

CSE 143

Lecture 17

Sorting

reading: 13.1, 13.3 - 13.4

slides adapted from Marty Stepp

<http://www.cs.washington.edu/143/>

Selection sort

- **selection sort:** Orders a list of values by repeatedly putting the smallest or largest unplaced value into its final position.

The algorithm:

- Look through the list to find the smallest value.
- Swap it so that it is at index 0.
- Look through the list to find the second-smallest value.
- Swap it so that it is at index 1.
- ...
- Repeat until all values are in their proper places.

Selection sort example

- Initial array:

index	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
value	22	18	12	-4	27	30	36	50	7	68	91	56	2	85	42	98	25

- After 1st, 2nd, and 3rd passes:

index	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
value	-4	18	12	22	27	30	36	50	7	68	91	56	2	85	42	98	25

index	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
value	-4	2	12	22	27	30	36	50	7	68	91	56	18	85	42	98	25

index	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
value	-4	2	7	22	27	30	36	50	12	68	91	56	18	85	42	98	25

Selection sort code

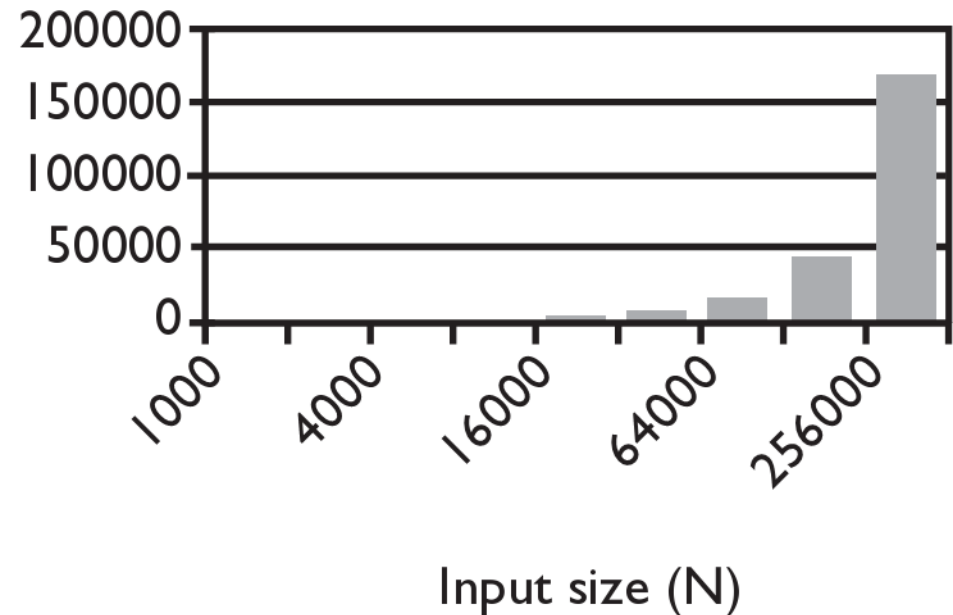
```
// Rearranges the elements of a into sorted order using
// the selection sort algorithm.
public static void selectionSort(int[] a) {
    for (int i = 0; i < a.length - 1; i++) {
        // find index of smallest remaining value
        int min = i;
        for (int j = i + 1; j < a.length; j++) {
            if (a[j] < a[min]) {
                min = j;
            }
        }
        // swap smallest value its proper place, a[i]
        swap(a, i, min);
    }
}

// Swaps a[i] with a[j].
public static void swap(int[] a, int i, int j) {
    if (i != j) {
        int temp = a[i];
        a[i] = a[j];
        a[j] = temp;
    }
}
```

Selection sort runtime (Fig. 13.6)

- What is the complexity class (Big-Oh) of selection sort?

N	Runtime (ms)
1000	0
2000	16
4000	47
8000	234
16000	657
32000	2562
64000	10265
128000	41141
256000	164985



