# Classical Planning Chapter 10

Mausam

(Based on slides of Dan Weld, Marie desJardins)

# **Planning**

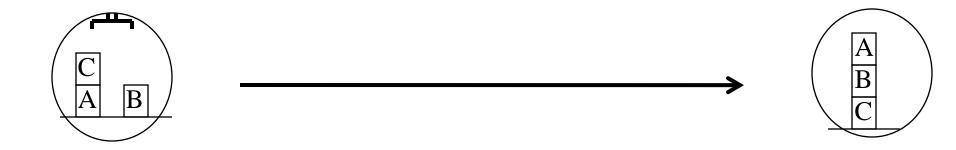
#### Given

- a logical description of the initial situation,
- a logical description of the goal conditions, and
- a logical description of a set of possible actions,

#### find

 a sequence of actions (a plan of actions) that brings us from the initial situation to a situation in which the goal conditions hold.

# Example: BlocksWorld



# Planning Input: State Variables/Propositions

- Types: block --- a, b, c
- (on-table a) (on-table b) (on-table c)
- (clear a) (clear b) (clear c)
- (arm-empty)
- (holding a) (holding b) (holding c)
- (on a b) (on a c) (on b a) (on b c) (on c a) (on c b)

• (on-table?b); clear(?b)

- (arm-empty); holding (?b)
- (on?b1?b2)

No. of state variables =16

No. of states =  $2^{16}$ 

No. of reachable states = ?

## Planning Input: Actions

• pickup a b, pickup a c, ···

• pickup?b1?b2

• place a b, place a c, ···

• place?b1?b2

- pickup-table a, pickup-table b, ···
- pickup-table?b

• place-table a, place-table b, ···

place-table?b

Total: 6 + 6 + 3 + 3 = 18 "ground" actions

**Total: 4 action schemata** 

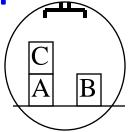
# Planning Input: Actions (contd)

```
• :action pickup?b1?b2
  :precondition
     (on?b1?b2)
     (clear?b1)
     (arm-empty)
  :effect
     (holding?b1)
     (not (on ?b1 ?b2))
     (clear?b2)
     (not (arm-empty))
```

```
    action pickup-table?b

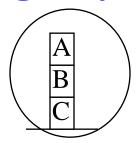
  :precondition
     (on-table?b)
     (clear?b)
     (arm-empty)
  :effect
      (holding?b)
     (not (on-table ?b))
     (not (arm-empty))
```

## Planning Input: Initial State



- (on-table a) (on-table b)
- (arm-empty)
- (clear c) (clear b)
- (on c a)
- All other propositions false
  - not mentioned → false

# Planning Input: Goal



• (on-table c) AND (on b c) AND (on a b)

• Is this a state?

In planning a goal is a set of states

# Planning Input Representation

- Description of initial state of world
  - Set of propositions

- Description of goal: i.e. set of worlds
  - E.g., Logical conjunction
  - Any world satisfying conjunction is a goal

Description of available actions

# Planning vs. Problem-Solving

#### Basic difference: Explicit, logic-based representation

- States/Situations: descriptions of the world by logical formulae
  - → agent can explicitly reason about and communicate with the world.
- Goal conditions as logical formulae vs. goal test (black box)
   → agent can reflect on its goals.
- Operators/Actions: Axioms or transformation on formulae in a logical form
  - → agent can gain information about the effects of actions by inspecting the operators.

# **Classical Planning**

- Simplifying assumptions
  - Atomic time
  - Agent is omniscient (no sensing necessary).
  - Agent is sole cause of change
  - Actions have deterministic effects
- STRIPS representation
  - World = set of true propositions (conjunction)
  - Actions:
    - Precondition: (conjunction of positive literals, no functions)
    - Effects (conjunction of literals, no functions)
  - Goal = conjunction of positive literals
  - Is Blocks World in STRIPS?
  - Goals = conjunctions (Rich ^ Famous)

## Planning as Search

#### Forward Search in ? Space

- World State Space
- start from start state; look for a state with goal property
  - dfs/bfs
  - A\*

