1. Comprehension

**Part A:** For each of the following binary trees, indicate which type of traversal is shown: pre-order, in-order, post-order, or none of these.

<table>
<thead>
<tr>
<th>Tree</th>
<th>Inorder</th>
<th>Preorder</th>
<th>Postorder</th>
<th>None</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image1.png" alt="Tree 1" /></td>
<td>44 -1 -2 -8 -9 7 2</td>
<td>☑️ pre-order</td>
<td>☧️ in-order</td>
<td>☐ post-order</td>
</tr>
<tr>
<td><img src="image2.png" alt="Tree 2" /></td>
<td>99 3 7 9 -1 -7 84 -1 5</td>
<td>☐ pre-order</td>
<td>☐ in-order</td>
<td>☑️ post-order</td>
</tr>
<tr>
<td><img src="image3.png" alt="Tree 3" /></td>
<td>99 8 -6 6 4 2 -1 -2 56</td>
<td>☐ pre-order</td>
<td>☑️ in-order</td>
<td>☐ post-order</td>
</tr>
</tbody>
</table>
Part B: Consider the following method in the IntTree class:

```java
public void parent() {
    int value = helper(overallRoot);
    if (value == 42) {
        System.out.println("42 is the meaning of life");
    } else {
        System.out.println("Continue the search for purpose…");
    }
}
```

```java
private int helper(IntTreeNode root) {
    if (root == null) {
        return -2;
    }

    return root.data + helper(root.left) + helper(root.right);
}
```

Draw a binary tree with at least 3 nodes that, if it were stored in the variable tree, the call tree.mystery() would print “42 is the meaning of life.”

Any tree with at least 3 nodes whose total sum adds up to exactly 42. Keep in mind the “-2” for every empty child.
2. Code Tracing

Consider the following recursive mystery method:

```java
public static boolean mystery(String str) {
    // custom method that removes all spaces found
    // ex: “hello world” -> “helloworld”
    String clean = str.removeAllSpaces();
    return helper(clean);
}

private static boolean helper(String str) {
    if (str.length() <= 1) {
        return true;
    }

    if (str.charAt(0) == str.charAt(str.length() - 1)) {
        return mystery(str.substring(1, str.length() - 1));
    } else {
        return false;
    }
}
```

Assume all string inputs are lowercase and have at least one character. For each of the following statements, indicate what the output would be:

- mystery("rotator")
  - true
- mystery("ufo tofu")
  - true
- mystery("never odd or even")
  - true
- mystery("high noon")
  - false
- mystery("yo banana boy")
  - true

This mystery program essentially checks whether the given string (not including spaces) is a palindrome.
3. Inheritance
Consider the following class:

```java
public class RecyclingCenter {
    private String location;
    private Map<String, Integer> materialCounts;
    private double totalWeightProcessed;

    public RecyclingCenter(String location) {
        this.location = location;
        this.materialCounts = new HashMap<>();
        this.totalWeightProcessed = 0;
    }

    public void processMaterials(String materialType, int count, double weight) {
        materialCounts.put(materialType, count);
        totalWeightProcessed += weight;
    }

    public int getMaterialCount(String materialType) {
        if (materialCounts.containsKey(materialType))
            return materialCounts.get(materialType);
        return 0;
    }

    public double getTotalWeightProcessed() {
        return totalWeightProcessed;
    }

    public boolean isEcoFriendly() {
        return totalWeightProcessed >= 10000;
    }
}
```

Write a new class called `AdvancedRecyclingCenter` that represents a more sophisticated recycling center with advanced sorting and processing capabilities. `AdvancedRecyclingCenter` should extend `RecyclingCenter` but differ in the following ways:

- **An AdvancedRecyclingCenter** has the ability to process electronic waste (e-waste) and keeps track of the integer number of e-waste eWasteCount and the double weight eWasteWeightProcessed. Include getter methods for the fields.
- **AdvancedRecyclingCenter** has a method `processEWaste()` that takes in a new count and new weight to add.
- **AdvancedRecyclingCenter** overrides the `isEcoFriendly()` method. In addition to the base class's criteria, an AdvancedRecyclingCenter is also considered eco-friendly if it has processed at least 1 metric ton of e-waste.

To earn an E on this problem, your AdvancedRecyclingCenter class must not duplicate any code from the RecyclingCenter class and must not include any unnecessary overrides.
public class AdvancedRecyclingCenter extends RecyclingCenter {
    private int eWasteCount;
    private double eWasteWeightProcessed;

    public AdvancedRecyclingCenter(String location) {
        super(location);
        this.eWasteCount = 0;
        this.eWasteWeightProcessed = 0;
    }

    public void processEWaste(int count, double weight) {
        eWasteCount += count;
        eWasteWeightProcessed += weight;
    }

    public int getEWasteCount() {
        return eWasteCount;
    }

    public double getEWasteWeightProcessed() {
        return eWasteWeightProcessed;
    }

    public boolean isEcoFriendly() {
        return super.isEcoFriendly() || eWasteWeightProcessed >= 1000;
    }
}
4. LinkedList Programming

Write an instance method called `cullMax()` that will be part of the `LinkedIntList` and accepts an integer value `int val`, and returns a new `LinkedIntList`. All ListNode values in the `LinkedIntList` that are less than or equal to the given integer value would stay in the original list while all values greater than the given integer value would be removed from the original and stored in a separate `LinkedIntList`. This list of nodes that have data values greater than the given integer value will be returned.

