

# Uninformed Search

## Chapter 3

(Based on slides by Stuart Russell, Subbarao Kambhampati, Dan Weld, Oren Etzioni, Henry Kautz, and other UW-AI faculty)

# Agent's Knowledge Representation

Type	State representation	Focus
Atomic	States are indivisible; No internal structure	Search on atomic states;
Propositional (aka Factored)	States are made of state variables that take values (Propositional or Multi-valued or Continuous)	Search+inference in logical (prop logic) and probabilistic (bayes nets) representations
Relational	States describe the objects in the world and their inter-relations	Search+Inference in predicate logic (or relational prob. Models)
First-order	+functions over objects	Search+Inference in first order logic (or first order probabilistic models)

# Illustration with Vacuum World

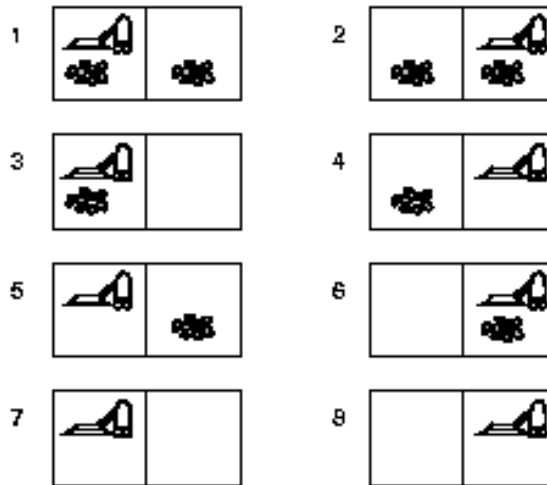
Atomic:

S1, S2.... S8

state is seen as an indivisible snapshot

All Actions are SXS matrices..

If you add a second roomba  
the state space *doubles*



Relational:

World made of objects: Roomba; L-room, R-room, dirt

Relations: In (<robot>, <room>); dirty(<room>)

If you add a second roomba, or more rooms, only the objects increase.

If you want to consider noisiness, you just need to add one other relation

Propositional/Factored:

States made up of 3 state variables

Dirt-in-left-room T/F

Dirt-in-right-room T/F

Roomba-in-room L/R

Each state is an assignment of  
Values to state variables

$2^3$  Different states

Actions can just mention the variables  
they affect

Note that the representation is  
compact (logarithmic in the  
size of the state space)

If you add a second roomba, the  
Representation increases by just one  
More state variable.

If you want to consider “noisiness” of  
rooms, we need *two* variables, one for  
Each room

# Atomic Agent

## Input:

- Set of states
- Operators [and costs]
- Start state
- Goal state [test]

## Output:

- Path: start  $\Rightarrow$  a state satisfying goal test
- [May require shortest path]

# What is Search?

- Search is a class of techniques for systematically finding or constructing solutions to problems.
  - Example technique: generate-and-test.
  - Example problem: Combination lock.
1. Generate a possible solution.
  2. Test the solution.
  3. If solution found THEN done ELSE return to step 1.

# Why is search interesting?

- Many (all?) AI problems can be formulated as search problems!
- Examples:
  - Path planning
  - Games
  - Natural Language Processing
  - Machine learning
  - ...

# Example: The 8-puzzle

7	2	4
5		6
8	3	1

Start State

	1	2
3	4	5
6	7	8

Goal State

- states?
- actions?
- goal test?
- path cost?

