CSE524 Parallel Algorithms

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30 March 2010

Computation CSE524 Parallel Algorithms

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Programming Computation CSE524 Parallel Algorithms

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Course Logistics

- ☐ Teaching Assistants: Matt Kehrt and Adrienne Wang
- ☐ Text: Lin&Snyder, *Principles of Parallel Programming*, Addison Wesley, 2008
 - There will also be occasional readings
- ☐ Class web page is headquarters for all data
- ☐ Take lecture notes -- the slides will be online sometime **after** the lecture

Informal class; ask questions immediately

Expectations

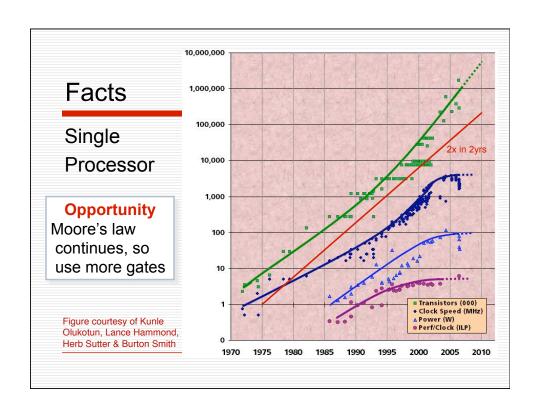
- ☐ Readings: We will cover much of the book; please read the text before class
- ☐ Lectures will layout certain details, arguments ... discussion is encouraged
- Most weeks there will be graded homework to be submitted electronically PRIOR to class
- ☐ Am assuming most students have access to a multi-core or other parallel machine
- ☐ Grading: class contributions, homework assignments; no final is contemplated at the moment

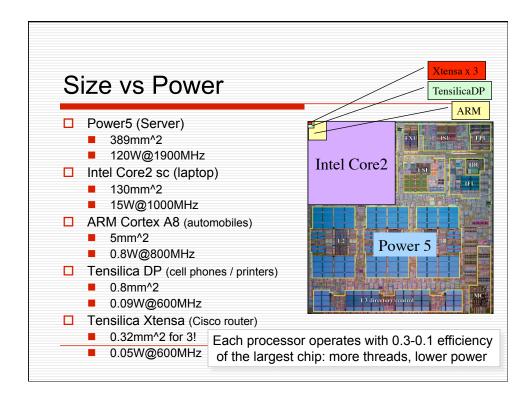
Part I: Introduction

Goal: Set the parameters for studying parallelism

Why Study Parallelism?

- ☐ After all, for most of our daily computer uses, sequential processing is plenty fast
 - It is a fundamental departure from the "normal" computer model, therefore it is inherently cool
 - The extra power from parallel computers is enabling in science, engineering, business, ...
 - Multicore chips present a new opportunity
 - Deep intellectual challenges for CS -- models, programming languages, algorithms, HW, ...





Topic Overview

- ☐ Goal: To give a good idea of parallel computation
 - Concepts -- looking at problems with "parallel eyes"
 - Algorithms -- different resources; different goals
 - Languages -- reduce control flow; increase independence; new abstractions
 - Hardware -- the challenge is communication, not instruction execution
 - Programming -- describe the computation without saying it sequentially
 - Practical wisdom about using parallelism

Everyday Parallelism

- ☐ Juggling -- event-based computation
- ☐ House construction -- parallel tasks, wiring and plumbing performed at once
- ☐ Assembly line manufacture -- pipelining, many instances in process at once
- ☐ Call center -- independent tasks executed simultaneously

How do we describe execution of tasks?

Parallel vs Distributed Computing

☐ Comparisons are often matters of degree

Characteristic	Parallel	Distributed
Overall Goal	Speed	Convenience
Interactions	Frequent	Infrequent
Granularity	Fine	Coarse
Reliable	Assumed	Not Assumed

Parallel vs Concurrent

- □ In OS and DB communities execution of multiple threads is logically simultaneous
- □ In Arch and HPC communities execution of multiple threads is physically simultaneous
- ☐ The issues are often the same, say with respect to races
- □ Parallelism can achieve states that are impossible with concurrent execution because two events happen at once

Consider A Simple Task ...