Consider the following given `LinkedIntList` and `val = 5`:

![Diagram of LinkedList with values 2, 8, 5, 3, 7, 4]

This will be the expected output if we have `LinkedIntList list2 = list1.cullMax(5)`.

Given List (list1):

![Diagram of List with values 2, 5, 3, 4]

Returned List (list2):

![Diagram of List with values 8, 7]

To earn an E on this problem, the original order of the provided `LinkedIntList` should be preserved and it doesn’t create any extra objects (other than the new 2nd list). This means auxiliary data structures are allowed. To earn a grade other than N, the method should still split the `LinkedIntList` in relation to the given integer value.

Write your solution on the next page.
Write your solution to problem #4 here:

```java
public LinkedList cullMax(int val) {
    LinkedList list2 = new LinkedList();
    ListNode curr2 = null;

    // front case
    while (this.front != null && this.front.data > val) {
        if (curr2 == null) {
            // if the new list is still empty
            list2.front = this.front;
            curr2 = list2.front;
        } else {
            curr2.next = this.front;
            curr2 = curr2.next;
        }
        this.front = this.front.next;
    }

    // middle and end cases
    ListNode curr = this.front;
    while (curr != null && curr.next != null) {
        if (curr.next.data > val) {
            if (curr2 == null) {
                // if the new list is still empty
                list2.front = curr.next;
                curr2 = list2.front;
            } else {
                curr2.next = curr.next;
                curr2 = curr2.next;
            }
            curr.next = curr.next.next;
        }
        curr = curr.next;
    }

    curr2.next = null;
    return list2;
}
```
5. Recursion Problem

Write a *recursive* method called letterCombinations that takes in one parameter, a String digits containing digits from 2-9, inclusive. Your method should return all possible letter combinations that a number could represent in a List of Strings. Return the answer in any order.

Here’s a throwback! A mapping of digits to letters (like on an old-school telephone) is given below. Note that 1 does not map to any letters.

```
1  ABC
2  DEF
3
4  GHI
5  JKL
6  MNO
7  PQRS
8  TUV
9  WXYZ
0
*   
```

For example, the call letterCombinations(“23”) would produce the following output.

```
Output: ["ad","ae","af","bd","be","bf","cd","ce","cf"]
```

Some other examples include:

```
Input: digits = ""
Output: []
```

```
Input: digits = "2"
Output: ["a","b","c"]
```

You may return the combinations in any order, but to earn an E, you must print *all* combinations and you must not print any combination more than once. To earn a grade other than N, your method **must** be implemented recursively, though you may also use loops as part of your recursive algorithm.

This constant will be provided to you and is encouraged to use in your solution:

```
static String[] KEYPAD = new String[]{"", "", "abc", "def", "ghi", "jkl", "mno", "pqrs", "tuv", "wxyz"};
```

Write your solution on the next page.
public static List<String> letterCombinations(String digits) {
    List<String> res = new ArrayList<>();
    letterCombinations("", 0, digits, res);
    return res;
}

private static void letterCombinations(String soFar, int index, String digits, List<String> res) {
    if (index == digits.length()) {
        res.add(soFar);
    } else {
        int currDigit = (int) digits.charAt(index);
        String options = KEYPAD[currDigit - '0']; // char->int trick
        for (int i = 0; i < options.length(); i++) {
            soFar += options.charAt(i); // choose
            letterCombinations(soFar, index + 1, digits, res); // explore
            soFar = soFar.substring(0, soFar.length() - 1); // unchoose
        }
    }
}
6. Binary Search Tree Problem

Consider the given class:

```java
public class DictionaryTree {
    private TreeNode overallRoot;

    public DictionaryTree() {
        overallRoot = null;
    }

    ...

    private class TreeNode {
        public String key;
        public int value;
        public TreeNode left, right;

        public TreeNode(String key, int value) {
            this.key = key;
            this.value = value;
            this.left = null;
            this.right = null;
        }
    }
}
```

Add a new method to the given `DictionaryTree` class called `insert()` that accepts a new `key` and `value` to insert into the tree. This method should modify the tree and add a node to the correct spot as described below:

- Compare each key to the current TreeNode:
  - If the `key` is less than the current node’s `key`, traverse to the left
  - If the `key` is greater than the current node’s `key`, traverse to the right
  - Continue the traversal until a spot is available to insert (i.e. current node is null)
- If the `key` already exists in the Tree, replace the existing `value` with the new given `value`

To earn an E, the node should be inserted into the correct place. Be sure to account for edge cases such as if the tree is empty. To earn a grade other than N, your method must be implemented recursively, though loops can be used (if necessary) as part of the recursive algorithm.

Write your solution on the next page.
public void insert(String key, int value) {
    overallRoot = insertHelper(root, key, value);
}

private TreeNode insertHelper(TreeNode root, String key, int value) {
    if (root == null) {
        root = new IntTreeNode(key, value);
        return root;
    }
    if (key < root.key) {
        root.left = insertHelper(root.left, key, value);
    } else if (key > root.key) {
        root.right = insertHelper(root.right, key, value);
    } else {
        root.value = value;
    }
    return root;
}