# Example: The 8-puzzle

7	2	4
5		6
8	3	1

Start State

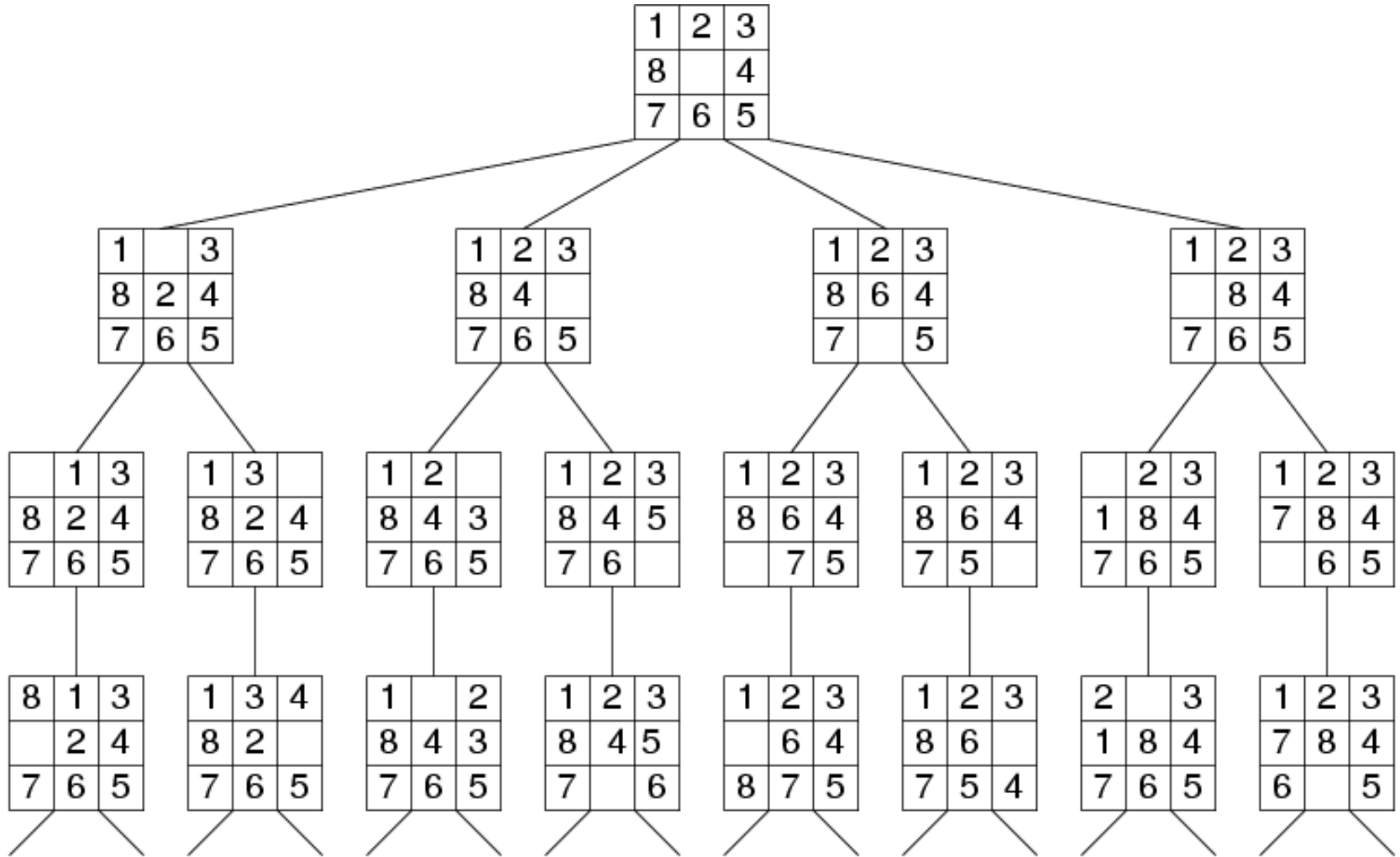
	1	2
3	4	5
6	7	8

Goal State

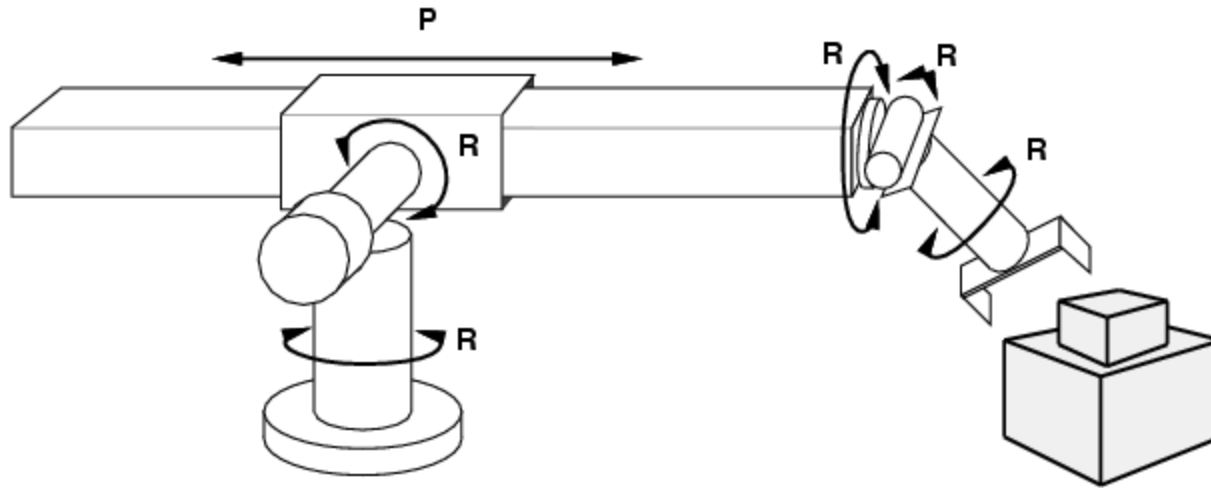
- states? locations of tiles
- actions? move blank left, right, up, down
- goal test? = goal state (given)
- path cost? 1 per move
- 
- [Note: optimal solution of  $n$ -Puzzle family is NP-hard]



# Search Tree Example: Fragment of 8-Puzzle Problem Space



# Example: robotic assembly



- states?: real-valued coordinates of robot joint angles parts of the object to be assembled
- 
- actions?: continuous motions of robot joints
- 
- goal test?: complete assembly
- 
- path cost?: time to execute
-

# Example: Romania

- On holiday in Romania; currently in Arad.
- Flight leaves tomorrow from Bucharest
- 
- **Formulate goal:**
  - be in Bucharest
  -
- **Formulate problem:**
