

CSE 143

Lecture 22

Comparable and Searching

reading: 13.1 - 13.3; 10.2

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Binary search (13.1)

- **binary search:** Locates a target value in a *sorted* array/list by successively eliminating half of the array from consideration.
 - How many elements will it need to examine? **$O(\log N)$**
 - Can be implemented with a loop or recursively
 - Example: Searching the array below for the value **42**:

index	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
value	-4	2	7	10	15	20	22	25	30	36	42	50	56	68	85	92	103

Diagram illustrating the binary search process on the array above. The current search range is highlighted with arrows pointing to the **min**, **mid**, and **max** indices.

Binary search code

```
// Returns the index of an occurrence of target in a,
// or a negative number if the target is not found.
// Precondition: elements of a are in sorted order
public static int binarySearch(int[] a, int target) {
    int min = 0;
    int max = a.length - 1;

    while (min <= max) {
        int mid = (min + max) / 2;
        if (a[mid] < target) {
            min = mid + 1;
        } else if (a[mid] > target) {
            max = mid - 1;
        } else {
            return mid;      // target found
        }
    }

    return -(min + 1);      // target not found
}
```

Recursive binary search (13.3)

- Write a recursive `binarySearch` method.
 - If the target value is not found, return its negative insertion point.

index	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
value	-4	2	7	10	15	20	22	25	30	36	42	50	56	68	85	92	103

```
int index  = binarySearch(data, 42); // 10
int index2 = binarySearch(data, 66); // -14
```

Exercise solution

```
// Returns the index of an occurrence of the given value in
// the given array, or a negative number if not found.
// Precondition: elements of a are in sorted order
public static int binarySearch(int[] a, int target) {
    return binarySearch(a, target, 0, a.length - 1);
}

// Recursive helper to implement search behavior.
private static int binarySearch(int[] a, int target,
                                int min, int max) {
    if (min > max) {
        return -1;           // target not found
    } else {
        int mid = (min + max) / 2;
        if (a[mid] < target) {           // too small; go right
            return binarySearch(a, target, mid + 1, max);
        } else if (a[mid] > target) {    // too large; go left
            return binarySearch(a, target, min, mid - 1);
        } else {
            return mid;    // target found; a[mid] == target
        }
    }
}
```

Binary search and objects

- Can we `binarySearch` an array of `Strings`?
 - Operators like `<` and `>` do not work with `String` objects.
 - But we do think of strings as having an alphabetical ordering.
- **natural ordering**: Rules governing the relative placement of all values of a given type.
- **comparison function**: Code that, when given two values *A* and *B* of a given type, decides their relative ordering:
 - $A < B$, $A == B$, $A > B$

The compareTo method (10.2)

- The standard way for a Java class to define a comparison function for its objects is to define a `compareTo` method.
 - Example: in the `String` class, there is a method:

```
public int compareTo(String other)
```
- A call of `A.compareTo(B)` will return:
 - a value < 0 if **A** comes "before" **B** in the ordering,
 - a value > 0 if **A** comes "after" **B** in the ordering,
 - or 0 if **A** and **B** are considered "equal" in the ordering.

Using compareTo

- `compareTo` can be used as a test in an `if` statement.

```
String a = "alice";
String b = "bob";
if (a.compareTo(b) < 0) { // true
    ...
}
```

Primitives	Objects
<code>if (a < b) { ... }</code>	<code>if (a.compareTo(b) < 0) { ... }</code>
<code>if (a <= b) { ... }</code>	<code>if (a.compareTo(b) <= 0) { ... }</code>
<code>if (a == b) { ... }</code>	<code>if (a.compareTo(b) == 0) { ... }</code>
<code>if (a != b) { ... }</code>	<code>if (a.compareTo(b) != 0) { ... }</code>
<code>if (a >= b) { ... }</code>	<code>if (a.compareTo(b) >= 0) { ... }</code>
<code>if (a > b) { ... }</code>	<code>if (a.compareTo(b) > 0) { ... }</code>

Binary search w/ strings

```
// Returns the index of an occurrence of target in a,
// or a negative number if the target is not found.
// Precondition: elements of a are in sorted order
public static int binarySearch(String[] a, int target) {
    int min = 0;
    int max = a.length - 1;

    while (min <= max) {
        int mid = (min + max) / 2;
        if (a[mid].compareTo(target) < 0) {
            min = mid + 1;
        } else if (a[mid].compareTo(target) > 0) {
            max = mid - 1;
        } else {
            return mid;      // target found
        }
    }

    return -(min + 1);      // target not found
}
```

compareTo and collections

- You can use an array or list of strings with Java's included binary search method because it calls `compareTo` internally.

```
String[] a = {"al", "bob", "cari", "dan", "mike"};  
int index = Arrays.binarySearch(a, "dan"); // 3
```

