LEC 07

CSE 123

Runtime Analysis

Questions during Class?

Raise hand or send here

cs.uw.edu/123/poll

sli.do #cse123x

BEFORE WE START

Talk to your neighbors:

What was the latest Youtube rabbit hole you went down?

Instructors: Brett Wortzman
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TAs:

Arohan	Neha	Rushil	Johnathan	Nicholas
Sean	Hayden	Srihari	Benoit	Isayiah
Audrey	Chris	Andras	Jessica	Kavya
Cynthia	Shreya	Kieran	Rohan	Eeshani
Amy	Packard	Cora	Dixon	Nichole
Trien	Lawrence	Liza	Helena	

Music: CSE 123 25wi Lecture Tunes

Announcements

- Resubmission Period 1 closes tonight at 11:59pm
- Programming Project 1 out now, due Feb. 12 at 11:59pm
- Brett's office hours scheduled!
  - See Staff page for date/time
- Quiz 0 grades released sometime next week
  - After makeups are complete, before Quiz 1

Runtime Analysis

- What's the "best" way to write code?
  - Depends on how you define best: Code quality, memory usage, speed, etc.

- Runtime = most popular way of analyzing solutions
  - Slow code = bad for business
- How do we figure out how long execution takes?
  - Stopwatch = human error
  - Computers = computer error (artifacts, operating systems, language)
  - Need a way to formalize abstractly…

Runtime Analysis

- We'll count simple operations as 1 unit
  - variable initialize / update `int x = 0;`
  - array accessing `arr[0] = 10;`
  - conditional checks `if (x < 10) {`

- Goal: determine how the number of operations scales w/ input size
  - Don't care about the difference between 2 and 4
  - Find the appropriate **complexity class**

- Result: evaluation tactic independent of OS, language, compiler, etc.
  - Simple operation = constant regardless of if it is truly 1

Complexity Classes

- Input will always be an array `arr` of length *n*
- Constant (1)
  - # Ops doesn't relate to *n*

```
return arr[0];
```

- Linear (n)
  - # Ops proportional to *n*

```
for (int i = 0; i < arr.length; i++)
```

- Quadradic (n^2)
  - # Ops proportional to *n^2*

```
for (int j = 0; j < arr.length; j++)
    for (int j = 0; j < arr.length; j++)
```

- Lets say # Ops = n^2 + 100000n
  - If n was really, really, really big, which term matters more?
  - Only care about the **dominating term** for complexity!

Complexity Classes

What's the complexity class of the following?

```
public static void mystery(int[] arr) {
    if (arr.length == 0) {
        throw new IllegalArgumentException();
    }
    return arr[arr.length - 1];
}
```

1
2
1

Constant Complexity (1)

Complexity Classes

What's the complexity class of the following?

```
public static int mystery(int[] arr) {
    int sum = 0;                          // 1
    for (int i = 0; i < arr.length; i++) {
        sum += arr[i];                    // 3
    }                                     // 3n
    return sum;                           // 1
}                                         // 3n + 2
```

Linear Complexity (n)

Complexity Classes

What's the complexity class of the following?

```
public static int mystery(int[] arr) {
    for (int i = 0; i < arr.length; i++) {
        for (int j = 0; j < arr.length; j++) {
            System.out.print(arr[i] + " ");
        }
        System.out.println();
    }
}
```

n(2n + 1)
= 2n^2 + n

2n

2

1

Quadratic Complexity (n^2)

Complexity Classes

What's the complexity class of the following?

```
public static int mystery(int[] arr) {
    for (int i = 0; i < arr.length; i++) {
        for (int j = i; j < arr.length; j++) {
            System.out.print(arr[i] + " ");
        }
        System.out.println();
    }
}
```

Quadratic Complexity (n^2)

Big-Oh Notation

- Programmers… are pessimists (or maybe realists)
  - Case in point: dominating term
- In the real world, best-case complexity isn't super useful
  - Want to make sure solutions work well in the worst possible situations

- We use Big-Oh notation to demonstrate worst-case complexity!

```
public static int indexOf(int[] arr, int x) {
    for (int i = 0; i < arr.length; i++) {
        if (arr[i] == x) return i;
    }
    return -1;
}
```

Worst-case linear

<u>O(n)</u>

ArrayList vs LinkedList

Operation	ArrayIntList	LinkedIntList
`size()`	O(1)	O(n)
`get(index)`	O(1)	O(n)
`add(val)`	O(1)	O(n)
`add(0, val)`	O(n)	O(1)
`add(index, val)`	O(n)	O(n)
`remove(0)`	O(n)	O(1)
`remove(n-1)`	O(1)	O(n)
`remove(index)`	O(n)	O(n)

How should we implement a stack?

- With an `ArrayIntList`?
  - push = what?
  - pop = what?

- With a `LinkedIntList`?
  - push = what?
  - pop = what?

Is running time an implementation detail?

- Yes
- No

- Does that help? :D