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Outline for the Evening

- DNA
- Approximate String Matching
- Approximate String Searching
- Dynamic Progamming
- Longest Common Subsequence
- DNA reconstruction
- Contiguous Ordering and PQ-trees

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Applications of Approximate Matching

- DNA string alignment.
 - Given two similar DNA sequences find the best way to align them to the same length.
- DNA database searching.
- Find DNA sequences that are similar to the query.
- Approximate text matching for searching.
- agrep in unix
- Spell checking
 - Find the words that most closely match the misspelled word.

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- Assume S has length m and T has length n.
- For all i and j, 0 ≤ i ≤ m and 0 ≤ j ≤ n, we find the maximum score for the sequences S[1..i] and T[1..j].
- The "dynamic program" fills in a (m+1)x(n+1) matrix M in increasing order of i and j with these maximum values.
- Once the dynamic program has completed we can recover the optimal string S' and T' from the matrix M.























		0	1	2	3	4	5	б	7	
			A	G	A	Т	С	G	Т	
0		0	-1	-2	-3	-4	-5	-6	-7	
1	А	-1	2	1	0	-1	-2	-3	-4	
2	G	-2	1	4	3	2	1	0	-1	
3	С	-3	0	3	3	2	4	3	2	
4	Α	-4	-1	2	5	4	3	3	2	
5	Т	-5	-2	1	4	7	6	5	5	
б	G	-6	-3	0	3	6	6	8 •	-7	



































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LCS Recurrence

$$\label{eq:ci_constraint} c[i,j] = \begin{cases} c[i-1,j-1]+1 & \text{if } x[i]=y[j] \\ max(c[i,j-1],c[i-1,j]) & \text{otherwise} \end{cases}$$

Proof: When calculating c[i,j], there are two cases to consider:

 First case: x[i]=y[j]: one more symbol in strings X and Y matches, so the length of LCS X_i and Y_j equals to the length of LCS of smaller strings X_{i-1} and Y_{i-1}, plus 1.

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PQ Tree Notes

- In algorithmic design only a linear number of nodes are ever processed.
- Designing the data structures to make the linear time processing a reality is very tricky.
- PQ trees solve the idealized DNA ordering problem.
- In reality, because of errors, the DNA ordering problem is NP-hard and other techniques are used.

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