- Java's TreeSet/Map use `compareTo` internally for ordering.

```
Set<String> set = new TreeSet<String>();  
for (String s : a) {  
    set.add(s);  
}  
System.out.println(s);  
// [al, bob, cari, dan, mike]
```

Ordering our own types

- We cannot binary search or make a TreeSet/Map of arbitrary types, because Java doesn't know how to order the elements.
 - The program compiles but crashes when we run it.

```
Set<HtmlTag> tags = new TreeSet<HtmlTag>();  
tags.add(new HtmlTag("body", true));  
tags.add(new HtmlTag("b", false));  
...
```

**Exception in thread "main" java.lang.ClassCastException
at java.util.TreeSet.add(TreeSet.java:238)**

Comparable (10.2)

```
public interface Comparable<E> {  
    public int compareTo(E other);  
}
```

- A class can implement the Comparable interface to define a natural ordering function for its objects.
- A call to your compareTo method should return:
 - a value < 0 if the other object comes "before" this one,
 - a value > 0 if the other object comes "after" this one,
 - or 0 if the other object is considered "equal" to this.
- If you want multiple orderings, use a Comparator instead (see Ch. 13.1)

Comparable template

```
public class name implements Comparable<name> {  
    ...  
    public int compareTo(name other) {  
        ...  
    }  
}
```

Comparable example

```
public class Point implements Comparable<Point> {  
    private int x;  
    private int y;  
    ...  
  
    // sort by x and break ties by y  
    public int compareTo(Point other) {  
        if (x < other.x) {  
            return -1;  
        } else if (x > other.x) {  
            return 1;  
        } else if (y < other.y) {  
            return -1;      // same x, smaller y  
        } else if (y > other.y) {  
            return 1;       // same x, larger y  
        } else {  
            return 0;       // same x and same y  
        }  
    }  
}
```

compareTo tricks

- *subtraction trick* - Subtracting related numeric values produces the right result for what you want `compareTo` to return:

```
// sort by x and break ties by y
public int compareTo(Point other) {
    if (x != other.x) {
        return x - other.x;      // different x
    } else {
        return y - other.y;      // same x; compare y
    }
}
```

- The idea:

- if $x > \text{other}.x$, then $x - \text{other}.x > 0$
- if $x < \text{other}.x$, then $x - \text{other}.x < 0$
- if $x == \text{other}.x$, then $x - \text{other}.x == 0$

– NOTE: This trick doesn't work for doubles (but see `Math.signum`)

compareTo tricks 2

- *delegation trick* - If your object's fields are comparable (such as strings), use their compareTo results to help you:

```
// sort by employee name, e.g. "Jim" < "Susan"  
public int compareTo(Employee other) {  
    return name.compareTo(other.getName());  
}
```

- *toString trick* - If your object's toString representation is related to the ordering, use that to help you:

```
// sort by date, e.g. "09/19" > "04/01"  
public int compareTo(Date other) {  
    return toString().compareTo(other.toString());  
}
```

Exercises

- Make the `HtmlTag` class from HTML Validator comparable.
 - Compare tags by their elements, alphabetically by name.
 - For the same element, opening tags come before closing tags.

```
// <body><b></b><i><b></b><br/></i></body>
Set<HtmlTag> tags = new TreeSet<HtmlTag>();
tags.add(new HtmlTag("body", true));           // <body>
tags.add(new HtmlTag("b", true));              // <b>
tags.add(new HtmlTag("b", false));             // </b>
tags.add(new HtmlTag("i", true));              // <i>
tags.add(new HtmlTag("b", true));              // <b>
tags.add(new HtmlTag("b", false));             // </b>
tags.add(new HtmlTag("br"));                  // <br />
tags.add(new HtmlTag("i", false));             // </i>
tags.add(new HtmlTag("body", false));          // </body>
System.out.println(tags);
// [<b>, </b>, <body>, </body>, <br />, <i>, </i>]
```

Exercise solution

```
public class HtmlTag implements Comparable<HtmlTag> {  
    ...  
    // Compares tags by their element ("body" before "head"),  
    // breaking ties with opening tags before closing tags.  
    // Returns < 0 for less, 0 for equal, > 0 for greater.  
    public int compareTo(HtmlTag other) {  
        int compare = element.compareTo(other.getElement());  
        if (compare != 0) {  
            // different tags; use String's compareTo result  
            return compare;  
        } else {  
            // same tag  
            if ((isOpenTag == other.isOpenTag()) {  
                return 0; // exactly the same kind of tag  
            } else if (other.isOpenTag()) {  
                return 1; // he=open, I=close; I am after  
            } else {  
                return -1; // I=open, he=close; I am before  
            }  
        }  
    }  
}
```