Merge sort

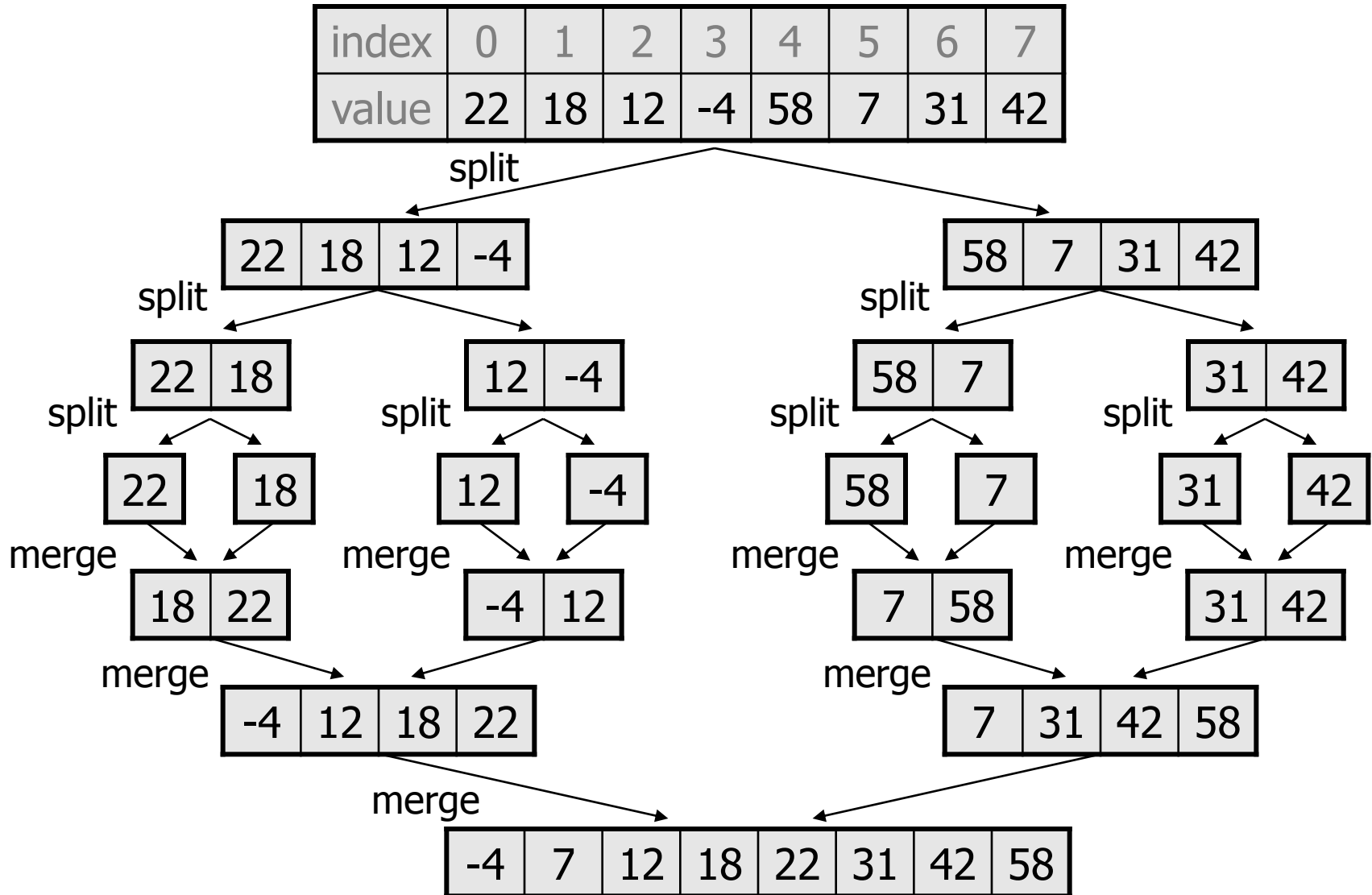
- **merge sort:** Repeatedly divides the data in half, sorts each half, and combines the sorted halves into a sorted whole.

The algorithm:

