CSE 143 Lecture 19

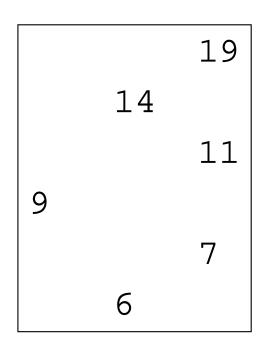
Binary Search Trees

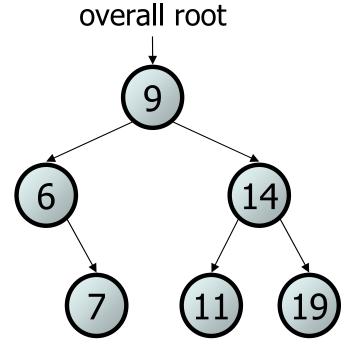
read 17.3

slides created by Marty Stepp http://www.cs.washington.edu/143/

Exercise

- Add a method named printSideways to the IntTree class that prints the tree in a sideways indented format, with right nodes above roots above left nodes, with each level 4 spaces more indented than the one above it.
 - Example: Output from the tree below:





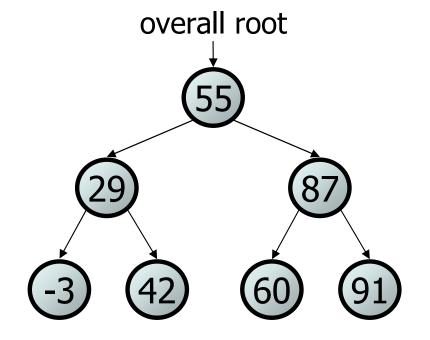
Exercise solution

```
// Prints the tree in a sideways indented format.
public void printSideways() {
    printSideways(overallRoot, "");
}
private void printSideways(IntTreeNode root,
                            String indent) {
    if (root != null) {
        printSideways(root.right, indent + "
                                                 ");
        System.out.println(indent + root.data);
        printSideways(root.left, indent + "
                                                 ");
```

Binary search trees

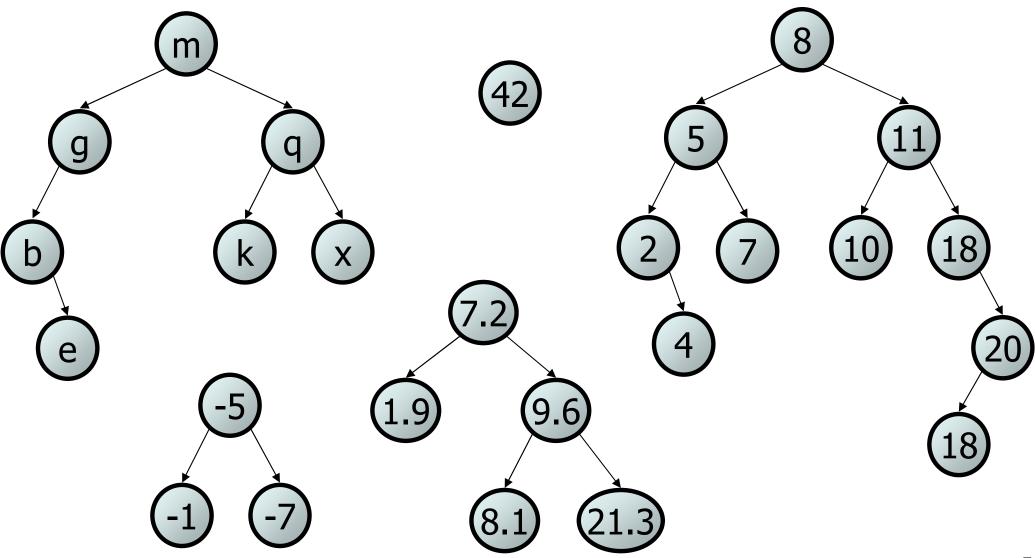
- **binary search tree** ("BST"): a binary tree that is either:
 - empty (null), or
 - a root node R such that:
 - every element of R's left subtree contains data "less than" R's data,
 - every element of R's right subtree contains data "greater than" R's,
 - R's left and right subtrees are also binary search trees.

