

# CSE / ENGR 142

## Programming I

### Recursion

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## Chapter 10: Recursion

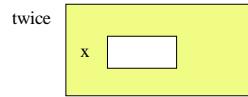
- 10.1 Nature of Recursion (skip "Mississippi" example 10.2)
- 10.2 Tracing: **Read!**
- 10.3 Recursive Math (but skip gcd example 10.6)
- 10.4 Skip
- 10.5 Skip
- 10.6 Towers of Hanoi: A Classic, but optional
- 10.7 Common Errors: **Read!**

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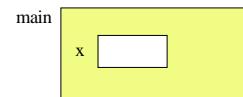
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### Review: Function Calling

```
int twice(int x) {
    return (2*x)
}
```



```
int main(void) {
    int x=3;
    x=twice(5);
}
```



6/1/99      Each time a function is called, memory is allocated to store value of local variables (including parameters)      R-3

### What is Recursion?

- Defn: A function is **recursive** if it calls itself

```
int foo(int x) {
    ...
    y = foo(...);
    ...
}
```

- Questions:

- How can recursion possibly work?
- Why would I want to write a recursive function?

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### Program vs. Process

- **Program** = a set of instructions
  - akin to a recipe
  - akin to the blueprint for an information factory
- **Process** = activity performed by computer when obeying the instructions
  - akin to the activity of cooking
  - akin to operation of a working factory
    - NO NEED FOR CEMENT OR STEEL
      - Instead, just need to allocate memory for local variables!!
    - CAN CREATE MULTIPLE FACTORIES AS NEEDED
      - FROM THE SAME BLUEPRINTS!!!

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### Factorial Function Revisited

0! is 1
1! is 1
2! is 1 * 2
3! is 1 * 2 * 3
...

```
int factorial ( int n ) {
    int product, i;
    product = 1;
    for ( i = n; i > 1; i = i - 1 ) {
        product = product * i;
    }
    return (product);
}
```

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## Factorial via Recursion

```
/* 0! = 1! = 1; for n > 1, n! = n(n-1)! */
```

```
int factorial(int n)
{
    int t;
    if (n <= 1)
        t = 1;
    else
        t = n * factorial(n - 1);
    return t;
}
```

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0! is 1  
1! is 1  
n! is n \* (n-1)!, for n>1

E.g.: 3! = 3 \* 2!  
= 3 \* 2 \* 1!  
= 3 \* 2 \* 1

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## Review: Function Basics

- Tracing recursive functions is no sweat if you remember the basics about functions:

- Parameters and variables declared in a function are local to it
  - Allocated (created) on function entry.
  - De-allocated (destroyed) on function return.
- Parameters are initialized by copying values of arguments when a function is called.

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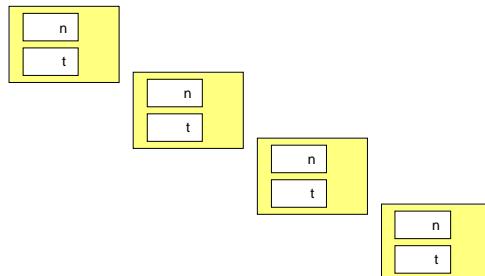
## Factorial

```
factorial(4) =
4 * factorial(3) =
4 * 3 * factorial(2) =
4 * 3 * 2 * factorial(1) =
4 * 3 * 2 * 1 = 24
```

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## Factorial Trace



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## Insist on 'y' or 'n'

```
char yes_or_no (void) {
    char answer = 'X';
    while (answer != 'y' && answer != 'n') {
        printf ("Please enter 'y' or 'n':");
        scanf (" %c", &answer);
    }
    return answer;
}
```

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## Insisting without Looping

```
char yes_or_no (void) {
    char answer;
    printf ("Please enter 'y' or 'n':");
    scanf (" %c", &answer);
    if (answer != 'y' && answer != 'n')
        answer = yes_or_no ( );
    return answer;
}
```

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## Iteration vs. Recursion

- Turns out **any** iterative algorithm can be reworked to use recursion instead (and vice versa).
- There are programming languages where recursion is the only choice(!)
- **Some algorithms are more naturally written with recursion**
  - But *naïve* applications of recursion can be inefficient

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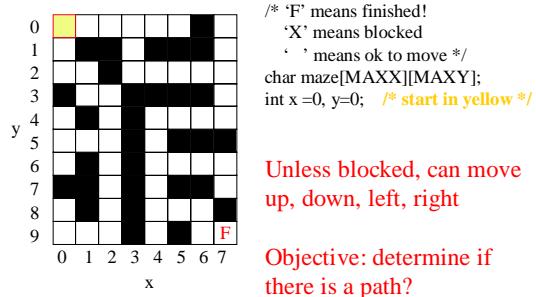
## When to use Recursion?

