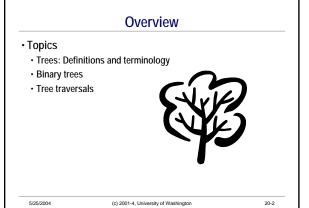
CSE 143 Java Trees (c) 2001-4, University of Washington 20-1



Trees

- · Most of the structures we've looked at so far are linear
 - Arrays
 - · Linked lists
- There are many examples of structures that are not linear, e.g. hierarchical structures
 - Organization charts
 - · Book contents (chapters, sections, paragraphs)
 - · Class inheritance diagrams
- Trees can be used to represent hierarchical structures

5/25/2004 (c) 2001-4, University of Washington 20-3

Looking Ahead To An Old Goal

- · Finding algorithms and data structures for fast searching
 - · A key goal
- Sorted arrays are faster than unsorted arrays, for searching
 Can use binary search algorithm
 - Not so easy to keep the array in order
- LinkedLists were faster than arrays (or ArrayLists), for insertion and removal operations

The extra flexibility of the "next" pointers avoided the cost of sliding But... LinkedLists are hard to search, even if sorted

- Is there an analogue of LinkedLists for sorted collections??
- The answer will be...Yes: a particular type of tree!

/25/2004 (c) 2001-4, University of Washington 20-4

Tree Definitions

- · A tree is a collection of nodes connected by edges
- · A node contains
 - · Data (e.g. an Object)
 - References (edges) to two or more *subtrees* or *children*
- · Trees are hierarchical
 - · A node is said to be the parent of its children (subtrees)
 - There is a single unique *root* node that has no parent
 - · Nodes with no children are called *leaf nodes*
 - · A tree with no nodes is said to be empty

5/25/2004 (c) 2001-4, University of Washington 20-5

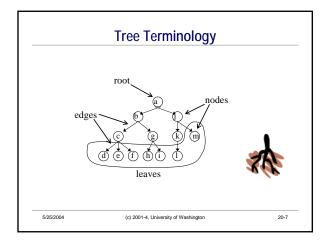
Drawing Trees

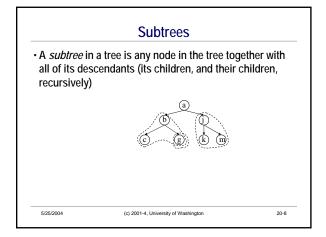
• For whatever reason, computer sciences trees are normally drawn upside down: root at the top

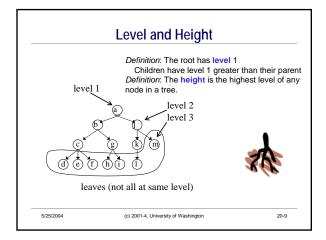


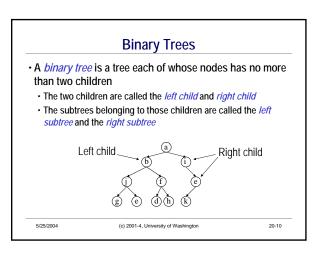


(c) 2001-4, University of Washington









Tree Algorithms

- The definition of a tree is naturally recursive:
 - A tree is either null (empty), or data + left (sub-)tree + right (sub-)tree
 - · Base case(s)?
 - · Recursive case(s)?
- Given a recursively defined data structure, recursion is often a very natural technique for algorithms on that data structure
 - Don't fight it!

5/25/2004

(c) 2001-4, University of Washington

public class BinTree { ... /** Return the number of items in this tree */ public int size() { return subtreeSize(root); } // Return the number of nodes in the (sub-)tree with root n private int subtreeSize(BTNode n) { if (n == null) { return ______; } else { return ______; } } 5/25/2004 (c) 2001-4, University of Washington 20-14

Tree Traversal

- Functions like subtreeSize systematically "visit" each node in a tree
 - · This is called a traversal
 - · We also used this word in connection with lists
- Traversal is a common pattern in many algorithms
 - The processing done during the "visit" varies with the algorithm
- · What order should nodes be visited in?
 - · Many are possible
 - Three have been singled out as particularly useful for binary trees: *preorder*, *postorder*, and *inorder*

5/25/2004

(c) 2001-4, University of Washington

20-15

Traversals

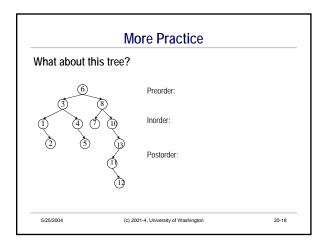
- · Preorder traversal:
- · "Visit" the (current) node first
 - i.e., do what ever processing is to be done
- Then, (recursively) do preorder traversal on its children, left to right
- · Postorder traversal:
 - First, (recursively) do postorder traversals of children, left to right
- · Visit the node itself last
- · Inorder traversal:
- (Recursively) do inorder traversal of left child
- · Then visit the (current) node
- Then (recursively) do inorder traversal of right child
 Footnote: pre- and postorder make sense for all trees; inorder only for binary trees

5/25/2004

(c) 2001-4, University of Washington

20-16

In what order are the nodes visited, if we start the process at the root? Preorder: Inorder: Postorder: Output Description: Postorder: Output Description: Output Descri



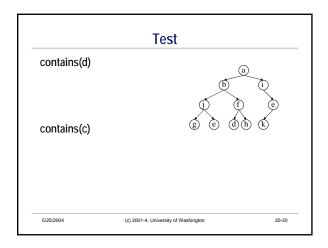
```
New Algorithm: contains

Return whether or not a value is an item in the tree public class BinTree {

/** Return whether elem is in tree '/ public boolean contains(Object elem) {
    return subtreeContains(root, elem):
    }

// Return whether elem is in (sub-)tree with root r
    private boolean subtreeContains(BTNode r, Object elem) {
    if (r == null) {
        return _____;
    } else {
        return _____;
    } else {
        return _____;
    }
}

5/25/2004 (c) 2001-4, University of Waashington 20-19
```



Cost of contains • Work done at each node: • Number of nodes visited: • Total cost: • Can we do better?