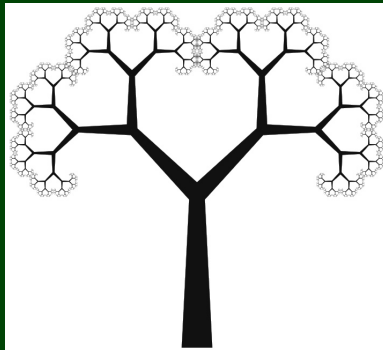


CSE 143

Computer Programming II

Binary Search Trees (BSTs)



Outline

1 More Tree Methods

2 Introducing BSTs

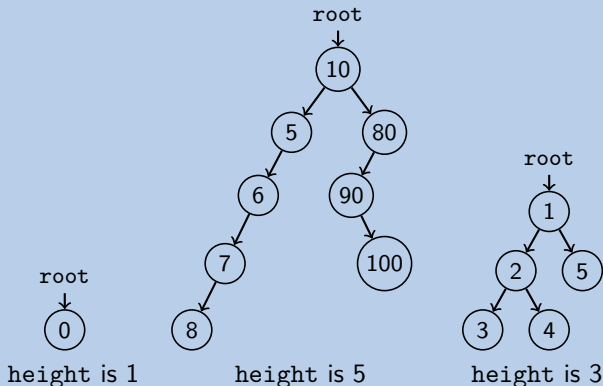
3 BST Methods

height

Write a tree method called `height` (inside the `IntTree` class) with the following method signature:

```
public int height()
```

that returns the number of nodes on the **longest path** from the root to any leaf. For example,



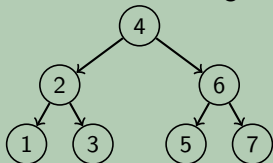
```
1 public int height() {
2     return height(this.root);
3 }
4
5 private int height(IntTreeNode current) {
6     // A null tree has height 0
7     if (current == null) {
8         return 0;
9     }
10    else {
11        // Find the largest path by taking the max
12        // of both branches recursively (and adding 1 for this node)
13        return 1 + Math.max(
14            height(current.left),
15            height(current.right)
16        );
17    }
18 }
```

Recall contains()

```
1 private boolean contains(IntTreeNode current, int value) {
2     /* If the tree is null, it definitely doesn't contain value... */
3     if (current == null) { return false; }
4
5     /* If current *is* value, we found it! */
6     else if (current.data == value) { return true; }
7
8     else {
9         return contains(current.left, value) ||
10            contains(current.right, value);
11     }
12 }
```

Runtime of contains(7)

Consider the following tree:

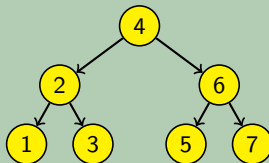
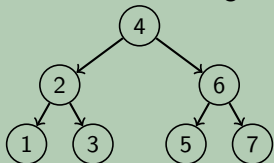


Recall contains()

```
1 private boolean contains(IntTreeNode current, int value) {
2     /* If the tree is null, it definitely doesn't contain value... */
3     if (current == null) { return false; }
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5     /* If current *is* value, we found it! */
6     else if (current.data == value) { return true; }
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8     else {
9         return contains(current.left, value) ||
10            contains(current.right, value);
11     }
12 }
```

Runtime of contains(7)

Consider the following tree: Which nodes do we visit for contains(7)

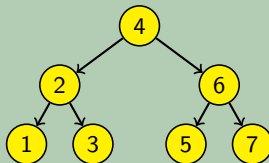
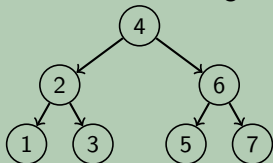


Recall contains()

```
1 private boolean contains(IntTreeNode current, int value) {
2     /* If the tree is null, it definitely doesn't contain value... */
3     if (current == null) { return false; }
4
5     /* If current *is* value, we found it! */
6     else if (current.data == value) { return true; }
7
8     else {
9         return contains(current.left, value) ||
10            contains(current.right, value);
11     }
12 }
```

Runtime of contains(7)

Consider the following tree: Which nodes do we visit for contains(7)



That makes the code $\mathcal{O}(n)$. Can we do better?

In general, **we can't do better**. BUT, sometimes, we can!

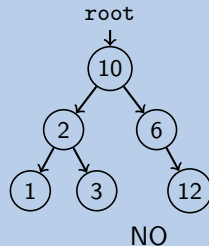
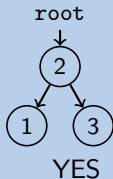
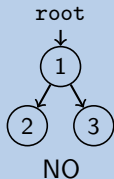
Definition (Binary **SEARCH** Tree (BST))

A binary tree is a **BST** when an **in-order traversal of the tree** yields a sorted list.