  - **states:** various cities
  - **actions:** drive between cities
  -
- **Find solution:**
  - sequence of cities, e.g., Arad, Sibiu, Fagaras, Bucharest
  -

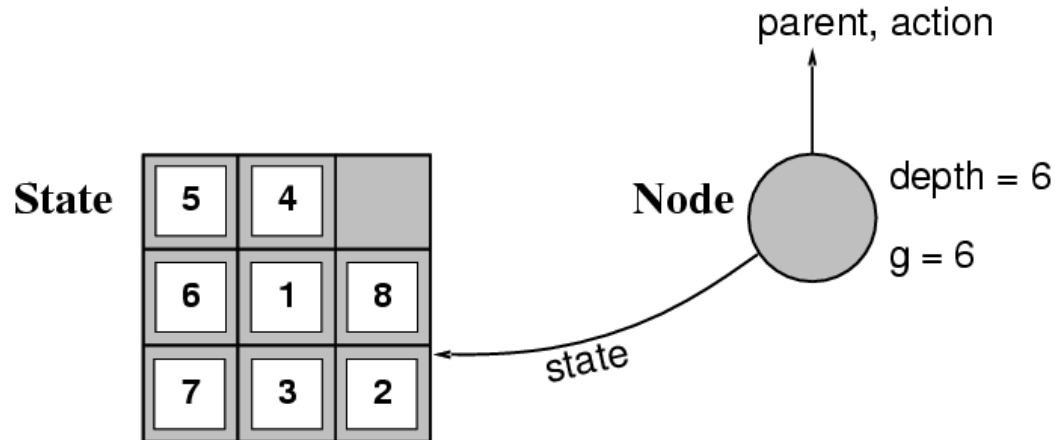
## Example: N Queens

- Input:
  - Set of states
  - Operators [and costs]
  - Start state
  - Goal state (test)
- Output

		Q	
Q			
			Q
	Q		

# Implementation: states vs. nodes

- A **state** is a (representation of) a physical configuration
- A **node** is a data structure constituting part of a search tree includes **state**, **parent node**, **action**, **path cost  $g(x)$** , **depth**



- The `Expand` function creates new nodes, filling in the various fields and using the `SuccessorFn` of the problem to create the corresponding states.
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# Search strategies

