

# Reading

Jain, Kasturi, Schunck, *Machine Vision*. McGraw-Hill, 1995. Sections 4.2-4.4, 4.5(intro), 4.5.5, 4.5.6, 5.1-5.4. [online handut]

## What is an image?

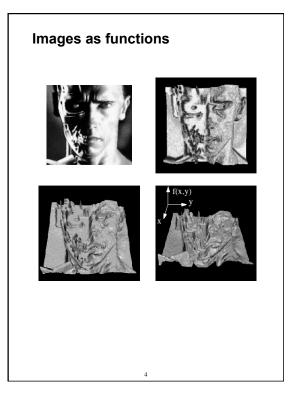
We can think of an **image** as a function, f, from  $\mathbb{R}^2$  to  $\mathbb{R}$ :

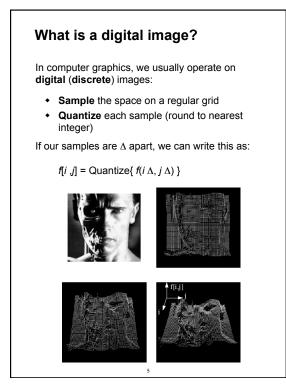
- f (x, y) gives the intensity of a channel at position (x, y)
- Realistically, we expect the image only to be defined over a rectangle, with a finite range:
  *f*: [*a*, *b*] x [c, d] → [0,1]

A color image is just three functions pasted together. We can write this as a "vector-valued" function:

$$f(x,y) = \begin{bmatrix} r(x,y) \\ g(x,y) \\ b(x,y) \end{bmatrix}$$

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### Image processing

An **image processing** operation typically defines a new image *g* in terms of an existing image *f*.

The simplest operations are those that transform each pixel in isolation. These pixel-to-pixel operations can be written:

g(x,y) = t(f(x,y))

Examples: threshold, RGB  $\rightarrow$  grayscale

Note: a typical choice for mapping to grayscale is to apply the YIQ television matrix and keep the Y.

ſŶ	1	[0.299	0.587	ן0.114	[ <i>R</i> ]
/	=	0.596	<b>0.587</b> -0.275 -0.523	-0.321	G
Q		0.212	-0.523	0.311	B

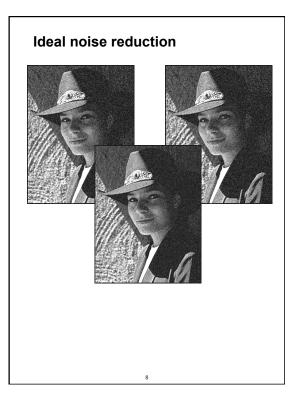
### Noise

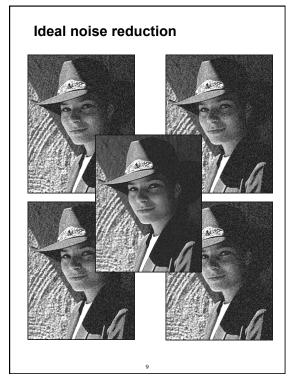
Image processing is also useful for noise reduction and edge enhancement. We will focus on these applications for the remainder of the lecture...  $\overbrace{Origina} \qquad \overbrace{Origina} \qquad \overbrace{Origina}$ 

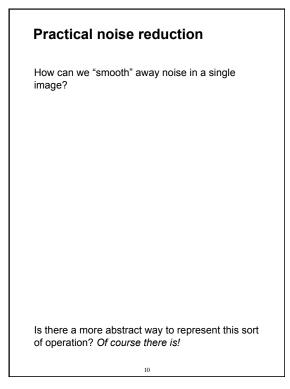
Impulse noise Gaussian noise

Common types of noise:

- Salt and pepper noise: contains random occurrences of black and white pixels
- Impulse noise: contains random occurrences of white pixels
- Gaussian noise: variations in intensity drawn from a Gaussian normal distribution







# **Discrete convolution** One of the most common methods for filtering an image is called **discrete convolution**. (We will just call this "convolution" from here on.) In 1D, convolution is defined as: $g[n] = f[n] * h[n] \\ = \sum_{n} f[n']h[n-n'] \\ = \sum_{n} f[n']h[n'-n]$ where h[n] = h[-n].