- ☐ Adding a sequence of numbers A[0],...,A[n-1]
- ☐ Standard way to express it

```
sum = 0;
for (i=0; i<n; i++) {
    sum += A[i];
}
```

- ☐ Semantics require: (...((sum+A[0])+A[1])+...)+A[n-1]
 - That is, sequential
- ☐ Can it be executed in parallel?

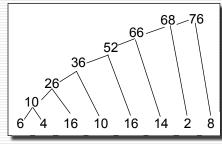
Parallel Summation

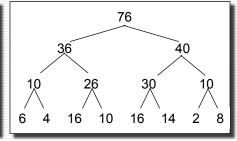
- ☐ To sum a sequence in parallel
 - add pairs of values producing 1st level results,
 - add pairs of 1st level results producing 2nd level results,
 - sum pairs of 2nd level results ...
- ☐ That is,

$$(...((A[0]+A[1]) + (A[2]+A[3])) + ... + (A[n-2]+A[n-1]))...)$$

Express the Two Formulations

☐ Graphic representation makes difference clear





Same number of operations; different order

The Dream ...

- ☐ Since 70s (Illiac IV days) the dream has been to compile sequential programs into parallel object code
 - Three decades of continual, well-funded research by smart people implies it's hopeless
 - ☐ For a tight loop summing numbers, its doable
 - ☐ For other computations it has proved **extremely** challenging to generate parallel code, even with pragmas or other assistance from programmers

What's the Problem?

- ☐ It's not likely a compiler will produce parallel code from a C specification any time soon...
- ☐ Fact: For most computations, a "best" sequential solution (practically, not theoretically) and a "best" parallel solution are usually fundamentally different ...
 - Different solution paradigms imply computations are not "simply" related
 - Compiler transformations generally preserve the solution paradigm

Therefore... the programmer must discover the || solution

A Related Computation

☐ Consider computing the prefix sums

```
for (i=1; i<n; i++) {
    A[i] += A[i-1];
}
```

A[i] is the sum of the first i + 1 elements

- ☐ Semantics ...
 - A[0] is unchanged
 - A[1] = A[1] + A[0]
 - A[2] = A[2] + (A[1] + A[0])

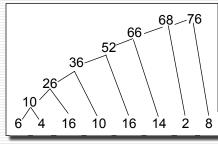
...

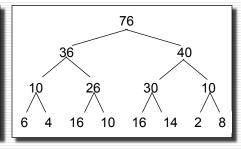
■ A[n-1] = A[n-1] + (A[n-2] + (... (A[1] + A[0]) ...)

What advantage can ||ism give?

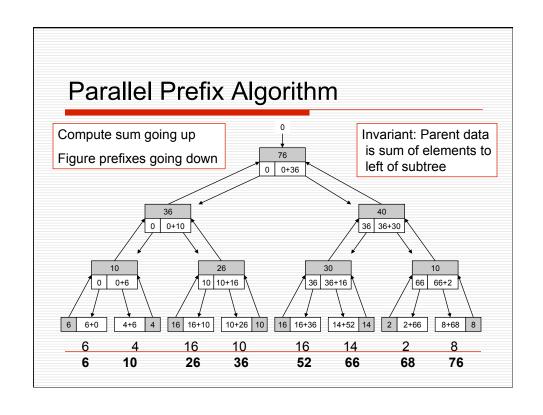
Comparison of Paradigms

☐ The sequential solution computes the prefixes ... the parallel solution computes only the last





☐ Or does it?



