## CSE 143 Lecture 19

## More Recursive Backtracking

## reading: "Appendix R" on course web site

slides adapted from Marty Stepp and Hélène Martin
http://www.cs.washington.edu/143/

## Exercise: solve maze

- Write a method solveMaze that accepts a Maze and a starting row/column as parameters and tries to find a path out of the maze starting from that position.
- If you find a solution:
- Your code should stop exploring.
- You should mark the path out of the maze on your way back out of the recursion, using backtracking.
- (As you explore the maze, squares you set as 'explored' will be printed with a dot, and squares you 'mark' will display an X.)


## \#\#\#\#\#\#\#\#\#\#

\# $\quad$ x \#
\# \#\#\#x\#\# \#
\# \# xx \# \# \# \# x\# \# \#
\# \#\#x\#\#\#\#\#
\# \#.xx \#
\# \#.\#x \# \#
\#\#\#\#\#x\#\#\#\#
\#... \#xxxx?
\#.\#..xx\#.\#
\#\#\#\#\#\#\#\#\#\#

## Maze class

- Suppose we have a Maze class with these methods:

| Method/Constructor | Description |
| :--- | :--- |
| public Maze (String text) | construct a given maze |
| public int getHeight(), getWidth() | get maze dimensions |
| public boolean isExplored(int r, int c) <br> public void setExplored(int r, int c) | get/set whether you <br> have visited a location |
| public void isWall (int r, int c) | whether given location <br> is blocked by a wall |
| public void mark(int r, int c) <br> public void isMarked(int r, int c) | whether given location <br> is marked in a path |
| public String toString() | text display of maze |

## Recall: Backtracking

A general pseudo-code algorithm for backtracking problems:

## Explore(choices):

- if there are no more choices to make: stop.
- else, for each available choice C:
- Choose C.
- Explore the remaining choices.
- Un-choose C, if necessary. (backtrack!)

What are the choices in this problem?


## The "8 Queens" problem

- Consider the problem of trying to place 8 queens on a chess board such that no queen can attack another queen.
- What are the "choices"?
- How do we "make" or "un-make" a choice?
- How do we know when to stop?

- for (each square on board):
- Place a queen there.
- Try to place the rest of the queens.
- Un-place the queen.
- How large is the solution space for this algorithm?
- $64 * 63 * 62 * \ldots$



## Better algorithm idea

- Observation: In a working solution, exactly 1 queen must appear in each row and in each column.
- Redefine a "choice" to be valid placement of a queen in a particular column.
- How large is the solution space now?

$$
\bullet 8 * 8 * 8 \text { * ... }
$$

## Exercise

- Suppose we have a Board class with the following methods:

| Method/Constructor | Description |
| :--- | :--- |
| public Board(int size) | construct empty board |
| public boolean isSafe(int row, int column) | true if queen can be <br> safely placed here |
| public void place(int row, int column) | place queen here |
| public void remove(int row, int column) | remove queen from here |
| public String toString() | text display of board |

- Write a method solveQueens that accepts a Board as a parameter and tries to place 8 queens on it safely.
- Your method should stop exploring if it finds a solution.


## Exercise solution

```
// Searches for a solution to the 8 queens problem
// with this board, reporting the first result found.
public static void solveQueens(Board board) {
    if (solveQueens (board, 1)) {
        System.out.println("One solution is as follows:");
        System.out.println(board);
    } else {
        System.out.println("No solution found.");
    }
}
```


## Exercise solution, cont'd.

```
// Recursively searches for a solution to 8 queens on this
// board, starting with the given column, returning true if a
// solution is found and storing that solution in the board.
// PRE: queens have been safely placed in columns 1 to (col-1)
public static boolean solveQueens(Board board, int col) {
    if (col > board.size()) {
        return true; // base case: all columns are placed
    } else {
        // recursive case: place a queen in this column
        for (int row = 1; row <= board.size(); row++) {
            if (board.isSafe(row, col)) {
                board.place(row, col); // choose
                        if (explore(board, col + 1)) { // explore
                        return true; // solution found
                            }
                                b.remove(row, col); // un-choose
            }
        }
        return false; // no solution found
    }
}
```


## Exercise: Dominoes

- The game of dominoes is played with small black tiles, each having 2 numbers of dots from 0-6. Players line up tiles to match dots.

- Given a class Domino with the following public methods:

```
int first()
int second()
void flip()
boolean contains(int n) // true if 1st/2nd == n
String toString() // e.g. "(3|5)"
```

- Write a method hasChain that takes a List of dominoes and a starting/ending dot value, and returns whether the dominoes can be made into a chain that starts/ends with those values.


## Domino chains

- Suppose we have the following dominoes:
- We can link them into a chain from 1 to 3 as follows:
- Notice that the 3|5 domino had to be flipped.
- P8:
- We can "link" one domino into a "chain" from 6 to 2 as follows: -000 ${ }^{\circ}$


## Exercise client code

```
import java.util.*; // for ArrayList
public class SolveDominoes {
    public static void main(String[] args) {
        // [(1|4), (2|6), (4|5), (1|5), (3|5)]
    List<Domino> dominoes = new ArrayList<Domino>();
    dominoes.add(new Domino(1, 4));
    dominoes.add(new Domino(2, 6));
    dominoes.add(new Domino(4, 5));
    dominoes.add(new Domino(1, 5));
    dominoes.add(new Domino(3, 5));
    System.out.println(hasChain(dominoes, 5, 5)); // true
    System.out.println(hasChain(dominoes, 1, 5)); // true
    System.out.println(hasChain(dominoes, 1, 3)); // true
    System.out.println(hasChain(dominoes, 1, 6)); // false
    System.out.println(hasChain(dominoes, 1, 2)); // false
    }
    public static boolean hasChain(List<Domino> dominoes,
                                    int start, int end) {
    }

\section*{Exercise solution}
```

public boolean hasChain(List<Domino> dominoes, int start, int end) {
if (start == end) {
for (Domino d : dominoes) {
if (d.contains(start)) { return true; }
}
return false; // base case
} else {
for (int i = 0; i < dominoes.size(); i++) {
Domino d = dominoes.remove(i); // choose
if (d.first() == start) { // explore
if (hasChain(dominoes, d.second(), end)) {
return true;
}
} else if (d.second() == start) {
if (hasChain(dominoes, d.first(), end)) {
return true;
}
}
dominoes.add(i, d); // un-choose
}
return false;
}

## Exercise: Print chain

- Write a variation of your haschain method that also prints the chain of dominoes that it finds, if any.
hasChain(dominoes, 1, 3);
$[(1 \mid 4),(4 \mid 5),(5 \mid 3)]$