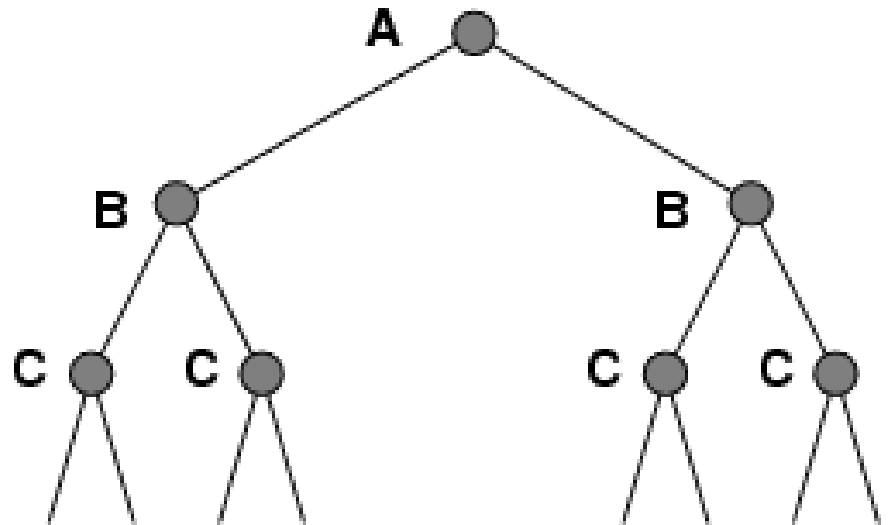
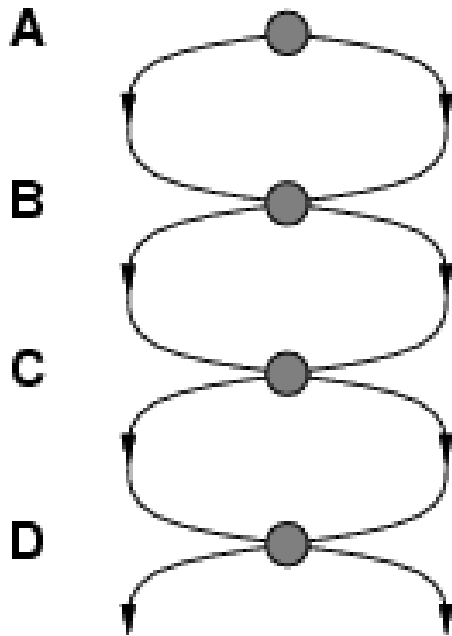
- A search strategy is defined by picking the **order of node expansion**
- Strategies are evaluated along the following dimensions:
  - **completeness**: does it always find a solution if one exists?
  - **time complexity**: number of nodes generated
  - **space complexity**: maximum number of nodes in memory
  - **optimality**: does it always find a least-cost solution?
  - **systematicity**: does it visit each state at most once?
- Time and space complexity are measured in terms of
  - *b*: maximum branching factor of the search tree
  - *d*: depth of the least-cost solution
  - *m*: maximum depth of the state space (may be  $\infty$ )

# Uninformed search strategies

- **Uninformed** search strategies use only the information available in the problem definition
- Breadth-first search
- Depth-first search
- Depth-limited search
- Iterative deepening search

# Repeated states

- Failure to detect repeated states can turn a linear problem into an exponential one!





# Depth First Search

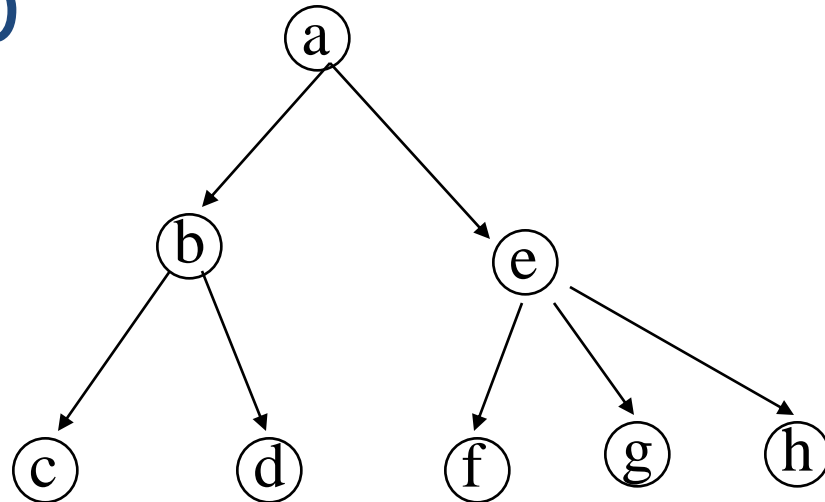
- Maintain stack of nodes to visit
- Evaluation
  - Complete? **No**