Fundamental Tool of || Pgmming

☐ Original research on parallel prefix algorithm published by

R. E. Ladner and M. J. Fischer Parallel Prefix Computation Journal of the ACM 27(4):831-838, 1980

The Ladner-Fischer algorithm requires *2log n* time, twice as much as simple tournament global sum, not linear time

Applies to a wide class of operations

Parallel Compared to Sequential Programming

- ☐ Has different costs, different advantages
- ☐ Requires different, unfamiliar algorithms
- Must use different abstractions
- More complex to understand a program's behavior
- More difficult to control the interactions of the program's components
- Knowledge/tools/understanding more primitive

Consider a Simple Problem

- ☐ Count the 3s in array[] of length values
- Definitional solution ...
 - Sequential program

```
count = 0;

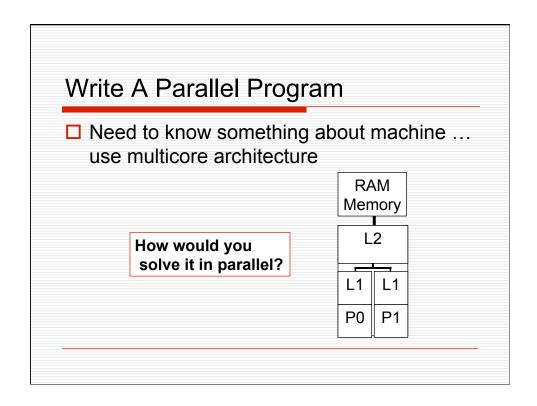
for (i=0; i<length; i++)

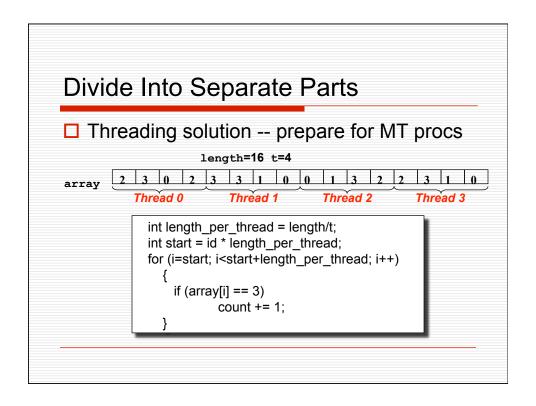
{

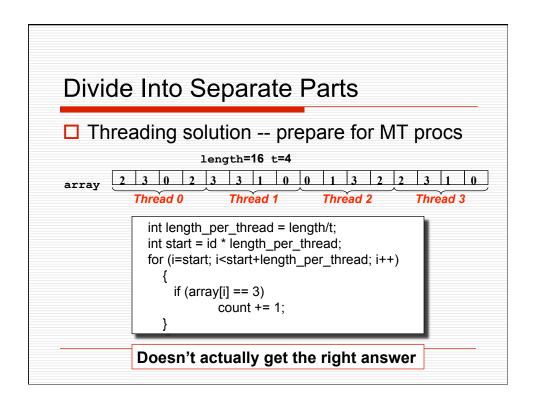
   if (array[i] == 3)

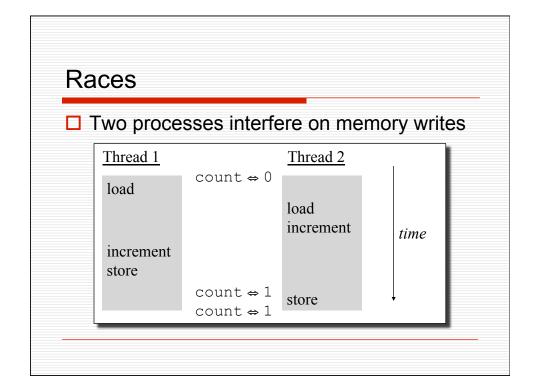
      count += 1;

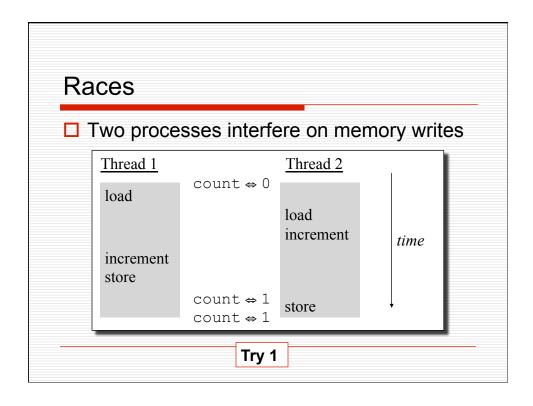
}
```