 BSTs store their elements in sorted order, which is helpful for searching/sorting tasks.



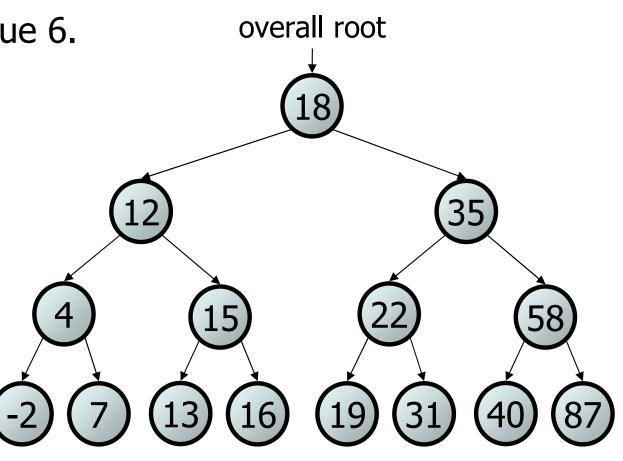
Exercise

• Which of the trees shown are legal binary search trees?



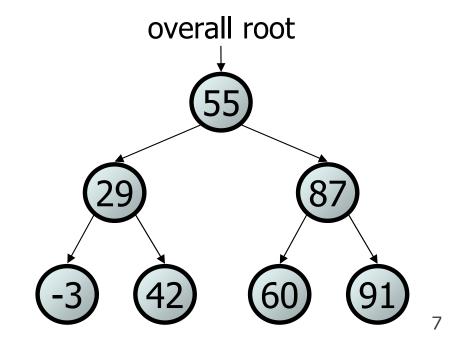
Searching a BST

- Describe an algorithm for searching the tree below for the value 31.
- Then search for the value 6.
- What is the maximum number of nodes you would need to examine to perform any search?



Exercise

- Add a method contains to the IntTree class that searches the tree for a given integer, returning true if it is found in the tree and false if not. Assume that the elements of the tree constitute a legal binary search tree.
 - If an IntTree variable tree referred to the tree below, the following calls would have the following results:
 - tree.contains(29) \rightarrow true
 - tree.contains(55) \rightarrow true
 - tree.contains(63) \rightarrow false
 - •tree.contains(35) \rightarrow false



Exercise solution

```
// Returns whether this tree contains the given integer.
public boolean contains(int value) {
    return contains(overallRoot, value);
}
private boolean contains(IntTreeNode root, int value) {
    if (root == null) {
        return false;
    } else if (root.data == value) {
        return true;
    }
}
```

```
} else if (root.data > value) {
    return contains(root.left, value);
} else { // root.data < value</pre>
```

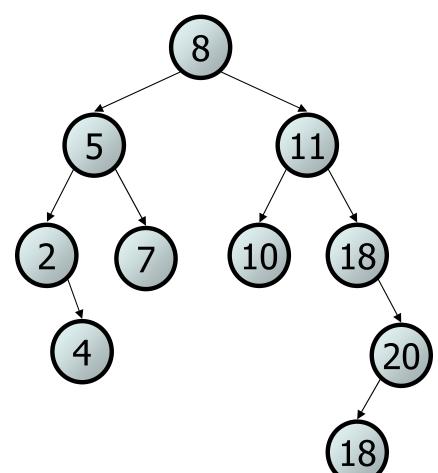
}

return contains(root.right, value);