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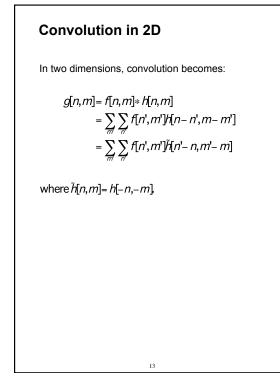
## **Discrete convolution**

One can show that convolution has some convenient properties. Given functions *a*, *b*, *c*:

a\*b=b\*a (a\*b)\*c=a\*(b\*c) a\*(b+c)=a\*b+a\*c

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We'll make use of these properties later...



# **Convolution representation**

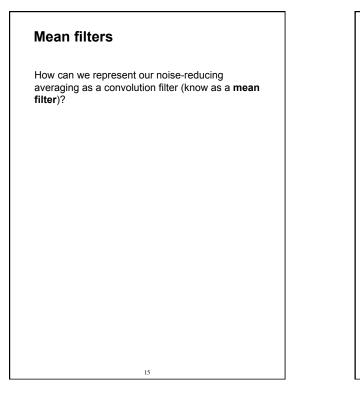
Since *f* and *h* are defined over finite regions, we can write them out in two-dimensional arrays:

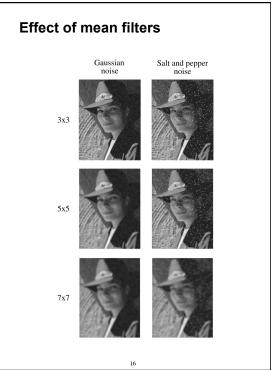
128	54	9	78	100
145	98	240	233	86
89	177	246	228	127
67	90	255	237	95
106	111	128	167	20
221	154	97	123	0

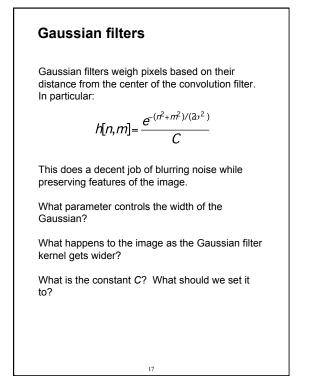
X 0.1	X 0.1	X 0.1
X 0.1	X 0.2	X 0.1
X 0.1	X 0.1	X 0.1

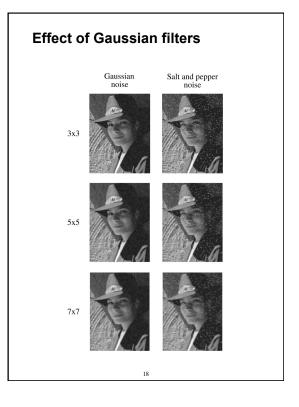
Note: This is not matrix multiplication!

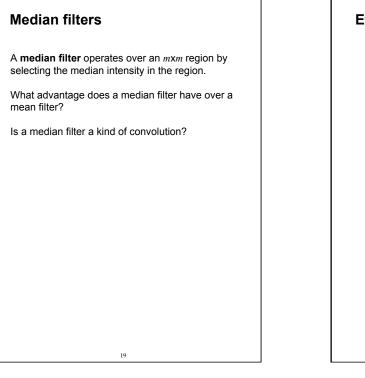
 ${\bf Q}:$  What happens at the boundary of the image?  $$_{\rm 14}$$ 

