



## **Elementary statistics**

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## A dice-rolling game

- Two players each roll a die
- The higher roll wins
  - Goal: roll as high as you can!
- Repeat the game 6 times

#### Hypotheses regarding the outcome

- Luck
- Fraud
  - loaded die
  - inaccurate reporting

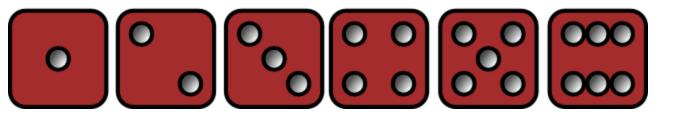
- How likely is luck?
- How do we decide?



#### Questions that statistics can answer

- I am flipping a coin. Is it fair?
   How confident am I in my answer?
- I have two bags of beans, each containing some black and some white beans. I have a handful of beans. Which bag did the handful come from?
- I have a handful of beans, and a single bag. Did the handful come from that bag?
- Does this drug improve patient outcomes?
- Which website design yields greater revenue?
- Which baseball player should my team draft?
- What premium should an insurer charge?
- Which chemical process leads to the best-tasting beer?

#### What can happen when you roll a die?



What is the likelihood of each?



## A dice-rolling experiment

Game: Roll one die, get paid accordingly:

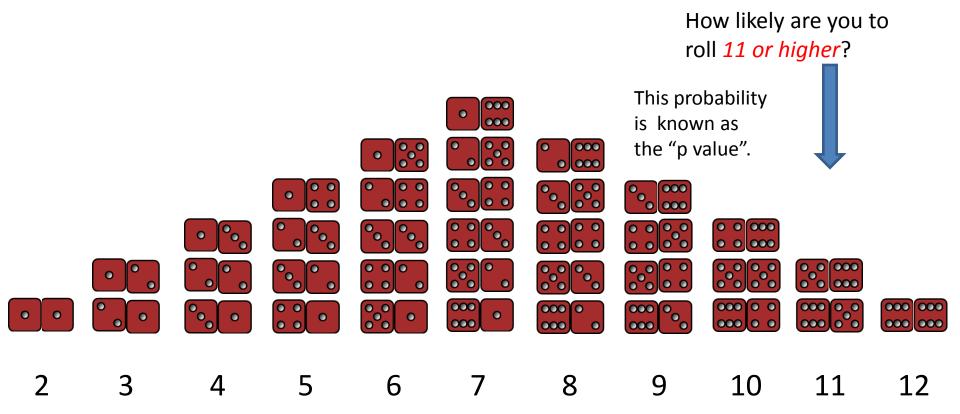
Roll	1	2	3	4	5	6
Payoff	1 CHF	2 CHF	3 CHF	4 CHF	5 CHF	0 CHF

Player self-reports the die roll and takes the money

no verification of the actual roll

From "Lies in disguise: An experimental study on cheating" by Urs Fischbacher and Franziska Heusi

#### What can happen when you roll two dice?



#### How to compute p values

- Via a statistical formula
  - Requires you to make assumptions and know which formula to use

- Computationally (simulation)
  - Run many experiments
  - Count the fraction with a better result
    - Requires a metric/measurement for "better"
  - Requires you to be able to run the experiments
  - We will use this approach exclusively

#### Interpreting p values

p value of 5% or less = statistically significant

This is a convention; there is nothing magical about 5%

Two types of errors may occur in statistical tests:

- false positive (or false alarm or Type I error): no real effect, but report an effect (through good/bad luck or coincidence)
  - If no real effect, a false positive occurs about 1 time in 20
- false negative (or miss or Type II error): real effect, but report no effect (through good/bad luck or coincidence)

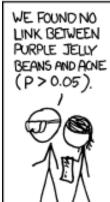
The *larger* the sample, the *less the likelihood* of a false positive or negative







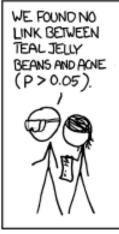












WE FOUND NO LINK BETWEEN SALMON JELLY BEANS AND ACNE

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WE FOUND NO LINK BETWEEN RED JELLY BEANS AND ACNE

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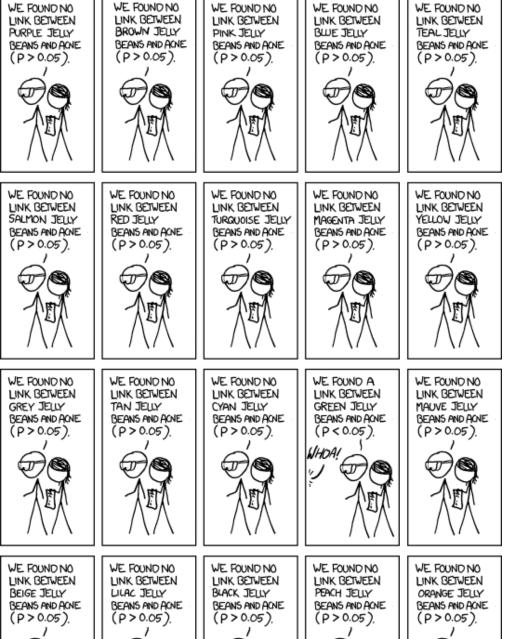
WE FOUND NO LINK BETWEEN TURQUOISE JELLY BEANS AND AONE

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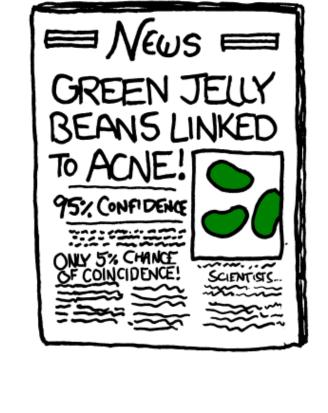
WE FOUND NO LINK BETWEEN MAGENTA JELLY BEANS AND ACNE (P > 0.05)

1 1 1 WE FOUND NO LINK BETWEEN YELLOW JELLY BEANS AND ACNE (P > 0.05)

http://xkcd.com/882/

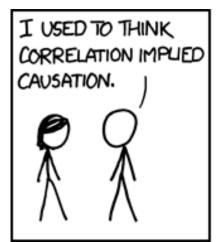




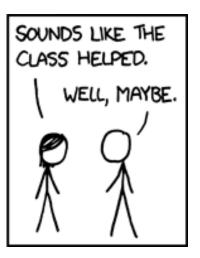


#### **Correlation** ≠ causation

Ice cream sales and murder rates are correlated







# Statistical significance ≠ practical importance

#### Summary of statistical methodology

- 1. Decide on a metric (bigger value = better)
- 2. Observe what you see in the real world
- Hypothesize that what you saw is normal/typical This is the "null hypothesis"
- 4. Simulate the real world many times
- 5. How different is what you observed from the simulations?
  - What percent of the simulation values are bigger than the real world values?
- If the percentage is 5% or less, reject the null hypothesis

# Analogy between hypothesis testing and mathematical proofs

"The underlying logic [of hypothesis testing] is similar to a proof by contradiction. To prove a mathematical statement, A, you assume temporarily that A is false. If that assumption leads to a contradiction, you conclude that A must actually be true."

From the book *Think Statistics* by Allen Downey

#### A common error

- 1. Observe what you see in the real world
- 2. Decide on a metric (bigger value = better)

This is backwards

For any observation, there is something unique about it.

Example: Roll dice, then be amazed because what are the odds you would get exactly that combination of rolls?

## Don't trust your intuition

- People have very bad statistical intuition
- It's much better to follow the methodology and do the experiments