Adding to a BST

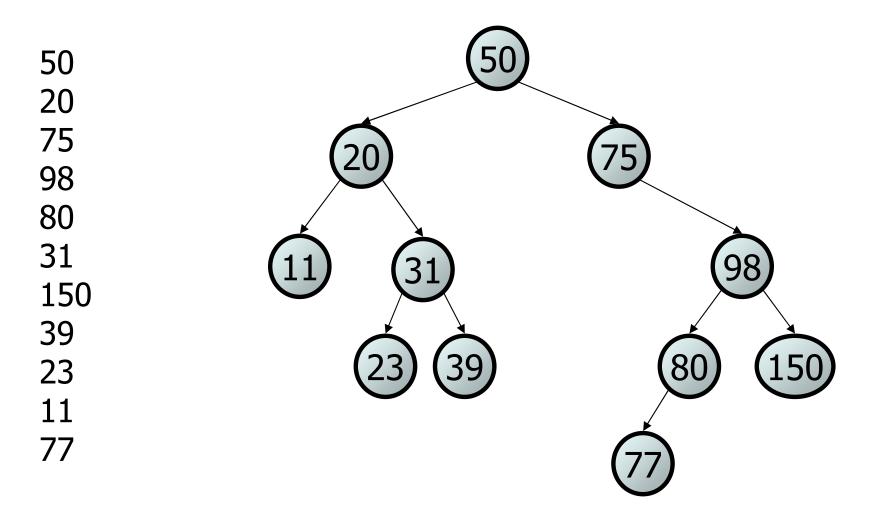
- Suppose we want to add the value 14 to the BST below.
 Where should the new node be added?
- Where would we add the value 3?
- Where would we add 7?
- If the tree is empty, where should a new value be added?





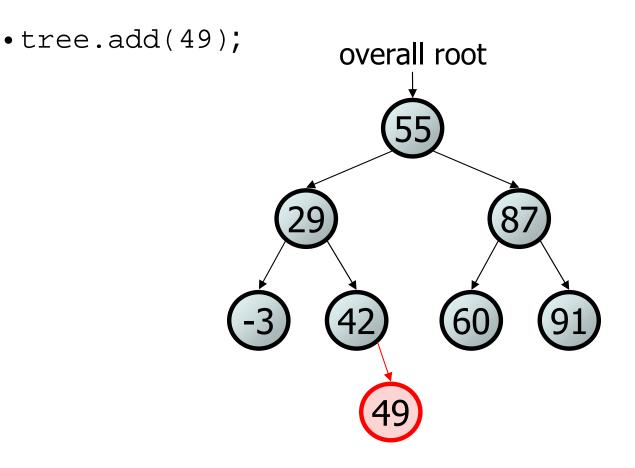
Adding exercise

• Draw what a binary search tree would look like if the following values were added to an initially empty tree in this order:





• Add a method add to the IntTree class that adds a given integer value to the tree. Assume that the elements of the IntTree constitute a legal binary search tree, and add the new value in the appropriate place to maintain ordering.



An incorrect solution

```
// Adds the given value to this BST in sorted order.
public void add(int value) {
    add(overallRoot, value);
}
private void add(IntTreeNode root, int value) {
    if (root == null) {
        root = new IntTreeNode(value);
    } else if (root.data > value) {
                                                overallRoot
        add(root.left, value);
    } else if (root.data < value) {</pre>
        add(root.right, value);
    // else root.data == value;
    // a duplicate (don't add)
                                                     60
```

• Why doesn't this solution work?

The problem

• Much like with linked lists, if we just modify what a local variable refers to, it won't change the collection.

```
root -49
private void add(IntTreeNode root, int value) {
    if (root == null) {
        root = new IntTreeNode(value);
        overallRoot
        for the linked list case, how did we
        correct this problem? How did we
        actually modify the list?
        for the linked list?
        for the linked list case, how did we
        actually modify the list?
        for the linked list?
        for the linked list case, how did we
        for the linked l
```

x = change(x);

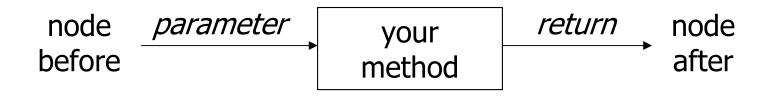
- All String object methods that modify a String actually return a new String object.
 - If we want to modify a string variable, we must re-assign it.

```
String s = "lil bow wow";
s.toUpperCase();
System.out.println(s); // lil bow wow
s = s.toUpperCase();
System.out.println(s); // LIL BOW WOW
```

- We call this general algorithmic pattern x = change(x);
- We will use this approach when writing methods that modify the structure of a binary tree.