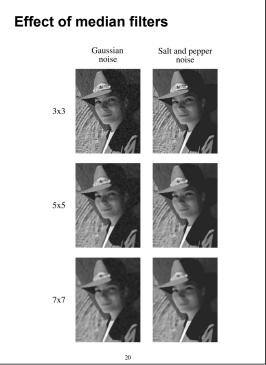


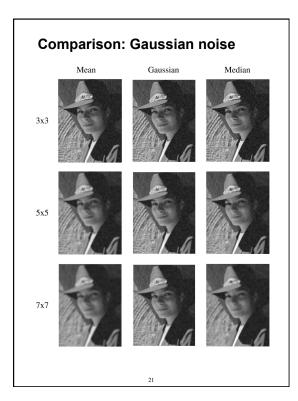


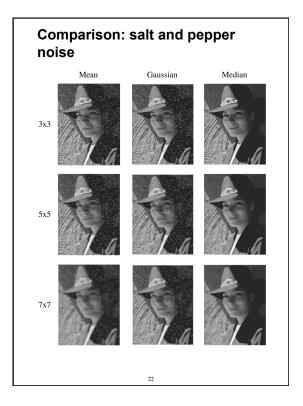


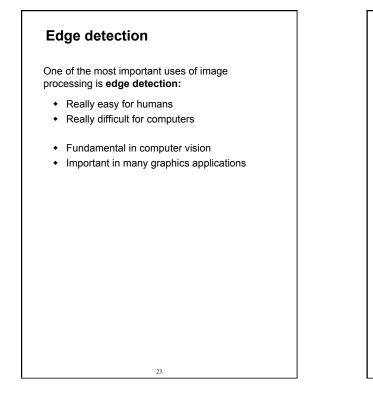


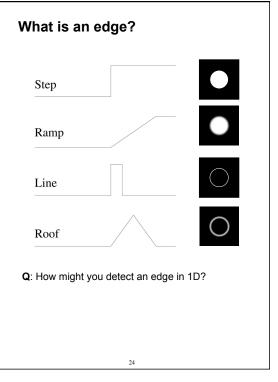














The **gradient** is the 2D equivalent of the derivative:

$$\nabla f(x, y) = \left(\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}\right)$$

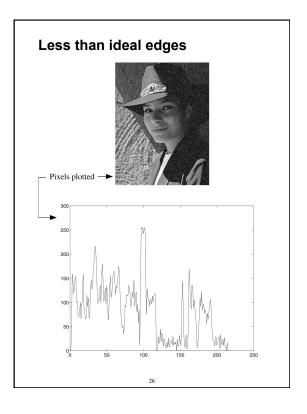
Properties of the gradient

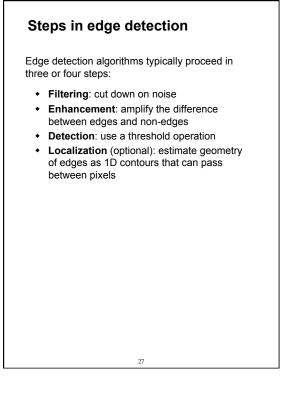
- It's a vector
- Points in the direction of maximum increase of *f*

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Magnitude is rate of increase

How can we approximate the gradient in a discrete image?





## Edge enhancement

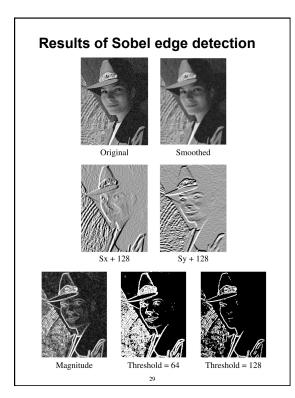
A popular gradient filter is the Sobel operator:

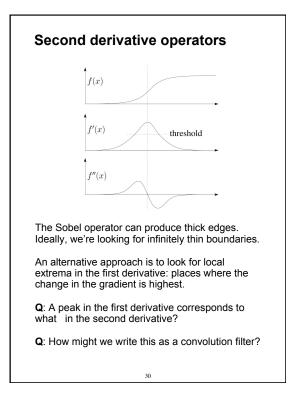
 $\tilde{s}_{x} = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$  $\tilde{s}_{y} = \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$ 

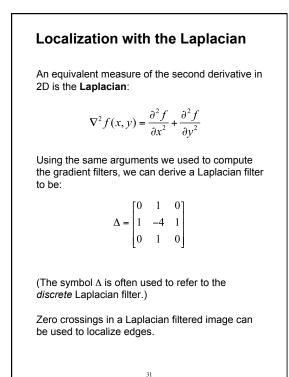
We can then compute the magnitude of the vector  $(\tilde{s}_x, \tilde{s}_y)$ .

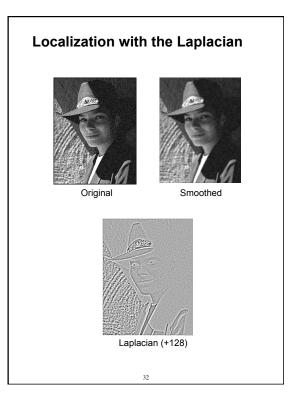
Note that these operators are conveniently "preflipped" for convolution, so you can directly slide these across an image without flipping first.

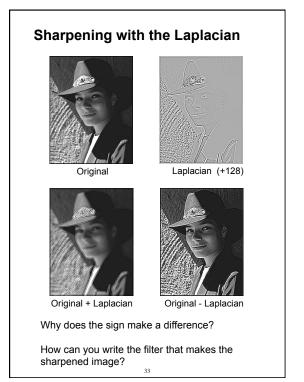
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# Summary

What you should take away from this lecture:

- The meanings of all the boldfaced terms.
- How noise reduction is done
- How discrete convolution filtering works
- The effect of mean, Gaussian, and median filters
- What an image gradient is and how it can be computed
- + How edge detection is done
- What the Laplacian image is and how it is used in either edge detection or image sharpening

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