Aliasing

Ray tracing is a form of sampling and can suffer from annoying visual artifacts...

Consider a continuous function $f(x)$. Now sample it at intervals $\Delta$ to give $f[i] = \text{quantize}(f[i\Delta])$.

Q: How well does $f[i]$ approximate $f(x)$?

Consider sampling a sinusoid:

In this case, the sinusoid is reasonably well approximated by the samples.

Aliasing (con’t)

Now consider sampling a higher frequency sinusoid

We get the exact same samples, so we seem to be approximating the first lower frequency sinusoid again.

We say that, after sampling the higher frequency sinusoid has taken on a new "alias", i.e., changed its identity to be a lower frequency sinusoid.
Aliasing in rendering

One of the most common rendering artifacts is the "jaggies". Consider rendering a white polygon against a black background:

We would instead like to get a smoother transition:

Anti-aliasing

Q. How do we avoid aliasing artifacts?
1. Sampling: *come - buy better display*
2. Pre-filtering: *(analytically) very difficult*
3. Combination: increase sampling rate via each pixel + average sample via each pixel

Example - polygon:

Anti-aliasing in a ray tracer

We would like to compute the average intensity in the neighborhood of each pixel.

When casting one ray per pixel, we are likely to have aliasing artifacts.

To improve matters, we can cast more than one ray per pixel and average the result.

A.k.a. super-sampling and averaging down.
Temporal aliasing

Suppose we are rendering a "clock" with a fast turning hand:

What happens if we sample too infrequently? (This is sometimes called the "wagon wheel" effect.)

Another more common scenario is something moving quickly across the frame, e.g., a fast-moving particle:

Trajectory

Frames

How might we address these temporal aliasing effects?... 3, 5, 8, 15, 20.

Speeding it up

Brute force ray tracing is really slow!

Consider rendering a single image with:

- $m \times n$ pixels
- $k \times k$ supersampling
- $n$ primitives
- average ray path length of $d$
- $\ell$ shadow rays per intersection
- 0.1 or 2 rays cost recursively per intersection

Asymptotic complexity $= n^{2 + k + \ell + (k \times \ell)}$

For $n=1000$, $k = 5, n = 100,000, \ell = 10, d=8...$ very expensive!

In practice, some acceleration technique is almost always used.

We've already looked at reducing $d$ with adaptive ray termination.

Now we look at reducing the effect of the $k$ and $n$
terms...

Antialiasing by adaptive sampling

Casting many rays per pixel can be unnecessarily costly.

For example, if there are no rapid changes in intensity at the pixel, maybe only a few samples are needed.

Solution: adaptive sampling.

Q: When do we decide to cast more rays in a particular area?

Faster ray-polyhedron intersection

Let's say you were intersecting a ray with a polyhedron:

Straightforward method

- Intersect the ray with each triangle
- Return the intersection with the smallest $t$-value.

Q: How might you speed this up?

Bounding volume
Hierarchical bounding volumes

We can generalize the idea of bounding volume acceleration with **hierarchical bounding volumes**.

...then intersect with children...

...until you reach the leaf nodes - the primitives.

Key: build balanced trees with tight bounding volumes.

Uniform spatial subdivision

Another approach is **uniform spatial subdivision**.

- Uniform subdivision in 2D
- Uniform subdivision in 3D

**Ideas**
- Partition space into cells (voxels)
- Associate each primitive with the cells it overlaps
- Trace ray through voxel array using fast incremental arithmetic to step from cell to cell

Non-uniform spatial subdivision

Still another approach is **non-uniform spatial subdivision**.

Quadtrees in 2D

Octrees in 3D

Other variants include k-d trees and BSP trees.

Various combinations of these ray intersection techniques are also possible.

Summary

What to take home from this lecture:
- The meanings of all the boldfaced terms.
- An intuition for what aliasing is.
- How to reduce aliasing artifacts in a ray tracer.
- An intuition for how ray tracers can be accelerated.