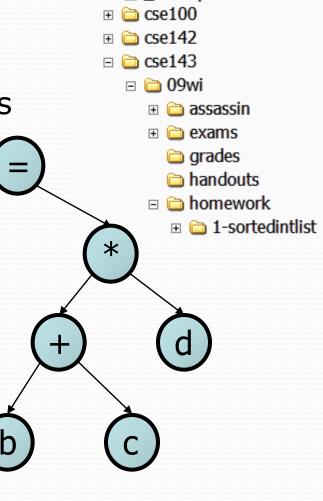
- tree: A directed, acyclic structure of linked nodes.
 - directed: Has one-way links between nodes.
 - acyclic: No path wraps back around to the same node twice.
- binary tree: One where each node has at most two children.
- Recursive definition: A tree is either:
 - empty (null), or
 - a root node that contains:
 - data,
 - a left subtree, and
 - a right subtree.
 - (The left and/or right subtree could be empty.)



Trees in computer science

- TreeMap and TreeSet implementations
- folders/files on a computer
- family genealogy; organizational charts
- AI: decision trees
- compilers: parse tree
 - a = (b + c) * d;
- cell phone T9

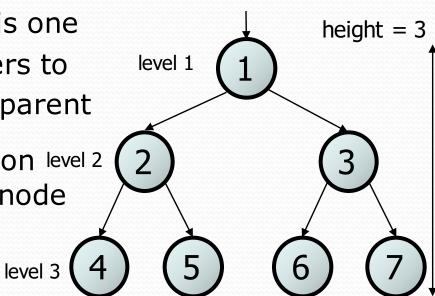




⊕ backup

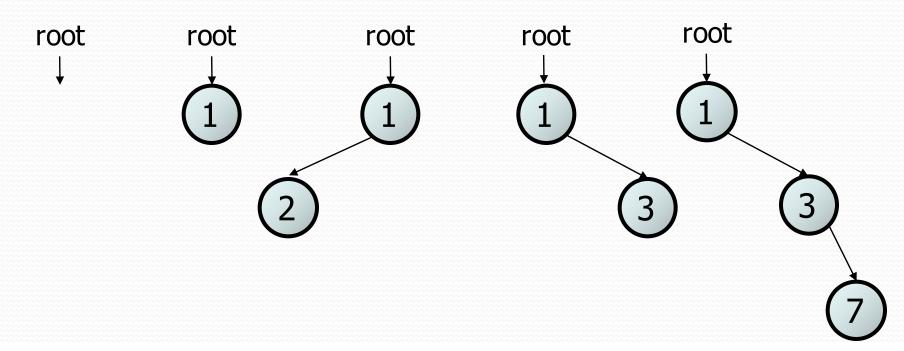
Terminology

- node: an object containing a data value and left/right children
 - root: topmost node of a tree
 - leaf: a node that has no children
 - branch: any internal node; neither the root nor a leaf
 - parent: a node that refers to this one
 - child: a node that this node refers to
 - sibling: a node with a common parent
- **subtree**: the smaller tree of nodes on level 2 the left or right of the current node
- height: length of the longest path from the root to any node
- level or depth: length of the path from a root to a given node



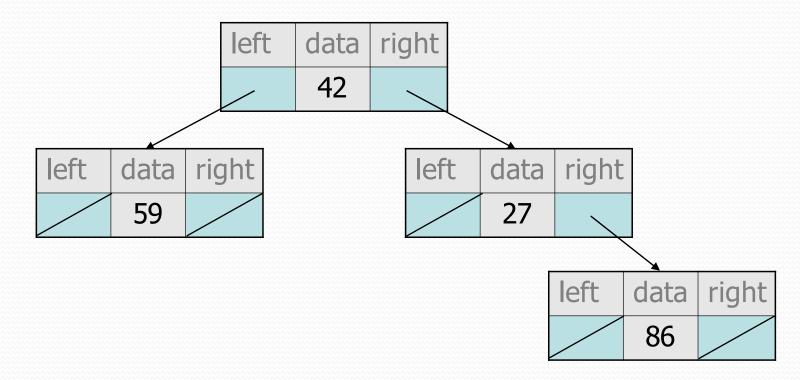
Recursive data structure

- Recursive definition: A tree is either:
 - empty (null), or
 - a root node that contains:
 - data,
 - a left tree, and
 - a right tree



A tree node for integers

- A basic tree node object stores data, refers to left/right
 - Multiple nodes can be linked together into a larger tree