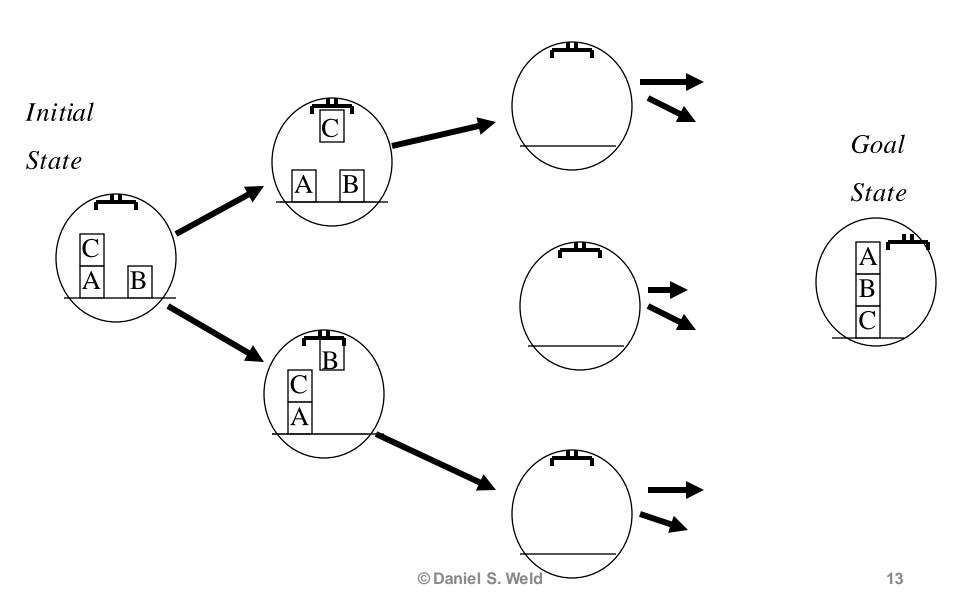
#### Backward Search in ? Space

- Subgoal Space
- start from goal conjunction; look for subgoal that holds in initial state
  - dfs/bfs/A\*

#### Local Search in ? Space

Plan Space

## Forward World-Space Search



#### Forward State-Space Search

 Initial state: set of positive ground literals (CWA: literals not appearing are false)

#### Actions:

- applicable if preconditions satisfied
- add positive effect literals
- remove negative effect literals
- Goal test: checks whether state satisfies goal
- Step cost: typically 1

#### Heuristics for State-Space Search

Count number of false goal propositions in current state

Admissible?

NO

- Subgoal independence assumption:
  - Cost of solving conjunction is sum of cost of solving each subgoal independently
  - Optimistic: ignores negative interactions
  - Pessimistic: ignores redundancy
  - Admissible? No
  - Can you make this admissible?

# Heuristics for State Space Search (contd)

 Delete all preconditions from actions, solve easy relaxed problem, use length

Admissible?

YES

 Delete negative effects from actions, solve easier relaxed problem, use length

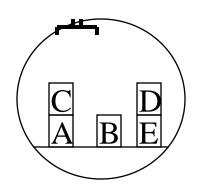
Admissible?

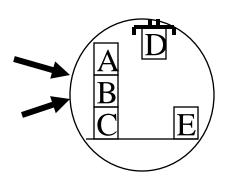
YES (if Goal has only positive literals, true in STRIPS)

#### **Backward Subgoal-Space Search**

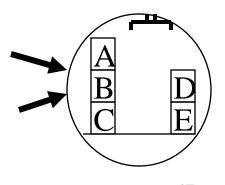
- Regression planning
- Problem: Need to find predecessors of state
- Problem: Many possible goal states are equally acceptable.
- From which one does one search?

