

CSE 143

Computer Programming II

Sorting



Outline

1 Selection Sort

2 Merge Sort

Why Do We Care About Sorting?

1

Sorting is a fundamental idea that is used in many places.

There are also **many different sorting algorithms** which gives us an opportunity to compare them.

How Do We Compare Sorts?

- Timing? (That's not so great, because it varies.)
- Number of steps? (What is a step?)
- Idea: **number of comparisons**

Selection Sort

2

Idea

Go from left to right and find the next smallest element. Then, put that element in the right place. Now we know everything up to that element is sorted. Continue until we get to the end of the array.

Code

```

1 public static void selectionsort(List<Integer> list) {
2     for (int i = 0; i < list.size(); i++) {
3         Integer index = null;
4         Integer selection = null;
5         for (int j = i; j < list.size(); j++) {
6             int next = list.get(j);
7             if (selection == null || next < selection) {
8                 selection = next;
9                 index = j;
10            }
11        }
12        // Swap index and i
13        list.set(index, list.get(i));
14        list.set(i, selection);
15    }
16 }
```

Merging Two Sorted Lists

3

Idea

Keep a finger on the last element we've handled from each list. Figure out which of the elements we're pointing to is smaller. Put the smaller one in the result and move that finger right. Keep on going until both fingers are past the last elements of their lists.

Code

```

1 public static List<Integer> merge(List<Integer> list1, List<Integer> list2) {
2     List<Integer> result = new ArrayList<Integer>(list1.size() + list2.size());
3     int i1 = 0;
4     int i2 = 0;
5     while (i1 + i2 < list1.size() + list2.size()) {
6         Integer a = null, b = null;
7         if (i1 < list1.size()) { a = list1.get(i1); }
8         if (i2 < list2.size()) { b = list2.get(i2); }
9         if (a != null && (b == null || a < b)) {
10             result.add(a);
11             i1++;
12         }
13         else {
14             result.add(b);
15             i2++;
16         }
17     }
18     return result;
19 }
```

Merge Sort By Picture

4

sort $\boxed{30 \ 10 \ 15 \ 5 \ 35 \ 25 \ 20 \ 80}$
 $a[0] \ a[1] \ a[2] \ a[3] \ a[4] \ a[5] \ a[6] \ a[7]$

sort $\boxed{30 \ 10 \ 15 \ 5}$
 $a[0] \ a[1] \ a[2] \ a[3]$

sort $\boxed{35 \ 25 \ 20 \ 80}$
 $a[4] \ a[5] \ a[6] \ a[7]$

sort $\boxed{30 \ 10}$
 $a[0] \ a[1]$

$\boxed{30} \quad \boxed{10}$

merge

$\boxed{10 \ 30}$
 $a[0] \ a[1]$

Merge Sort By Picture

5

sort $\boxed{30 \ 10 \ 15 \ 5 \ 35 \ 25 \ 20 \ 80}$
 $a[0] \ a[1] \ a[2] \ a[3] \ a[4] \ a[5] \ a[6] \ a[7]$

sort $\boxed{30 \ 10 \ 15 \ 5}$
 $a[0] \ a[1] \ a[2] \ a[3]$

sort $\boxed{35 \ 25 \ 20 \ 80}$
 $a[4] \ a[5] \ a[6] \ a[7]$

$\boxed{10 \ 30}$
 $a[0] \ a[1]$

Merge Sort By Picture

6

sort $\boxed{30 \ 10 \ 15 \ 5 \ 35 \ 25 \ 20 \ 80}$
 $a[0] \ a[1] \ a[2] \ a[3] \ a[4] \ a[5] \ a[6] \ a[7]$

sort $\boxed{30 \ 10 \ 15 \ 5}$
 $a[0] \ a[1] \ a[2] \ a[3]$

sort $\boxed{35 \ 25 \ 20 \ 80}$
 $a[4] \ a[5] \ a[6] \ a[7]$

$\boxed{10 \ 30}$
 $a[0] \ a[1]$

sort $\boxed{15 \ 5}$
 $a[2] \ a[3]$

$\boxed{15} \quad \boxed{5}$
 $a[2] \ a[3]$

merge

$\boxed{5 \ 15}$
 $a[2] \ a[3]$

Merge Sort By Picture

7

sort $\boxed{30 \ 10 \ 15 \ 5 \ 35 \ 25 \ 20 \ 80}$
 $a[0] \ a[1] \ a[2] \ a[3] \ a[4] \ a[5] \ a[6] \ a[7]$

sort $\boxed{30 \ 10 \ 15 \ 5}$
 $a[0] \ a[1] \ a[2] \ a[3]$

sort $\boxed{35 \ 25 \ 20 \ 80}$
 $a[4] \ a[5] \ a[6] \ a[7]$

$\boxed{10 \ 30}$
 $a[0] \ a[1]$

$\boxed{5 \ 15}$
 $a[2] \ a[3]$

Merge Sort By Picture

8

sort $\boxed{30 \ 10 \ 15 \ 5 \ 35 \ 25 \ 20 \ 80}$
 $a[0] \ a[1] \ a[2] \ a[3] \ a[4] \ a[5] \ a[6] \ a[7]$