– Time Complexity?

$$O(b^m)$$

– Space Complexity?

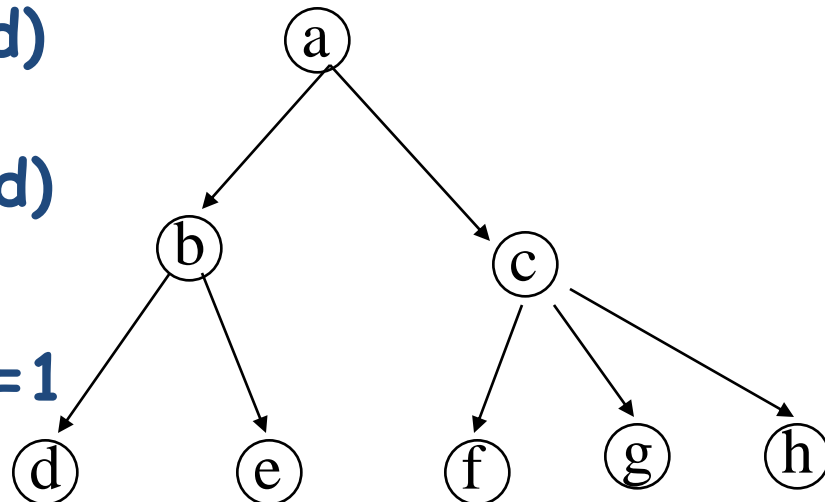
$$O(bm)$$



<http://www.youtube.com/watch?v=dtoFAvtVE4U>

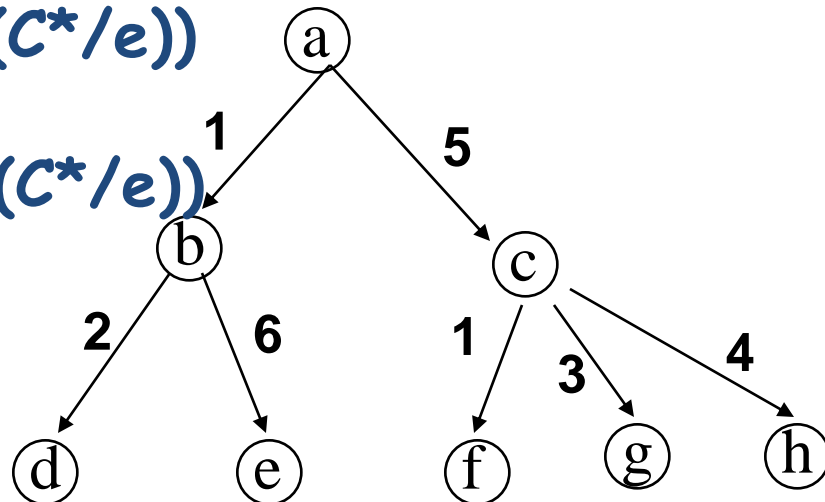
# Breadth First Search: shortest first

- Maintain queue of nodes to visit
- Evaluation
  - Complete? **Yes (b is finite)**
  - Time Complexity?  **$O(b^d)$**
  - Space Complexity?  **$O(b^d)$**
  - Optimal? **Yes, if stepcost=1**



# Uniform Cost Search: cheapest first

- Maintain queue of nodes to visit
- Evaluation
  - Complete? **Yes (b is finite)**
  - Time Complexity?  $O(b^{(C^*/e)})$
  - Space Complexity?  $O(b^{(C^*/e)})$
  - Optimal? **Yes**



<http://www.youtube.com/watch?v=z6lUnb9ktkE>