Initial State is completely defined



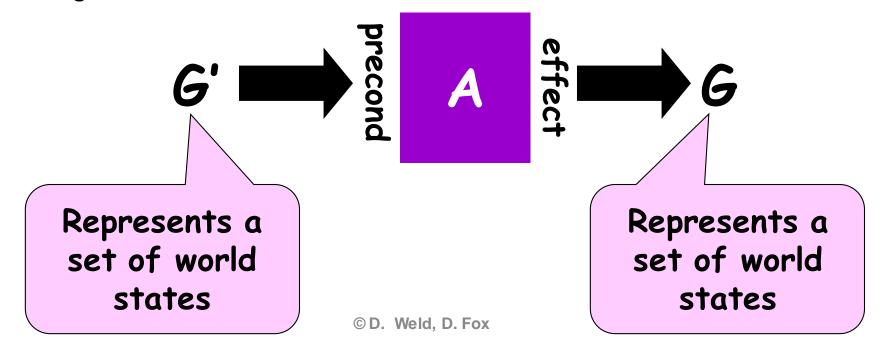




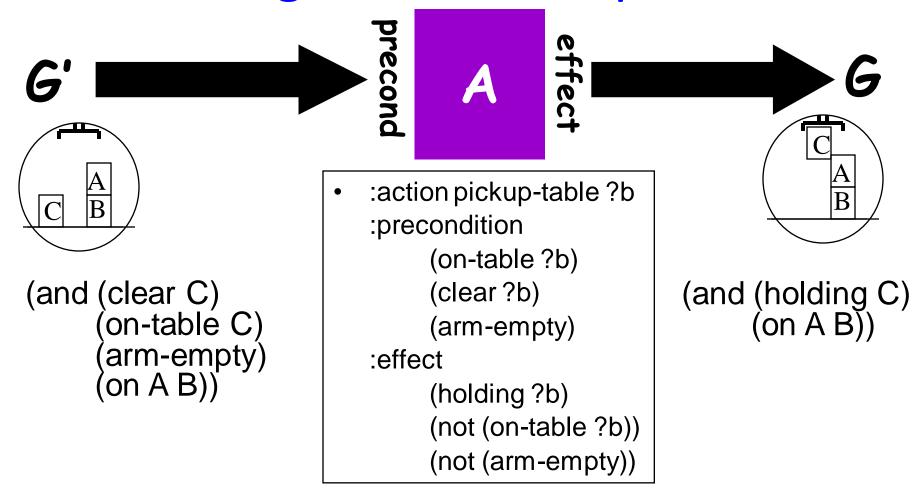


## Regression

- Let G be a KR sentence (e.g. in logic)
- Relevance: needs to achieve one subgoal
- Consistency: does not undo any other subgoal
- Regressing a goal, G, thru an action, A yields the weakest precondition G'
  - Such that: if G' is true before A is executed
  - G is guaranteed to be true afterwards



## Regression Example



Remove positive effects Add preconditions for A

# **Complexity of Planning**

- Size of Search Space
  - Forward: size of world state space
  - Backward: size of subsets of partial state space!

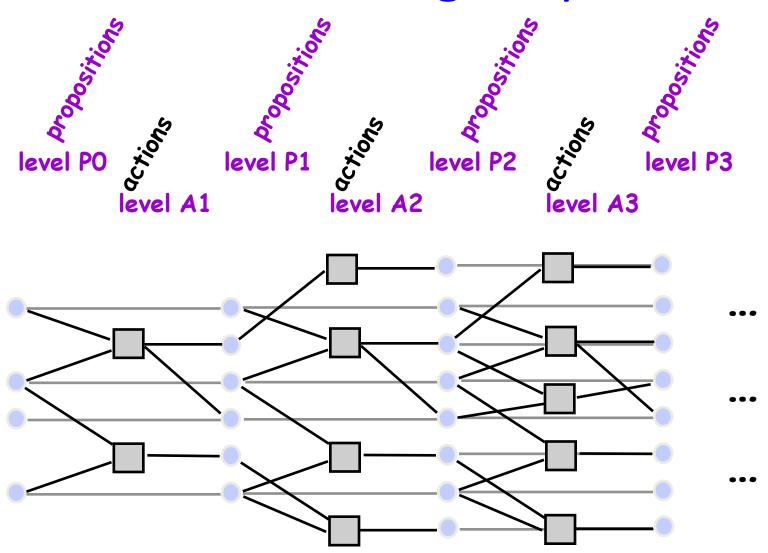
- Size of World state space
  - exponential in problem representation

- What to do?
  - Informative heuristic that can be computed in polynomial time!

# Planning Graph: Basic idea

- Construct a planning graph: encodes constraints on possible plans
- Use this planning graph to compute an informative heuristic (Forward A\*)
- Planning graph can be built for each problem in polynomial time

# The Planning Graph



Note: a few noops missing wifer clarity

# **Graph Expansion**

#### **Proposition level 0**

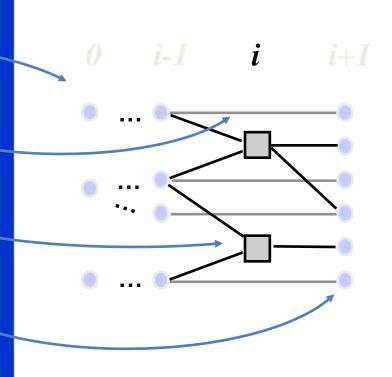
initial conditions

#### **Action level i**

no-op for each proposition at level i-1 action for each operator instance whose preconditions exist at level i-1

