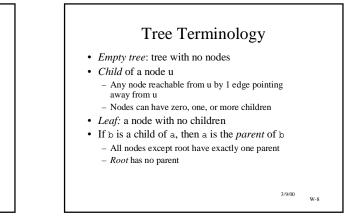
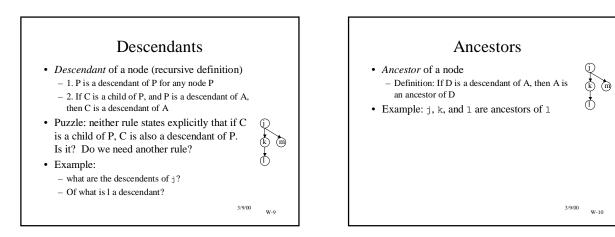
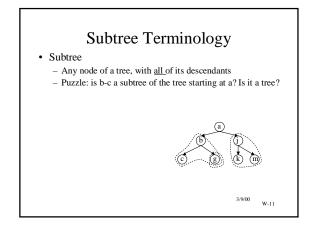


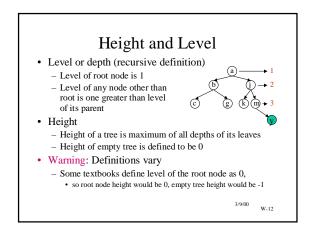
- A *general tree* T is either empty, or is a set of nodes such that T is partitioned into disjoint subsets:
 - 1. A subset with a single node $r \mbox{ (called the root)}$
 - 2. Subsets that are themselves general trees (these are called the subtrees of T).
- Notes:
 - This definition is recursive!
 - The nodes are not defined. They can be anything, and still satisfy the definition.

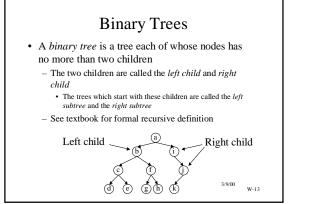
3/9/00 W-7

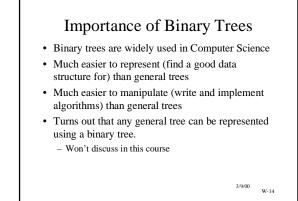


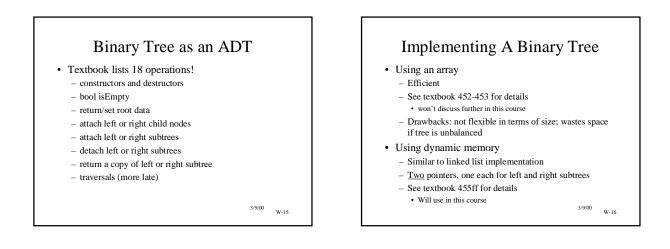


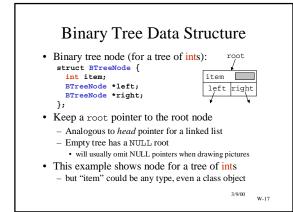


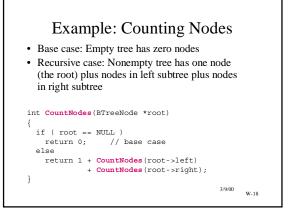


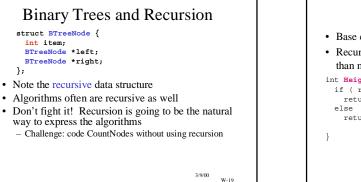


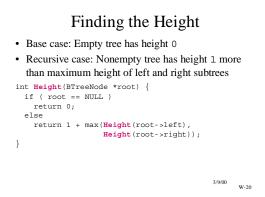


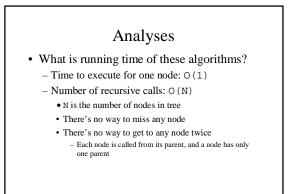




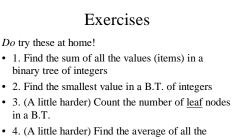






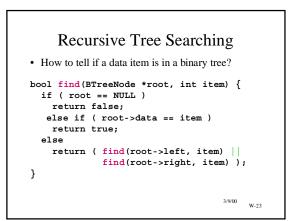


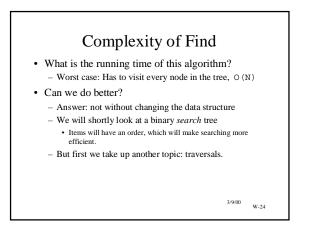
3/9/00 W-21



values in a B.T. (one approach: think in terms of a "kickoff" function)

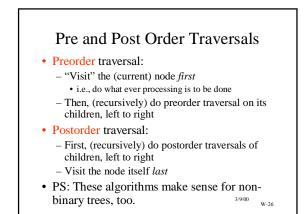
3/9/00 W-22

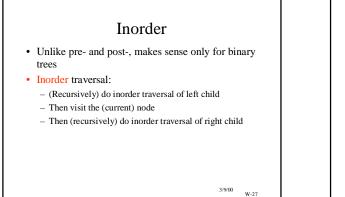


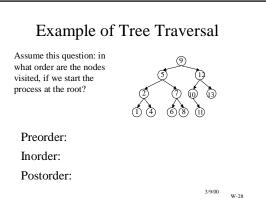


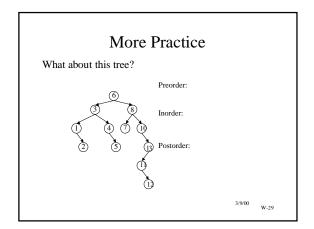
Tree Traversal

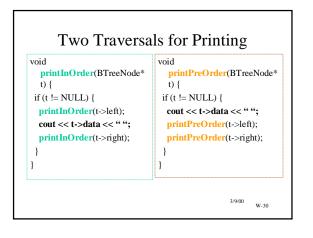
- Functions to count nodes, find height, sum, etc. systematically "visit" each node
- This is called a *traversal*
- We also used this word in connection with lists.
- Traversal is a common pattern in many algorithms
 - The processing done during the "visit" varies with the algorithm
- What order should nodes be visited in?
 Many are possible
 - Many are possible
 Three have been singled out as particularly useful: preorder, postorder, and inorder
 - 3/9/00 W-25

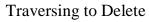








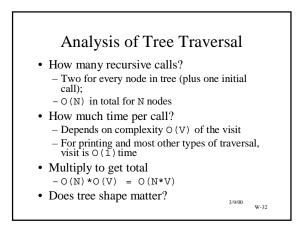




• Use a postorder traversal to return a whole tree to the heap.

```
void deleteTree(BTreeNode* t) {
  if (t != NULL) {
    deleteTree(t->left);
    deleteTree(t->right);
    delete t;
  }
}
```

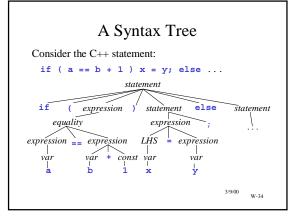
• Would inorder or preorder work just as $we_{MM}^{119?}$



Sidebar: Syntax and Expression Trees

- Computer programs have a hierarchical structure
 - All statements have a fixed form
 - Statements can be ordered and nested almost arbitrarily (nested if-then-else)
- Can use a structure known as a *syntax tree* to represent programs
 - Trees capture hierarchical structure

3/9/00 W-33



Syntax Trees

- Compilers usually use syntax trees when compiling programs
 - Can apply simple rules to check program for syntax errors
 - Easier for compiler to translate and optimize than text file
- Process of building a syntax tree is called *parsing*

3/9/00 W-35

