









# Formal Textbook Definition

- A *general tree* T is either empty, or is a set of nodes such that T is partitioned into disjoint subsets:
  - 1. A subset with a single node r (called the root)
  - 2. Subsets that are themselves general trees (these are called the subtrees of T).
- Notes:
  - This definition is recursive!
  - The nodes are not defined. They can be anything, and still satisfy the definition.

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# Description of the problem of the problem

















# **Binary Trees and Recursion**

struct BTreeNode {
 int item;
 BTreeNode \*left;
 BTreeNode \*right;
};

- Note the recursive data structure
- Algorithms often are recursive as well
- Don't fight it! Recursion is going to be the natural way to express the algorithms
  - Challenge: code CountNodes without using recursion

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# Analyses What is running time of these algorithms? Time to execute for one node: O(1) Number of recursive calls: O(N) N is the number of nodes in tree There's no way to miss any node There's no way to get to any node twice Each node is called from its parent, and a node has only one parent

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### Do try these at home!

- 1. Find the sum of all the values (items) in a binary tree of integers
- 2. Find the smallest value in a B.T. of integers
- 3. (A little harder) Count the number of <u>leaf</u> nodes in a B.T.
- 4. (A little harder) Find the average of all the values in a B.T. (one approach: think in terms of a "kickoff" function)

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# Recursive Tree Searching • How to tell if a data item is in a binary tree? // true iff "item appears in tree with given root" bool find(BTreeNode \*root, int item) { if ( root == NULL ) return false; else if ( root->data == item ) return true; else return ( find(root->left, item) || find(root->right, item) ); } 08/1201 W-23



## Tree Traversal

- Functions to count nodes, find height, sum, etc. systematically "visit" each node
- This is called a traversal
  - We also used this word in connection with lists.
- Traversal is a common pattern in many algorithms
  - The processing done during the "visit" varies with the algorithm
- What order should nodes be visited in?
  - Many are possible
  - Three have been singled out as particularly useful: preorder, postorder, and inorder 08/12/01 W-25



Inorder • Unlike pre- and post-, makes sense only for binary trees • Inorder traversal: - (Recursively) do inorder traversal of left child - Then visit the (current) node - Then (recursively) do inorder traversal of right child 08/12/01 W-27











# Sidebar: Syntax and Expression Trees

- Computer programs have a hierarchical structure
  - All statements have a fixed form
  - Statements can be ordered and nested almost arbitrarily (nested if-then-else)
- Can use a structure known as a *syntax tree* to represent programs
  - Trees capture hierarchical structure

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# Syntax Trees

- Compilers usually use syntax trees when compiling programs
  - Can apply simple rules to check program for syntax errors
  - Easier for compiler to translate and optimize than text file
- Process of building a syntax tree is called *parsing*

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