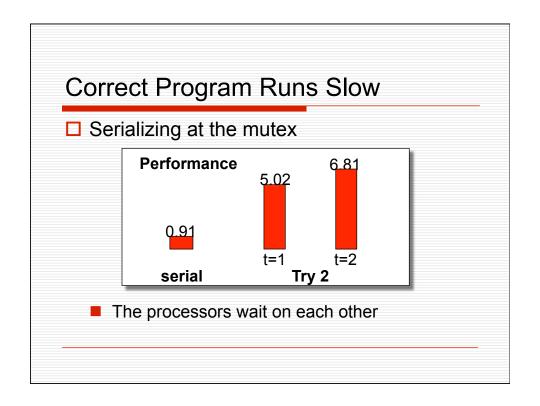






Protect Memory References Protect Memory References mutex m; for (i=start; i<start+length_per_thread; i++) { if (array[i] == 3) { mutex_lock(m); count += 1; mutex_unlock(m); } }

Protect Memory References Protect Memory References mutex m; for (i=start; i<start+length_per_thread; i++) { if (array[i] == 3) { mutex_lock(m); count += 1; mutex_unlock(m); } } Try 2



Closer Look: Motion of count, m Lock Reference and Contention mutex m; for (i=start; i<start+length_per_thread; i++) { if (array[i] == 3) { mutex_lock(m); count += 1; mutex_unlock(m); } }

Accumulate Into Private Count

☐ Each processor adds into its own memory; combine at the end

```
for (i=start; i<start+length_per_thread; i++)
    {
      if (array[i] == 3)
        {
          private_count[t] += 1;
      }
    }
mutex_lock(m);
count += private_count[t];
mutex_unlock(m);</pre>
```

Accumulate Into Private Count

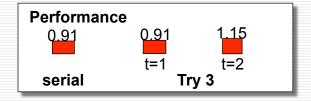
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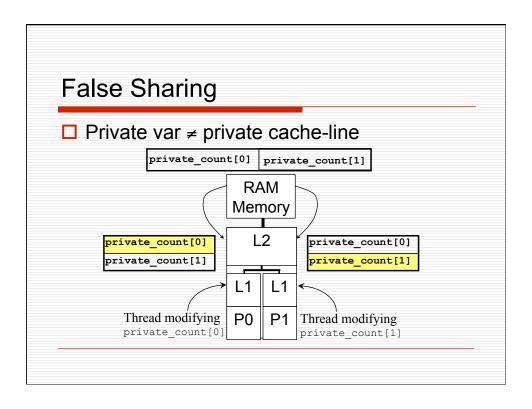
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      count += private_count[t];
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```

Try 3

Keeping Up, But Not Gaining

☐ Sequential and 1 processor match, but it's a loss with 2 processors



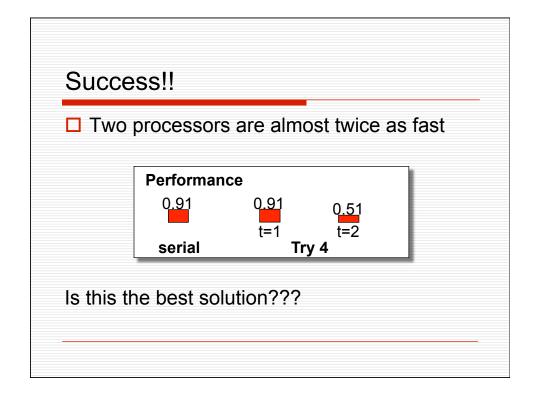


Force Into Different Lines

☐ Padding the private variables forces them into separate cache lines and removes false sharing

```
struct padded_int
{ int value;
char padding[128];
} private_count[MaxThreads];
```

Force Into Different Lines Padding the private variables forces them into separate cache lines and removes false sharing struct padded_int { int value; char padding[128]; } private_count[MaxThreads]; Try 4



Count 3s Summary

- ☐ Recapping the experience of writing the program, we
 - Wrote the obvious "break into blocks" program
 - We needed to protect the count variable
 - We got the right answer, but the program was slower ... lock congestion
 - Privatized memory and 1-process was fast enough, 2- processes slow ... false sharing
 - Separated private variables to own cache line

