## Cryptography

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Slides based on presentation by Josh Benaloh

## Internet Security

- The Internet was NOT designed for security.
- Sending data through the Internet is like sending a postcard through the mail...
- ...when you don't trust the post office


## A typical internet session

You
Server


I want to make a purchase
What is your credit card number?

My CC number is 123456789999

## Basic encryption

Can we AT LEAST protect the credit card number so it won't be revealed to anybody except the merchant?

## Kerckhoff's Principle (1883)

- The security of a cryptosystem should depend only on the key.
- You should assume that attackers know everything about your system except the key


## Some terminology

- Informally...
- A PIN is a 4-6 digit speed bump
- A password is a short, user-chosen, usually guessable selection from a small dictionary.
- A key is an unguessable, randomly chosen string usually at least 128 bits


## Off-Line Attacks

- Don't even think about using user-chosen passwords as encryption keys.
- Don't even think about using keys derived deterministically from user-chosen passwords.
- Given the ciphertext, an attacker can do a (guided) exhaustive search through the space to find the password.


## Symmetric cryptography

- If the client has a pre-existing relationship with the merchant, the two parties may have a shared secret key K - known only to these two.
- User encrypts private data with key K.
- Merchant decrypts data with key K.
- Two classes
- Stream ciphers
- Block ciphers


## Stream Cipher

- RC4, A5/1, SEAL, etc.
- Use the key as a seed to a pseudo-random number-generator.
- Take the stream of output bits from the PRNG and XOR it with the plaintext to form the ciphertext.
- (1x1->0, 1x0->1, ox1->1, oxo->0)

Plaintext: PRNG (seed): Ciphertext:


## Stream Cipher Decryption

## Plaintext: PRNG (seed): Ciphertext:



## Stream cipher evaluation

- The good
- Usually fast
- Usually simple
- Same function for encrypt and decrypt
- The bad
- Hint: Something XOR'ed with itself disappears, which is why decryption works
- If the same PRNG seed is ever reused...
- $(\mathrm{PT} 1 \times \mathrm{PRNG}) \times(\mathrm{PT} 2 \times \mathrm{PRNG})=(\mathrm{PT} 1 \times \mathrm{PT} 2)$


## More bad

- It is easy for an adversary (even one who can' t decrypt the ciphertext)to alter the plaintext in a known way.
- Eg,.Bob to Bob's Bank:
- Please transfer \$0,000,002.00 to the account of my good friend Alice.
- Please transfer \$1,000,002.00 to the account of my good friend Alice.


## Block Cipher



## Feistel cipher



Encoding

## Feistel cipher



Decoding

## Feistel performance

- Typically, Feistel ciphers are iterated for about 10-16 rounds.
- Different "sub-keys" are used for each round.
- Even a weak round function can yield a strong Feistel cipher, if iterated sufficiently.


## Feistel cipher



## Our new encoded system

You
Server


I want to make a purchase
What is your credit card number?

My CC number is $E(12345678$ 9999)

## Our new encoded system

You
Server


Please encrypt your \# with our shared secret key
????

## Asymmetric cryptography

- What if the user and merchant have no prior relationship?
- Asymmetric encryption allows someone to encrypt a message for a recipient without knowledge of the recipient's decryption key.
- Usually involves lots of math.


## The Fundamental Equation

$$
\mathrm{Z}=\mathrm{Y}^{\mathrm{x}} \bmod \mathrm{~N}
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If Z is unknown, it can be computed efficiently.

## The Fundamental Equation

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## $\mathrm{Z}=\mathrm{Y}^{\mathrm{x}} \bmod \mathrm{N}$

If Y is unknown, the problem is called the discrete root finding and is generally hard to solve, without factorization of N .

## The Fundamental Equation

$$
\mathrm{Z}=\mathrm{Y}^{\mathrm{x}} \bmod \mathrm{~N}
$$

## If N is unknown, the problem is not well studied.

## RSA encryption

- Pick two primes p and q, compute $\mathrm{n}=\mathrm{pq}$
- Pick two numbers e and d, such that:
- ed $=(\mathrm{p}-1)(\mathrm{q}-1) \mathrm{k}+1$ (for some k$)$
- Publish n and e (public key), encode with: - (original message) ${ }^{\mathrm{e}} \bmod \mathrm{n}$
- Keep d, p and q secret (private key), decode with:
- (encoded message) ${ }^{\text {d }} \bmod n$


## Why does it work?

- Original message is carried to the e power, then to the d power:
- $\left(\mathrm{msg}^{\mathrm{e}}\right)^{\mathrm{d}}=\mathrm{msg}^{\text {ed }}$
- Remember how we picked e and d:
- $\mathrm{msg}^{\mathrm{ed}}=\operatorname{msg}^{(\mathrm{p}-1)(\mathrm{q}-1) \mathrm{k}+1}$
- Apply some simple algebra:
$\circ \mathrm{msg}^{\mathrm{ed}}=\left(\mathrm{msg}^{(\mathrm{p}-1)(\mathrm{q}-1)}\right)^{\mathrm{k}} \times \mathrm{msg}^{1}$
- Applying Fermat's Little Theorem:
- $\mathrm{msg}^{\mathrm{ed}}=(1)^{\mathrm{k}} \mathrm{msg}^{1}=\mathrm{msg}$


## A brief history of RSA

- British discovered RSA first but kept it secret
- Phil Zimmerman tried to bring cryptography to the masses w/PGP
- Investigated as an arms dealer by FBI and a grand jury
- Shor's algorithm would break RSA if only we had a quantum computer
- The NSA hires more mathematicians than any other organization


## Our RSA based system

You
Server


Please encrypt your \# with my public key E
My CC is $E(12345678$ 9999)

## Problems

- Man-in-the-middle attack
- Someone pretends to be the server
- Solution: Certificates
- Need certificate authorities
- Must guarantee the certificate authorities
- Replay attack
- Someone repeats your encoded message
- Solution: a unique nonce (number)