IntTreeNode class

```
// An IntTreeNode object is one node in a binary tree of ints.
public class IntTreeNode {
                     // data stored at this node
    public int data;
    public IntTreeNode left;  // reference to left subtree
    public IntTreeNode right; // reference to right subtree
    // Constructs a leaf node with the given data.
    public IntTreeNode(int data) {
        this (data, null, null);
    // Constructs a branch node with the given data and links.
    public IntTreeNode (int data, IntTreeNode left,
                                 IntTreeNode right) {
        this.data = data;
        this.left = left;
        this.right = right;
                                                     data
                                                left
                                                          right
```

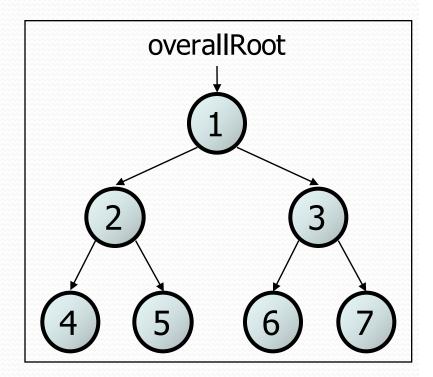
IntTree class

```
// An IntTree object represents an entire binary tree of ints.
public class IntTree {
    private IntTreeNode overallRoot; // null for an empty tree
```

methods

}

- Client code talks to the IntTree,
 not to the node objects inside it.
- Methods of the IntTree create and manipulate the nodes, their data and links between them.



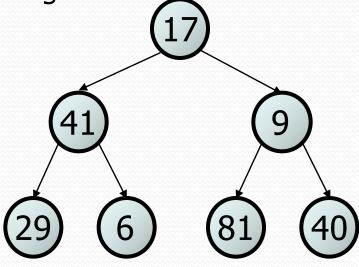
IntTree constructors

For now, assume we have the following constructors:

```
public IntTree(IntTreeNode overallRoot)
public IntTree(int height)
```

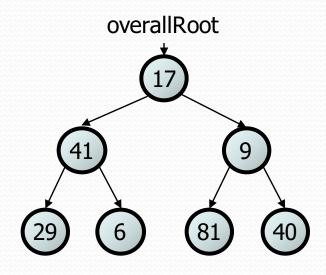
The 2nd constructor will create a tree and fill it with nodes with random data values overallRoot from 1-100 until it is full at the given height.

IntTree tree = new IntTree(3);



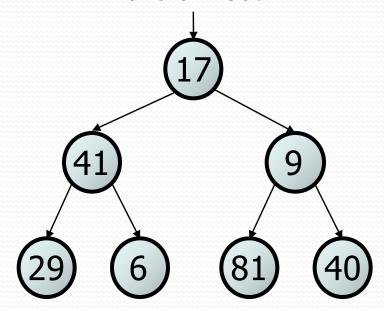
Traversals

- traversal: An examination of the elements of a tree.
 - A pattern used in many tree algorithms and methods
- Common orderings for traversals:
 - pre-order: process root node, then its left/right subtrees
 - in-order: process left subtree, then root node, then right
 - post-order: process left/right subtrees, then root node



Traversal example

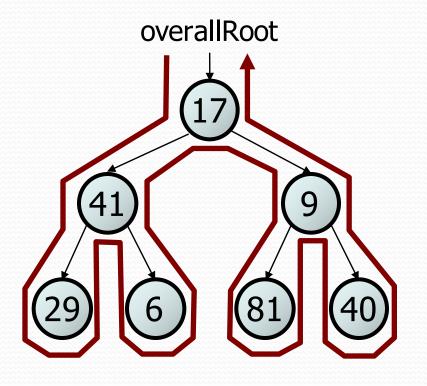
overallRoot



- pre-order: 17 41 29 6 9 81 40
- in-order: 29 41 6 17 81 9 40
- post-order: 29 6 41 81 40 9 17

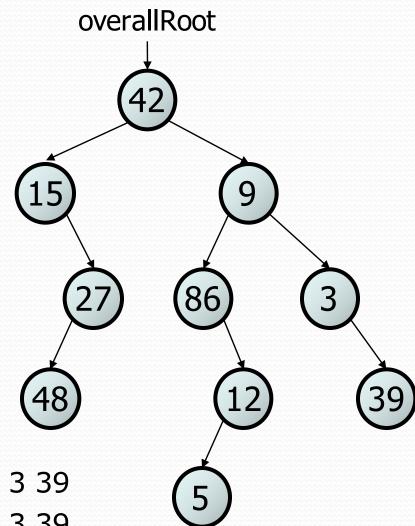
Traversal trick

- To quickly generate a traversal:
 - Trace a path around the tree.
 - As you pass a node on the proper side, process it.
 - pre-order: left side
 - in-order: bottom
 - post-order: right side