Finally, success

Break

□ During break think about how to generalize the "sum n-integers" computation for n>8, and possibly, more processors

Variations

- What happens when more processors are available?
 - 4 processors
 - 8 processors
 - 256 processors
 - 32,768 processors

Our Goals In Parallel Programming

- ☐ Goal: Scalable programs with performance and portability
 - Scalable: More processors can be "usefully" added to solve the problem faster
 - Performance: Programs run as fast as those produced by experienced parallel programmers for the specific machine
 - Portability: The solutions run well on all parallel platforms

Program A Parallel Sum

- ☐ Return to problem of writing a parallel sum
- □ Sketch solution in class when n > P = 8
- ☐ Use a logical binary tree?

Program A Parallel Sum

- ☐ Return to problem of writing a parallel sum
- \square Sketch solution in class when n > P = 8
- ☐ Assume communication time = 30 ticks
- \Box *n* = 1024
- □ compute performance

Program A Parallel Sum

- ☐ Return to problem of writing a parallel sum
- \square Sketch solution in class when n > P = 8
- ☐ and communication time = 30 ticks
- \square *n* = 1024
- compute performance
- Now scale to 64 processors

Program A Parallel Sum

- ☐ Return to problem of writing a parallel sum
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- □ and communication time = 30 ticks
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- □ compute performance
- □ Now scale to 64 processors

This analysis will become standard, intuitive

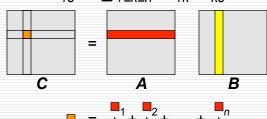
Matrix Product: || Poster Algorithm

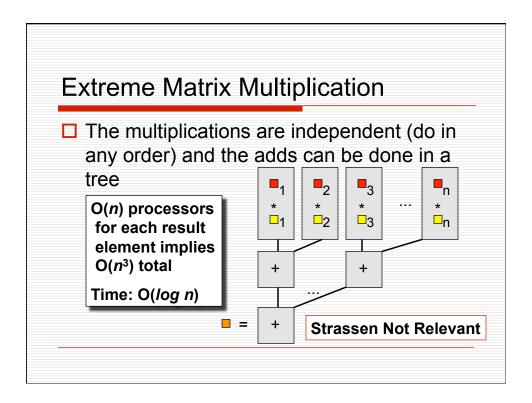
- ☐ Matrix multiplication is most studied parallel algorithm (analogous to sequential sorting)
- Many solutions known
 - Illustrate a variety of complications
 - Demonstrate great solutions
- ☐ Our goal: explore variety of issues
 - Amount of concurrency
 - Data placement
 - Granularity

Exceptional by requiring $O(n^3)$ ops on $O(n^2)$ data

Recall the computation...

☐ Matrix multiplication of (square n x n) matrices \boldsymbol{A} and \boldsymbol{B} producing n x n result \boldsymbol{C} where $\boldsymbol{C}_{rs} = \sum_{1 \le k \le n} \boldsymbol{A}_{rk}^* \boldsymbol{B}_{ks}$





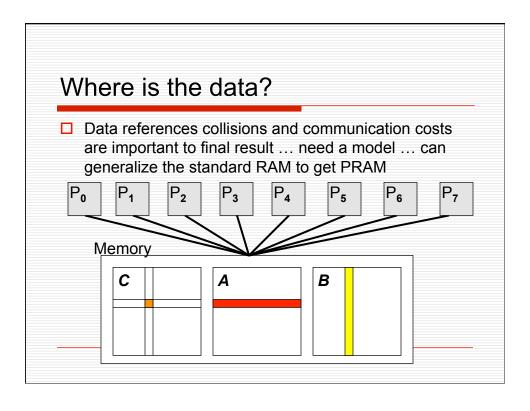
O(log n) MM in the real world ...