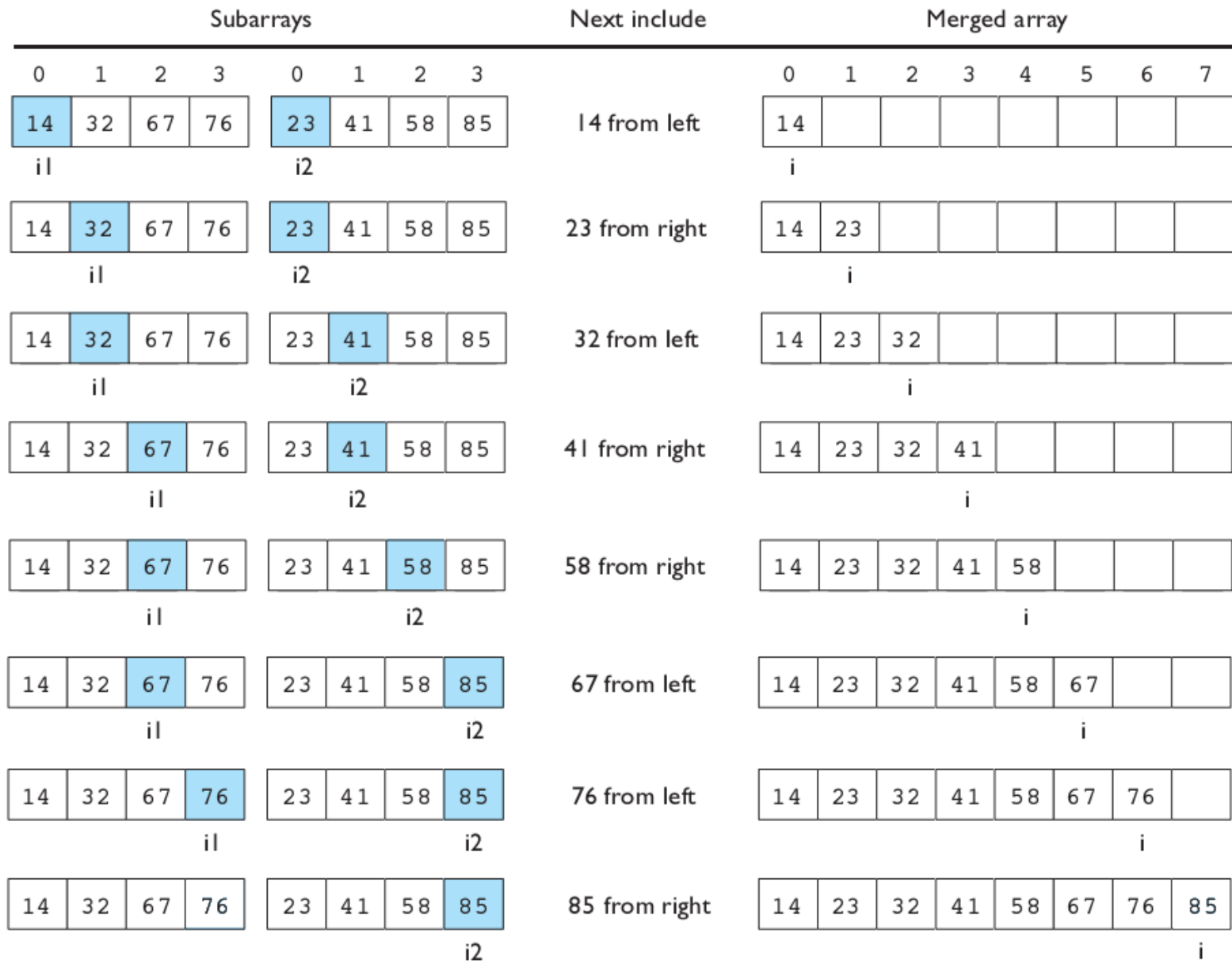
- Divide the list into two roughly equal halves.
- Sort the left half.
- Sort the right half.
- Merge the two sorted halves into one sorted list.

- Often implemented recursively.
- An example of a "divide and conquer" algorithm.
 - Invented by John von Neumann in 1945

Merge sort example



Merging sorted halves



Merge halves code

```
// Merges the left/right elements into a sorted result.
// Precondition: left/right are sorted
public static void merge(int[] result, int[] left,
                        int[] right) {
    int i1 = 0;    // index into left array
    int i2 = 0;    // index into right array

    for (int i = 0; i < result.length; i++) {
        if (i2 >= right.length ||
            (i1 < left.length && left[i1] <= right[i2])) {
            result[i] = left[i1];    // take from left
            i1++;
        } else {
            result[i] = right[i2];    // take from right
            i2++;
        }
    }
}
```

Merge sort code

```
// Rearranges the elements of a into sorted order using
// the merge sort algorithm.
public static void mergeSort(int[] a) {
    // split array into two halves
    int[] left  = Arrays.copyOfRange(a, 0, a.length/2);
    int[] right = Arrays.copyOfRange(a, a.length/2, a.length);

    // sort the two halves
    ...

    // merge the sorted halves into a sorted whole
    merge(a, left, right);
}
```

Merge sort code 2

```
// Rearranges the elements of a into sorted order using
// the merge sort algorithm (recursive).
public static void mergeSort(int[] a) {
    if (a.length >= 2) {
        // split array into two halves
        int[] left  = Arrays.copyOfRange(a, 0, a.length/2);
        int[] right = Arrays.copyOfRange(a, a.length/2, a.length);

        // sort the two halves
        mergeSort(left);
        mergeSort(right);

        // merge the sorted halves into a sorted whole
        merge(a, left, right);
    }
}
```

Merge sort runtime

- What is the complexity class (Big-Oh) of merge sort?

N	Runtime (ms)
1000	0
2000	0
4000	0
8000	0
16000	0
32000	15
64000	16
128000	47
256000	125
512000	250
1e6	532
2e6	1078
4e6	2265
8e6	4781
1.6e7	9828
3.3e7	20422
6.5e7	42406
1.3e8	88344