- pre-order: 17 41 29 6 9 81 40
- in-order: 29 41 6 17 81 9 40
- post-order: 29 6 41 81 40 9 17

 Give pre-, in-, and post-order traversals for the following tree:

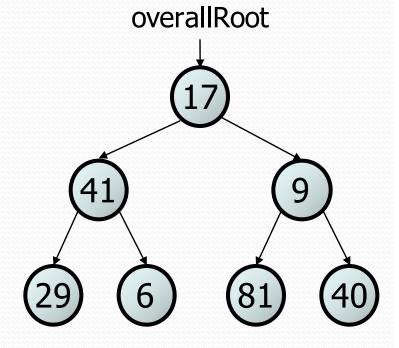


pre: 42 15 27 48 9 86 12 5 3 39

- in: 15 48 27 42 86 5 12 9 3 39

- post: 48 27 15 5 12 86 39 3 42

- Add a method print to the IntTree class that prints the elements of the tree, separated by spaces.
 - A node's left subtree should be printed before it, and its right subtree should be printed after it.
 - Example: tree.print();
 29 41 6 17 81 9 40



Exercise solution

```
// An IntTree object represents an entire binary tree of ints.
public class IntTree {
    private IntTreeNode overallRoot; // null for an empty tree
    public void print() {
        print(overallRoot);
        System.out.println(); // end the line of output
    private void print(IntTreeNode root) {
        // (base case is implicitly to do nothing on null)
        if (root != null) {
            // recursive case: print left, center, right
            print(overallRoot.left);
            System.out.print(overallRoot.data + " ");
            print(overallRoot.right);
```

Template for tree methods

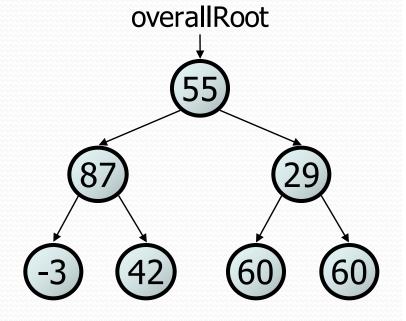
```
public class IntTree {
    private IntTreeNode overallRoot;
    ...

public type name(parameters) {
        name(overallRoot, parameters);
    }

private type name(IntTreeNode root, parameters) {
        ...
}
```

- Tree methods are often implemented recursively
 - with a public/private pair
 - the private version accepts the root node to process

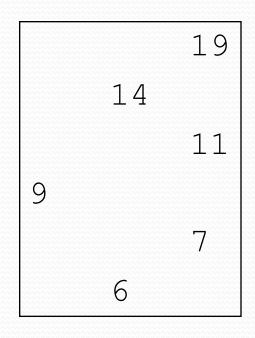
- Add a method contains to the IntTree class that searches the tree for a given integer, returning true if it is found.
 - If an IntTree variable tree referred to the tree below, the following calls would have these results:
 - tree.contains(87) 🗞 true
 - tree.contains(60) 🗞 true
 - tree.contains(63) 🚳 false
 - tree.contains(42) 🚳 false

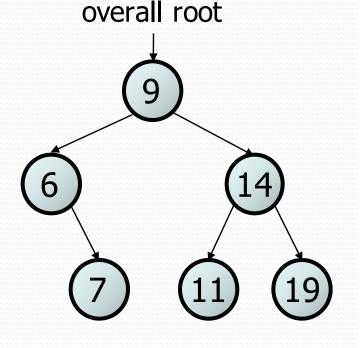


Exercise solution

```
// Returns whether this tree contains the given integer.
public boolean contains(int value) {
    return contains (overallRoot, value);
private boolean contains(IntTreeNode node, int value) {
    if (node == null) {
        return false; // base case: not found here
    } else if (node.data == value) {
        return true; // base case: found here
    } else {
        // recursive case: search left/right subtrees
        return contains (node.left, value) | |
               contains(node.right, value);
```

- Add a method named printSideways to the IntTree class
 that prints the tree in a sideways indented format, with right
 nodes above roots above left nodes, with each level 4
 spaces more indented than the one above it.
 - Example: Output from the tree below:





Exercise solution