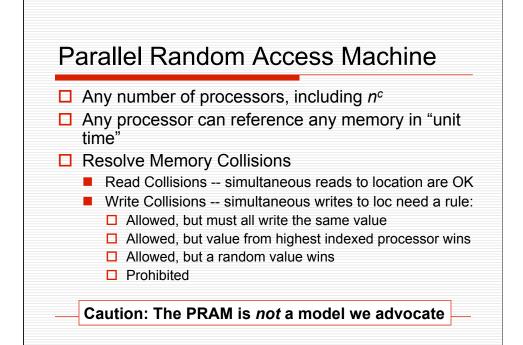
Good properties

- Extremely parallel ... shows limit of concurrency
- Very fast -- log₂ n is a good bound ... faster?

Bad properties

- Ignores memory structure and reference collisions
- Ignores data motion and communication costs
- Under-uses processors -- half of the processors do only 1 operation





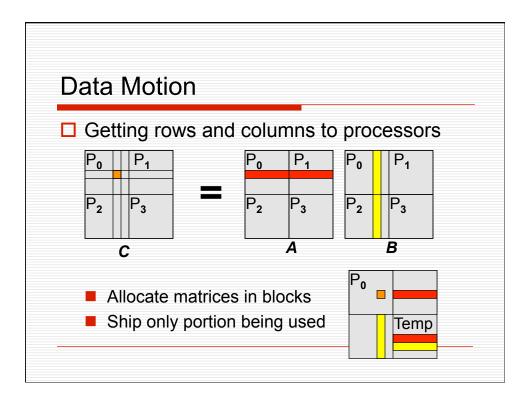
PRAM says O(log n) MM is good

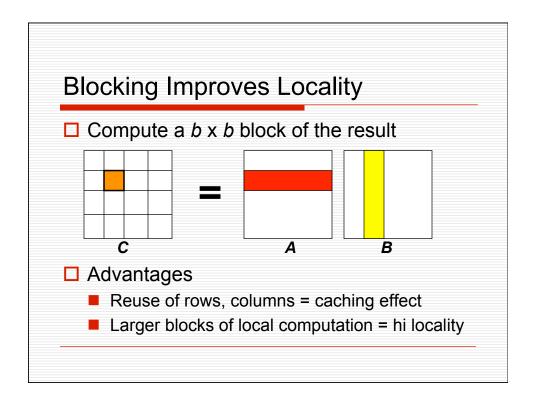
- \square PRAM allows any # processors => O(n^3) OK
- ☐ A and B matrices are read simultaneously, but that's OK
- □ **C** is written simultaneously, but no location is written by more than 1 processor => OK

PRAM model implies O(log n) algorithm is best ... but in real world, we suspect not

We return to this point later

Where else could data be? □ Local memories of separate processors ... $P_{\mathbf{0}}$ P_1 P_2 P_3 Mem Mem Mem Mem Mem Mem Mem Mem Point-to-point Network ☐ Each processor could compute block of **C** Avoid keeping multiple copies of A and B Architecture common for servers





Caching in Parallel Computers

- ☐ Blocking = caching ... why not automatic?
 - Blocking improves locality, but it is generally a manual optimization in sequential computation
 - Caching exploits two forms of locality
 - ☐ Temporal locality -- refs clustered in time
 - ☐ Spatial locality -- refs clustered by address
- ☐ When multiple threads touch the data, global reference sequence may not exhibit clustering features typical of one thread -- thrashing

Sweeter Blocking It's possible to do even better blocking ... rrows { C A B Completely use the cached values before reloading

Best MM Algorithm?

- ☐ We haven't decided on a good MM solution
- □ A variety of factors have emerged
 - A processor's connection to memory, unknown
 - Number of processors available, unknown
 - Locality--always important in computing--
 - ☐ Using caching is complicated by multiple threads
 - ☐ Contrary to high levels of parallelism
- ☐ Conclusion: Need a better understanding of the constraints of parallelism

Next week, architectural details + model of ||ism

Assignment for Next Time

- ☐ Reproduce the parallel prefix tree labeling to compute the bit-wise & scan
- ☐ Try the "count 3s" computation on your multi-core computer
 - Implementation Discussion Board ... please contribute – success, failure, kibitzing, ...
 - https://catalysttools.washington.edu/gopost/ board/snyder/16265/