











One More Important Choice

Sentence Splitter Solution

24 25

26

When doing recursive backtracking, we need to differentiate between:

- finding a result
- failing to find a result (e.g., backtracking)

Generally, we do this by treating null as a failure. For example:

- On the input, "thisisasentence", none of the recursive calls should return "thisis", because it isn't a word.
- If we get down to an empty string, that would indicate a failure; so, we'd return null

public String splitSentence(String sentence) { // The entire sentence is a dictionary word if (words.contains(sentence)) { return sentence; 5 6 // Try splitting at every character until we find one that works... for (int i = sentence.length() - 1; i > 0; i--){ 8 String left = sentence.substring(0, i); 10 String right = sentence.substring(i, sentence.length()); 11 // If the left isn't a word, don't bother recursing. // If it is, split the remainder of the sentence recursively. 12 13 14 if (words.contains(left)) { 15 right = splitSentence(right); 16 // Since the left was a word, if the right is also an answer, // then we found an answer to the whole thing! if (right != null) { return left + " " + right; 17 18 19

// Undo our choice by going back to sentence

Client vs. Implementor, again

6

You may have noticed that many of the class examples I've been showing involve me using a class that I've already written. There are several reasons for this:

- Learning to read and use an API is a really important programming skill
- Switching between the client and implementor views is an important goal of this course
- The code I write is usually easy, but really tedious (so, it would be a waste of time to write in class)

Take-Away

Every time I print out an API for you, you should try to understand it from the comments. This will help you on the homework, on exams, and in any future programming endeavors.

BooleanExpression

return null:

7

Today's API is BooleanExpression.

What is a BooleanExpression?

The BooleanExpression class allows us to represent the conditions we write in if statements. For instance, to represent the following:

We would do

new BooleanExpression("(!a && b)");

Notice that we use single letter variable names instead of queue.size() > 0. This is a simplification for implementation.

$\textbf{Evaluating} \ \texttt{BooleanExpression}$

8

Evaluating BooleanExpressions

Remember when we took (1+2)*3 and evaluated it to 9 recursively? We can do a similar thing for BooleanExpressions: Consider the BooleanExpression from above:

"(!a && b)"

Suppose we know the following:

- a is true.
- b is false.

What does this expression evaluate to?

 $(!\texttt{a \&\& b}) \longrightarrow (!\texttt{true \&\& false}) \longrightarrow (\texttt{false \&\& false}) \longrightarrow \texttt{false}$

Suppose we wanted to write a method:

public static boolean evaluate(BooleanExpression e, ??? assn)

where assn represents the truth values of the variables.

What type would assn be? It's a mapping from variables to truth values.

Evaluating BooleanExpression

9

Okay, so, we have:

Consider the following case:

evaluate return value?

- e is a && b
- assignments map is {a=true}.

What should evaluate return?

We can't answer the question. What seems like a good idea? null.

So, we change the return type to Boolean.

Who Should Implement evaluate?

10

Who Writes evaluate?

- The implementor of BooleanExpression
 - ...if so, it should be inside the BooleanExpression class
- The client of BooleanExpression
- ...if so, it should be outside the BooleanExpression class

The implementor of ${\tt BooleanExpression}$ should write the method, because then all the clients can use it.

That pesky static...

- If the implementor writes evaluate, then the method signature is: public Boolean evaluate(Map<String, Boolean> assn)
- If the client writes evaluate, then the method signature is:

```
public static Boolean evaluate(
   BooleanExpression e,
   Map<String, Boolean> assn
)
```

Uh Oh... How can we try assignments?

12

We don't have a way of passing assignments through to the function. How can we fix this?

public/private pair!

```
Public/Private Recursive Pair

public static boolean canBeTrue(BooleanExpression b)

private static boolean canBeTrue(
BooleanExpression b,
Map<String, Boolean> m
)
```

BTW, Why does this problem matter?

14

Solving canBeTrue quickly is the **most important** open problem in Computer Science.

If you solve this problem in $\mathcal{O}(n^k)$ time for any k, the following happen:

- You get one million dollars.
- You get a PhD.
- You become the most famous Computer Scientist, pretty much ever
- You break all banks, credit cards, website encryption, etc.

Finally, Back To Recursive Backtracking...

11

canBeTrue

Write a method

public static boolean canBeTrue(BooleanExpression b)

that returns true if it is possible for the input to to **evaluate to true** and false otherwise.

Some examples:

- \blacksquare a && b \longrightarrow if we have {a=true, b=true}, then it is true.
- a && !a → no matter what a is, this will always be false.

To do recursive backtracking, we need to answer these questions:

- What are the choices we're making incrementally? ...assignments of each variable to true/false
- How do we "undo" a choice?
 - ... remove the assignment from the map
- What are the base case(s)?
 - ... the assignment must be true/false

```
{\tt canBeTrue} \  \, {\color{red} \textbf{Solution}}
```

12

```
public static Map<String, Boolean> canBeTrue(BooleanExpression b) {
    Map<String, Boolean> assignmentMap = new TreeMap<>();
    if (canBeTrue(b, assignmentMap)) { // Some assignment works...
        return assignmentMap;
    }
    return null;
}

private static boolean canBeTrue(BooleanExpression b, Map<String, Boolean> m) {
    Boolean result = b.evaluate(m); // See if the current assignment works
    if (result!= null) { // If we can't answer, backtrack
        return result;
    }
}

Set<String> variables = b.getVariables();
variables.removeAll(m.keySet());
for (String variable : variables) { // Try to assign any
    boolean[] choices = (true, false); // variable we haven't
    for (boolean assignment);
    boolean assignment);
    boolean attempt = canBeTrue(b, m);
    if (attempt) { // If we found an
        return true; // assignment, we're good.
    }
    m.remove(variable); // Otherwise, backtrack
}

return false;
}

return false;
}
```