To put it another way, a binary tree is a **BST** when:

- All data “to the left of” a node is less than it
- All data “to the right of” a node is greater than it
- All sub-trees of the binary tree are also BSTs

Example (Which of the following are BSTs?)



isBST

Write a function `isBST` with the following signature:

```
private boolean isBST(IntTreeNode current, Integer min,  
                      Integer max)
```

that returns true if the tree at root `current` is a BST.

```
1 private boolean isBST(IntTreeNode current, Integer min, Integer max) {  
2     if (current == null) {  
3         return true;  
4     }  
5     else if ((min != null && current.data < min) ||  
6             (max != null && current.data > max)) {  
7         return false;  
8     }  
9     else if (!isBST(current.left, min, current.data)) {  
10        return false;  
11    }  
12    else {  
13        return isBST(current.right, current.data, max);  
14    }  
15 }
```

Write contains() for a BST

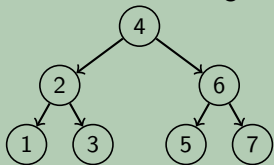
Fix contains so that it takes advantage of the BST properties.

Recall contains()

```
1 private boolean contains(IntTreeNode current, int value) {
2     /* If the tree is null, it definitely doesn't contain value... */
3     if (current == null) { return false; }
4
5     /* If current *is* value, we found it! */
6     else if (current.data == value) { return true; }
7
8     else if (current.data < value) {
9         return contains(current.right, value);
10    }
11    else {
12        return contains(current.left, value);
13    }
14 }
```

Runtime of (better) contains(7)

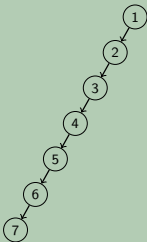
Consider the following tree:



That makes the code $\log n$. Much better!

WARNING!

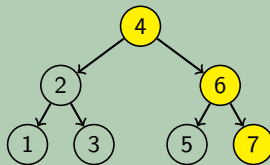
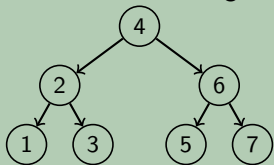
Consider the following tree:



This is the same tree, but now **we have to visit all the nodes!**

Runtime of (better) contains(7)

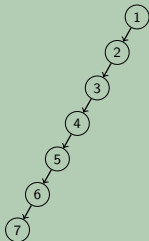
Consider the following tree: Which nodes do we visit for contains(7)



That makes the code $\log n$. Much better!

WARNING!

Consider the following tree:



This is the same tree, but now **we have to visit all the nodes!**

add

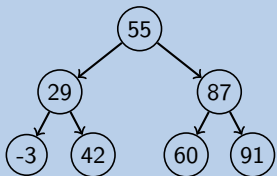
Write a method add in the BST class with the following signature:

```
public void add(int value);
```

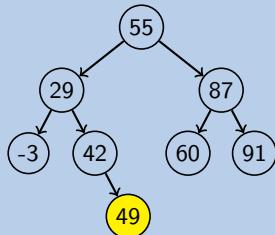
that preserves the BST property.

Example (tree.add(49))

Before



After



Attempt #1

```
1 public void add(int value) {
2     add(this.root, value);
3 }
4 private void add(Node current, int value) {
5     if (current == null) {
6         current = new Node(value);
7     }
8     else if (current.data > value) {
9         add(current.left, value);
10    }
11    else if (current.data < value) {
12        add(current.right, value);
13    }
14 }
```

What's wrong with this solution?

Just like with LinkedLists where we must change front or .next, we're not actually changing anything here. We're discarding the result.

Consider the following code:

```
1 public static void main(String[] args) {  
2     String s = "hello world";  
3     s.toUpperCase();  
4     System.out.println(s);  
5 }
```

OUTPUT

```
>> hello world
```

```
1 public static void main(String[] args) {  
2     String s = "hello world";  
3     s = s.toUpperCase();  
4     System.out.println(s);  
5 }
```

OUTPUT

```
>> HELLO WORLD
```

We must USE the result; otherwise, it gets discarded

If you want to write a method that can change the object that a variable refers to, you must do three things:

- 1 Pass in the original state of the object to the method
- 2 Return the new (possibly changed) object from the method
- 3 Re-assign the caller's variable to store the returned result

```
1    p = change(p); // in main
2    public static Point change(Point thePoint) {
3        thePoint = new Point(99, -1);
4        return thePoint;
5    }
```

Fixed Attempt

```
1 public void add(int value) {
2     this.root = add(this.root, value);
3 }
4 private Node add(Node current, int value) {
5     if (current == null) {
6         current = new Node(value);
7     }
8     else if (current.data > value) {
9         current.left = add(current.left, value);
10    }
11    else if (current.data < value) {
12        current.right = add(current.right, value);
13    }
14    return current;
15 }
```

This works because we **always update the result**, **always return the result**, and **always update the root**.

- BSTs can make searching/inserting/etc. much faster.
- Make sure that you can figure out if a tree is a BST or not.
- Whenever you are writing a BST method, you **must** use the `x = change(x)` pattern. It won't work otherwise.