









Sample			
Action	Result		
• type h	• h		
• type e	• he		
• type I	• hel		
• type o	• helo		
• type <	• hel		
• type I	• hell		
 type w 	• hellw		
• type <	• hell		
• type <	• hel		
• type <	• he		
• type <	• h		
• type i	• hi		
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What's common

- I have data to store
- •boxcars; characters
- •The order of adding data is remembered
- I can only remove or affect what I most recently put in
- •We say the data structure is LIFO or Last In, First Out, and we call it a Stack.
- •The point where you can add data is called the **Top**.
- boxcar train: Top is the end of the train
- character line: Top is the rightmost character

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Abstract Stack Operations *push(item)*: Adds an element to top of stack, increasing stack height by one *item pop()*: Removes topmost element from stack and returns it, decreasing stack height by one *item top()*: Returns a copy of topmost element of stack, leaving stack unchanged <u>No</u> "direct access" cannot index to a particular data item <u>No</u> way to traverse the collection









Stacks in CS

- Implementing function calls
 Activation records go on a stack
- Evaluating expressions
 How does a calculator (or compiler) understand (3 +4)/5?
 more later
- "Backtracking" to systematically try all combinations of possibilities
 - e.g., to explore paths through a maze

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A Stack Class Interface class IntStack { public: IntStack(); //constructor //should have operator= & copy // constructor, too bool isEmpty(); // = "this stack is empty" void push(int item);// add item to top int pop(); // remove and return top item int top(); // show the top item private: . . . }; ^{08/02/01} O-14













Stack Via Linked List (2)			
<pre>struct Node { int data; Node* next; };</pre>			
<pre>class IntStack { public: //same as before private: Node * top; //points to top</pre>			
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Discussion

- •Why learn three different ways to implement the same ADT?
- •What are the pro's and con's of each way?
- Programming effort?
- Speed (efficiency) of execution?Suitability to application?
- Other factors?

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Stack Application: Evaluating Expressions expressions like "3 * (4 + 5)" have to be evaluated by calculators and compilers We'll look first at another form of expression, called "postfix" or "reverse Polish notation" furns out a stack algorithm works like magic to do postfix evaluation And... another stack algorithm can be used to convert from infix to postfix!

Postfix vs. Infix

- Review: Expressions have operators (+, -, *, /, etc) and operands (numbers, variables)
- In everyday use, we write the binary operators in between the operands
- "4 + 5" means "add 4 and 5" • called *infix* notation
- •No reason why we couldn't write the two
- operands first, then the operator
- "4 5 +" would mean "add 4 and 5" • called *postfix* notation

riotation

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Why Postfix?

- •Does not require parentheses!
- Some calculators make you type in that way
- •Easy to process by a program
- The processing algorithm uses a stack for operands (data)
- simple and efficient

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CSE 143

Refinements and Errors

- If data stack is ever empty when data is needed for an operation:
- Then the original expression was bad
- Too many operators up to that point
- If the data stack is <u>not</u> empty after the last token has been processed and the stack popped:
- Then the original expression was bad
- Too few operators or too many operands

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A different algorithm converts from infix to postfix Uses a stack of operators. Algorithm: Read a token If operand, output it immediately If of', push the '(' on stack If operator: if stack top is an op of ⇒ precedence: pop and output stop when '(' is on top or stack empty push the new operator If o'), pop and output until '(' has been popped Repeat until end of input pop rest of stack

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- •Searching for a path through a maze
- Algorithm: try all possible sequences of locations in the maze until you find one that works (or no more to try)
- called "exhaustive search"
- A stack helps keep track of the possibilities
 traces a path of locations
- just like the recursive activation records in the mazesolver

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