#### **Proposition level i**

effects of each no-op and action at level i



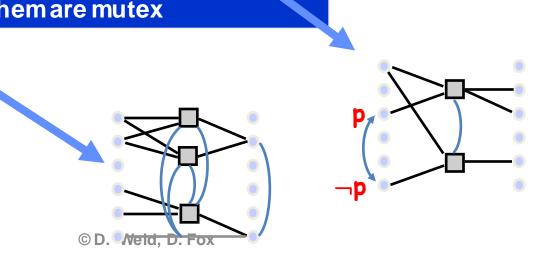
#### Mutual Exclusion

#### Two actions are mutex if

- one clobbers the other's effects or preconditions
- they have mutex preconditions

Two proposition are mutex if

- one is the negation of the other
- •all ways of achieving them are mutex



#### **Dinner Date**

<u>Initial Conditions</u>: (:and (cleanHands) (quiet))

Goal: (:and (noGarbage) (dinner) (present))

#### Actions:

:effect (present))

# Planning Graph

noGarb

carry

cleanH cleanH

dolly

quiet quiet

cook

dinner

wrap

present

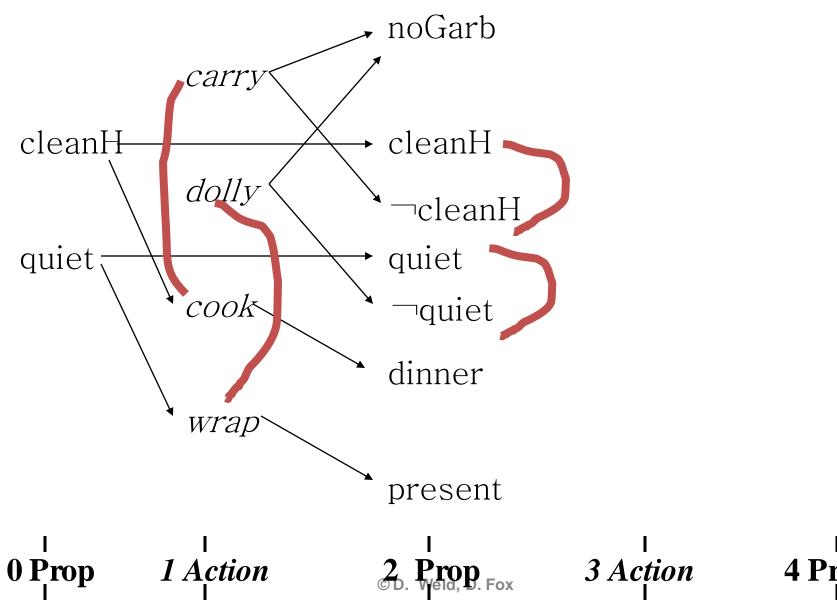
0 Prop 1 Action

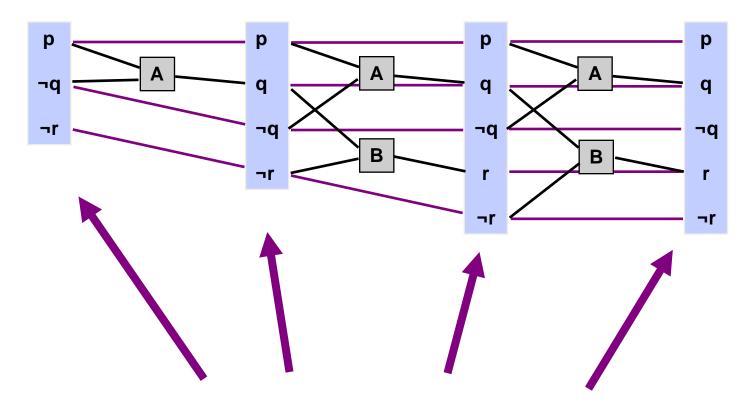
2. Prop. Fox

3 Action

4 Prop

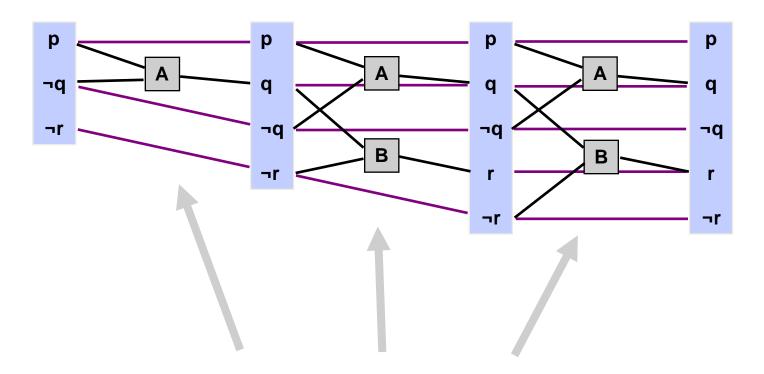
# Are there any exclusions?



