The language used in Problem 1 is similar to the extended lambda-calculi considered in class and Homework 3. The key addition is *access modifiers* on record fields; see point 6.

1. Variables, function application, integers, addition, booleans, and conditionals are just like in Homework 3. Note `Iszero` should be used only on integers. (Type-checking conditionals in a language with subtyping is interesting; see the problem description and the challenge problems.)

2. Lambdas are like in class except we simplify type-checking by requiring a type annotation that is the type of the argument.

3. Closures use an `env ref` instead of an `env` just to make `Letrec` easier to interpret. You do not need to understand this for the homework, but look at the `Letrec` case of `interp` if curious.

4. `Letrec(t1,f,x,t2,e)` describes a recursive function named `f` with body `e`, argument name `x`, return type `t1` and argument type `t2`. (So the body assumes `f` is a function from `t2` to `t1`.)

5. A record is a collection of mutable fields. Strings are field names; the type-checker ensures they are unique. A `RecordE` appears in source programs and is not a value (its fields must be evaluated). A `RecordV` is a value (and all its fields are references to values). The `Get` operation gets the contents of a record-value field and the `Set` operation changes the contents. The type-checker can raise an exception if it encounters a `RecordV`. Type-checking does not need mutation.

6. A record type lists the fields, their types, and *access modifiers*. A `Get e` operation with field `l` type-checks only if `e` has a record type that includes field `l` and where `l`‘s access is not `Write` (i.e., write-only). Similarly, a `Set e` operation with field `l` type-checks only if `e` has a record type that includes field `l` and where `l`‘s access is not `Read` (i.e., read-only). A `RecordE` has a type where every field has access `Both` — explicit type annotations (in casts and functions) can lead to types with other access modifiers. The relevant subtyping is for you to figure out as described in the problem statement.

7. A cast allows only casts to supertypes and has no run-time effect. It type-checks if the type of the expression is a subtype of the explicit annotation.