sort $\boxed{30 \ 10 \ 15 \ 5}$
 $a[0] \ a[1] \ a[2] \ a[3]$

sort $\boxed{35 \ 25 \ 20 \ 80}$
 $a[4] \ a[5] \ a[6] \ a[7]$

$\boxed{10 \ 30}$
 $a[0] \ a[1]$

sort $\boxed{5 \ 15}$
 $a[2] \ a[3]$

merge

$\boxed{5 \ 10 \ 15 \ 30}$
 $a[0] \ a[1] \ a[2] \ a[3]$

Merge Sort By Picture

9

sort $\boxed{30 \ 10 \ 15 \ 5 \ 35 \ 25 \ 20 \ 80}$
 $a[0] \ a[1] \ a[2] \ a[3] \ a[4] \ a[5] \ a[6] \ a[7]$

$\boxed{5 \ 10 \ 15 \ 30}$
 $a[0] \ a[1] \ a[2] \ a[3]$

sort $\boxed{35 \ 25 \ 20 \ 80}$
 $a[4] \ a[5] \ a[6] \ a[7]$

Merge Sort By Picture

10

sort

30	10	15	5	35	25	20	80
a[0]	a[1]	a[2]	a[3]	a[4]	a[5]	a[6]	a[7]

5	10	15	30
a[0]	a[1]	a[2]	a[3]

sort

35	25	20	80
a[4]	a[5]	a[6]	a[7]

sort

35	25
a[4]	a[5]

35	25
a[4]	a[5]

merge

25	35
a[4]	a[5]

Merge Sort By Picture

11

sort

30	10	15	5	35	25	20	80
a[0]	a[1]	a[2]	a[3]	a[4]	a[5]	a[6]	a[7]

5	10	15	30
a[0]	a[1]	a[2]	a[3]

sort

35	25	20	80
a[4]	a[5]	a[6]	a[7]

25	35
a[4]	a[5]

Merge Sort By Picture

12

sort

30	10	15	5	35	25	20	80
a[0]	a[1]	a[2]	a[3]	a[4]	a[5]	a[6]	a[7]

5	10	15	30
a[0]	a[1]	a[2]	a[3]

sort

35	25	20	80
a[4]	a[5]	a[6]	a[7]

25	35
a[4]	a[5]

 sort

20	80
a[6]	a[7]

20	80
a[6]	a[7]

merge

20	80
a[6]	a[7]

Merge Sort By Picture

13

sort

30	10	15	5	35	25	20	80
a[0]	a[1]	a[2]	a[3]	a[4]	a[5]	a[6]	a[7]

5	10	15	30
a[0]	a[1]	a[2]	a[3]

sort

35	25	20	80
a[4]	a[5]	a[6]	a[7]

25	35
a[4]	a[5]

20	80
a[6]	a[7]

Merge Sort By Picture

14

sort

30	10	15	5	35	25	20	80
a[0]	a[1]	a[2]	a[3]	a[4]	a[5]	a[6]	a[7]

5	10	15	30
a[0]	a[1]	a[2]	a[3]

sort

35	25	20	80
a[4]	a[5]	a[6]	a[7]

25	35
a[4]	a[5]

20	80
a[6]	a[7]

merge

20	25	35	80
a[4]	a[5]	a[6]	a[7]

Merge Sort By Picture

15

sort

30	10	15	5	35	25	20	80
a[0]	a[1]	a[2]	a[3]	a[4]	a[5]	a[6]	a[7]

5	10	15	30
a[0]	a[1]	a[2]	a[3]

20	25	35	80
a[4]	a[5]	a[6]	a[7]

Merge Sort By Picture

16

sort	30	10	15	5	35	25	20	80
	a[0]	a[1]	a[2]	a[3]	a[4]	a[5]	a[6]	a[7]

5	10	15	30
a[0]	a[1]	a[2]	a[3]

20	25	35	80
a[4]	a[5]	a[6]	a[7]

merge

5	10	15	20	25	30	35	80
a[0]	a[1]	a[2]	a[3]	a[4]	a[5]	a[6]	a[7]

Merge Sort By Picture

17

5	10	15	20	25	30	35	80
a[0]	a[1]	a[2]	a[3]	a[4]	a[5]	a[6]	a[7]

Merge Sort

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Idea

Break the list into two equal pieces. Sort the left piece; sort the right piece. Use our previous algorithm to merge the two sorted pieces together.

Code

```
1 public static void mergesort(List<Integer> list) {  
2     if (list.size() > 1) {  
3         int mid = list.size() / 2;  
4         List<Integer> left = list.subList(0, mid);  
5         List<Integer> right = list.subList(mid, list.size());  
6  
7         mergesort(left);  
8         mergesort(right);  
9  
10        List<Integer> merged = merge(left, right);  
11        for (int i = 0; i < merged.size(); i++) {  
12            list.set(i, merged.get(i));  
13        }  
14    }  
15 }
```