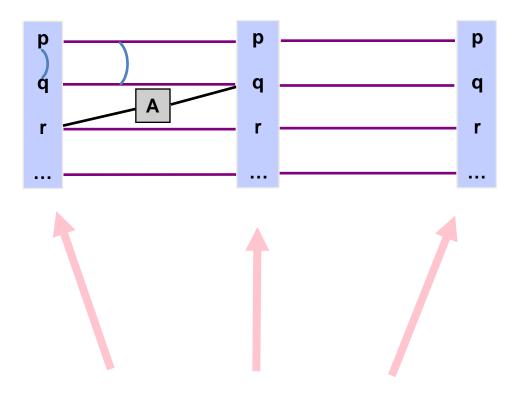


#### **Propositions monotonically increase**

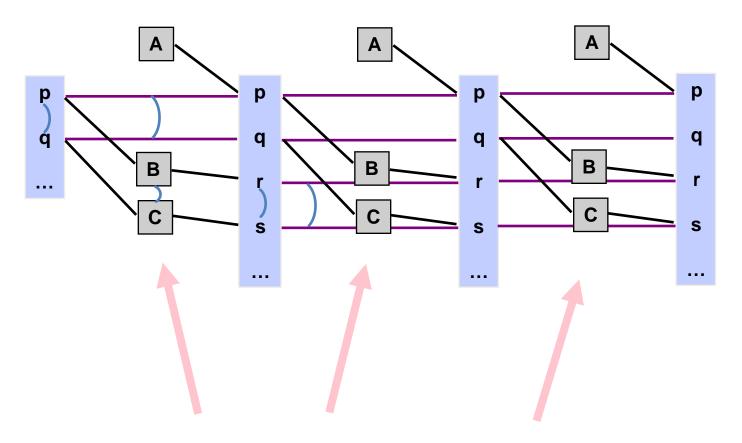
(always carried forward by no-ops)



**Actions monotonically increase** 



Proposition mutex relationships monotonically decrease



Action mutex relationships monotonically decrease

Planning Graph 'levels off'.

- After some time k all levels are identical
- Because it's a finite space, the set of literals never decreases and mutexes don't reappear.

# **Properties of Planning Graph**

- If goal is absent from last level
  - Goal cannot be achieved!
- If there exists a path to goal goal is present in the last level
- If goal is present in last level there may not exist any path still

#### Heuristics based on Planning Graph

- Construct planning graph starting from s
- h(s) = level at which goal appears non-mutex
  - Admissible?
  - YES

- Relaxed Planning Graph Heuristic
  - Remove negative preconditions build plan. graph
  - Use heuristic as above
  - Admissible? YES
  - More informative? NO
  - Speed: FASTER

#### FF

Topmost classical planner until 2009

- State space local search
  - Guided by relaxed planning graph
  - Full bfs to escape plateaus enforced hill climbing
  - A few other bells and whistles...

# SATPlan: Planning as SAT

- Formulate the planning problem as a CSP
- Assume that the plan has k actions
- Create a binary variable for each possible action a:
  - Action(a,i) (TRUE if action a is used at step i)
- Create variables for each proposition that can hold at different points in time:
  - Proposition(p,i) (TRUE if proposition p holds at step i)

#### **Constraints**

- XOR: Only one action can be executed at each time step
- At least one action must be executed at each time step
- Constraints describing effects of actions
  - Action(a,i)  $\rightarrow$  prec(a,i-1); Action(a,i)  $\rightarrow$  eff(a,i)
- Maintain action: if an action does not change a prop p, then maintain action for proposition p is true
  - Action(maint\_p,i) → Action(a1,i) v Action(a2,i)... [for all a<sub>i</sub> that don't effect p]
- A proposition is true at step i only if some action (possibly a maintain action) made it true
- Constraints for initial state and goal state

# **Popular Application**



# **Planning Summary**

- Problem solving algorithms that operate on explicit propositional representations of states and actions.
- Make use of specific heuristics.
- STRIPS: restrictive propositional language
- State-space search: forward (progression) / backward (regression) search
- Local search FF; using compilation into SAT

 Partial order planners search space of plans from goal to start, adding actions to achieve goals (did not cover)