Applying x = change(x)

- Methods that modify a tree should have the following pattern:
 - input (parameter): old state of the node
 - output (return): new state of the node



• In order to actually change the tree, you must reassign:

```
root = change(root, parameters);
root.left = change(root.left, parameters);
root.right = change(root.right, parameters);
```

A correct solution

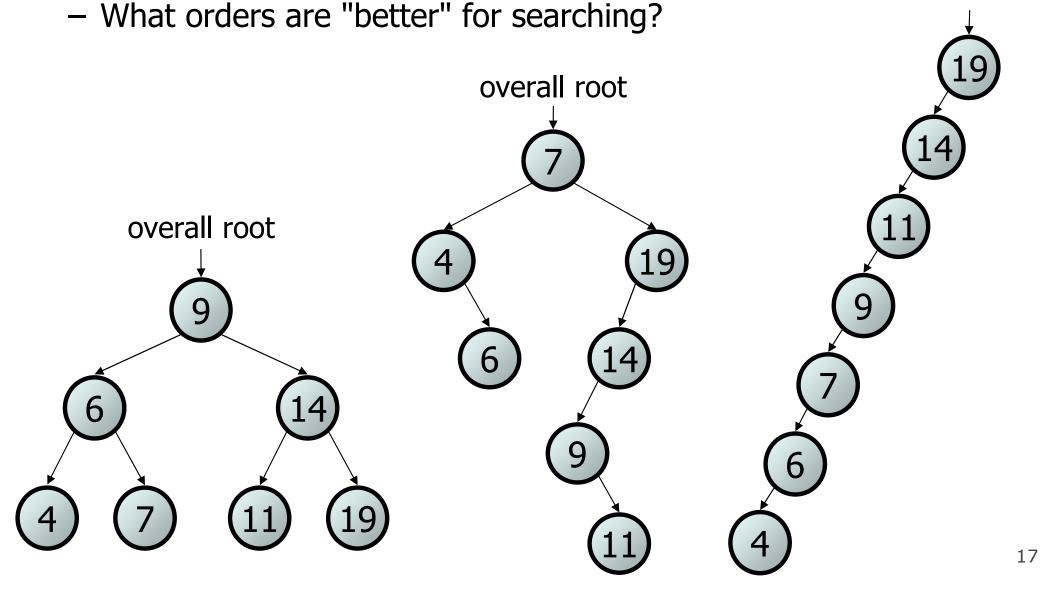
```
// Adds the given value to this BST in sorted order.
public void add(int value) {
    overallRoot = add(overallRoot, value);
private IntTreeNode add(IntTreeNode root, int value) {
    if (root == null) {
        root = new IntTreeNode(value);
    } else if (root.data > value) {
        root.left = add(root.left, value);
    } else if (root.data < value) {
                                                  overallRoot
        root.right = add(root.right, value);
    } // else a duplicate
                                                    55
    return root;

    Think about the case when root is a leaf...
```

Searching BSTs

overall root

• The BSTs below contain the same elements.



Trees and balance

- **balanced tree**: One whose subtrees differ in height by at most 1 and are themselves balanced.
 - A balanced tree of N nodes has a height of $\sim \log_2 N$.
 - A very unbalanced tree can have a height close to N.
 - The runtime of adding to / searching a BST is closely related to height.
 - Some tree collections (e.g. TreeSet) contain code to balance themselves as new nodes are added.