- **Problem has one or more simple cases**
  - These have a straightforward nonrecursive solution
- **Other cases can be redefined in terms of problems that are closer to simple cases**
  - By repeating this redefinition process one gets to one of the simple cases

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## Example: Path planning

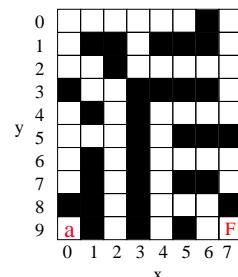


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## Simple Cases

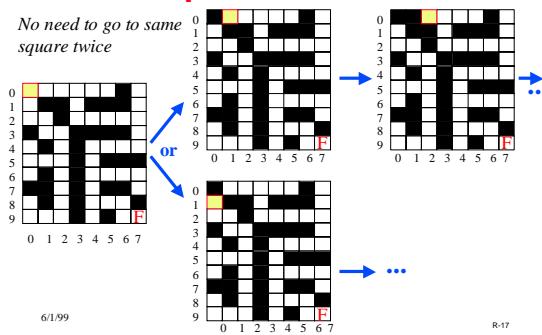
- Suppose at  $x,y$
- If  $\text{maze}[x][y] == 'F'$ 
  - Then "yes!"
- If no place to go
  - Then "no!"



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## Redefining a hard problem to several simpler ones



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## Helper function

```
/* Returns true if <x,y> is a legal move
   given the maze, otherwise returns false */
int legal_mv (char m[MAXX][MAXY],
               int x, int y) {
    return(x>=0 && x<=MAXX &&
           y>=0 && y<= MAXY &&
           m [x][y] != 'X');
}
```

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## Elegant Solution

```
/* Returns true if there is a path from <x,y> to an element of maze
   containing 'F' otherwise returns false */

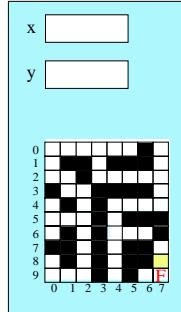
int is_path(char m[MAXX][MAXY ], int x, int y) {
    if (m [x][y] == 'F')
        return(TRUE);
    else {
        m[x][y] = 'X';
        return((legal_mv(m,x+1,y) && is_path(m,x+1,y)) ||
               (legal_mv(m,x-1,y) && is_path(m,x-1,y)) ||
               (legal_mv(m,x,y-1) && is_path(m,x,y-1)) ||
               (legal_mv(m,x,y+1) && is_path(m,x,y+1)))
    }
}
```

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## Example

is\_path(maze, 7, 8)

```
int is_path(char m[MAXX][MAXY ], int x, int y) {
    if (m [x][y] == 'F')
        return(TRUE);
    else {
        m[x][y] = 'X';
        return((legal_mv(m,x+1,y) && is_path(m,x+1,y)) ||
               (legal_mv(m,x-1,y) && is_path(m,x-1,y)) ||
               (legal_mv(m,x,y-1) && is_path(m,x,y-1)) ||
               (legal_mv(m,x,y+1) && is_path(m,x,y+1)))
    }
}
```



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## Example Cont is\_path(maze, 7, 7)

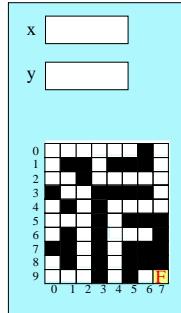
```
int is_path(char m[MAXX][MAXY ], int x, int y) {
    if (m [x][y] == 'F')
        return(TRUE);
    else {
        m[x][y] = 'X';
        return((legal_mv(m,x+1,y) && is_path(m,x+1,y)) ||
               (legal_mv(m,x-1,y) && is_path(m,x-1,y)) ||
               (legal_mv(m,x,y-1) && is_path(m,x,y-1)) ||
               (legal_mv(m,x,y+1) && is_path(m,x,y+1)))
    }
}
```

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## Example Cont is\_path(maze, 7, 9)

```
int is_path(char m[MAXX][MAXY ], int x, int y) {
    if (m [x][y] == 'F')
        return(TRUE);
    else {
        m[x][y] = 'X';
        return((legal_mv(m,x+1,y) && is_path(m,x+1,y)) ||
               (legal_mv(m,x-1,y) && is_path(m,x-1,y)) ||
               (legal_mv(m,x,y-1) && is_path(m,x,y-1)) ||
               (legal_mv(m,x,y+1) && is_path(m,x,y+1)))
    }
}
```



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