CSE P505, Winter 2009
Sample Exam Questions

Notes:

• Some of these questions are from old exams given in slightly different classes, so don’t worry too much if one or two problems feel only tangentially related to what you learned. Others were written a bit quickly, so they may be more “study problems” than “exam problems” but they are still in the style of exam problems.

• The actual exam will cover some of the same topics and some different ones. There were be roughly 6–8 questions on the exam, so not everything can be covered.

• You can bring one sheet of paper to the exam with whatever you want on it (front and back). The idea is to make sure memorization isn’t an issue, but the exam is not “open notes” which just encourages everyone to print everything remotely related to the course.

• The actual exam will have a reference page or two with some relevant inference rules and functions from class. That does not mean the whole exam is related to the reference material. You will also need to be able to read/write Caml programs, OO-style programs, etc. Most of the reference material will in fact not be directly helpful with the exam, but this way you know they will be there and you don’t have to put them on your sheet of paper.

• The exam will likely be tough, perhaps with a mean around 70%. Such an exam is actually much more fair than an exam with a mean above 90%
1. Consider this Caml code. It uses `strcmpl`, which has type `string->string->bool` and the expected behavior.

```caml
exception NoValue
let empty = fun s -> raise NoValue
let extend m x v = fun s -> if strcmp s x then v else m s
let lookup m x = m x
```

(a) *What functionality* do these three bindings provide a client?
(b) *What types* do each of the bindings have?
    (Note: They are all polymorphic and may have more general types than expected.)
2. (a) Consider this Caml code:

```caml
type t = A of int | B of (int->int)
let x = 2
let f y = x + y
let ans1 = (let x = 3 in
  let a = A (f 4) in
  let x = 5 in
  match a with A x -> x | B x -> x + 6)
let ans2 = (let x = 3 in
  let b = B f in
  let x = 5 in
  match b with A x -> x | B x -> x + 6)
```

After evaluating this code, what values are `ans1` and `ans2` bound to?

(b) Consider this Caml code:

```caml
let rec g x =
  match x with
  | [] -> []
  | hd::tl -> (fun y -> hd + y)::(g tl)
```

i. What does this function do?

ii. What is this function’s type?

iii. Write a function `h` that is the inverse of `g`. That is, `fun x -> h (g x)` would return a value equivalent to its input.
3. Consider the following Caml code.

    let catch_all1 t1 t2 = try t1 () with x -> t2 ()

    let catch_all2 t1 t2 = try t1 () with x -> t2

    (a) Under what conditions, if any, does using `catch_all1` raise an exception?
    (b) Under what conditions, if any, does using `catch_all2` raise an exception?
    (c) What type does Caml give `catch_all1`?
    (d) What type does Caml give `catch_all2`?
4. (Bad statement rules)

(a) Why do we not have this rule in our IMP statement semantics?

\[
\begin{array}{c}
H_0 \downarrow s_1 \\
H_1 \downarrow \\
H_2 \downarrow \\
H_3 \downarrow \\
H_0; s_1; (s_2; s_3) \downarrow H_3
\end{array}
\]

(b) Why do we not have this rule in our IMP statement semantics?

\[
\begin{array}{c}
H_0 \downarrow s_2 \\
H_1 \downarrow \\
H_2 \downarrow \\
H_0; s_1; s_2 \downarrow H_2
\end{array}
\]
5. When we added sums (syntax $A \ e$, $B \ e$, and $\text{match } e_1 \ \text{with } A \ x \rightarrow e_2 | B \ y \rightarrow e_3$) to the $\lambda$-calculus, we gave a small-step semantics and had exactly two constructors.

(a) Give sums a large-step semantics, still for exactly two constructors. That is, extend the call-by-value large-step judgment $e \Downarrow v$ with new rules. (Use 4 rules.)

(b) Suppose a program is written with three constructors ($A$, $B$, and $C$) and match expressions that have exactly three cases:

$$\text{match } e_1 \text{ with } A \ x \rightarrow e_2 | B \ y \rightarrow e_3 | C \ z \rightarrow e_4$$

Explain a possible translation of such a program into an equivalent one that uses only two constructors. (That is, explain how to translate the 3 constructors to use 2 constructors and how to translate match expressions. Do not write inference rules.)
6. Suppose we add *division* to our IMP expression language. In Caml, the expression syntax becomes:

\[
\text{type exp = Int of int | Var of string | Plus of exp * exp | Times of exp * exp | Div of exp * exp}
\]

Our interpreter (not shown) raises a Caml exception if the second argument to \texttt{Div} evaluates to 0. We are ignoring statements; assume an IMP program is an expression that takes an unknown heap and produces an integer.

(a) Write a Caml function \texttt{nsz} (stands for “no syntactic zero”) of type \texttt{exp->bool} that returns false if and only if its argument contains a division where the second argument is the integer constant 0. Note we are *not* interpreting the input; \texttt{nsz} is *not* even passed a heap.

(b) If we consider division-by-zero at run-time a “stuck state” and \texttt{nsz} a “type system” (where true means “type-checks”), then:

i. Is \texttt{nsz} sound? Explain.

ii. Is \texttt{nsz} complete? Explain.
7. For all subproblems, assume the simply-typed $\lambda$ calculus.

(a) Give a $\Gamma$, $e_1$, $e_2$, and $\tau$ such that $\Gamma \vdash e_1 : \tau$ and $\Gamma \vdash e_2 : \tau$ and $e_1 \neq e_2$.

(b) Give a $\Gamma_1$, $\Gamma_2$, $e$, and $\tau$ such that $\Gamma_1 \vdash e : \tau$ and $\Gamma_2 \vdash e : \tau$ and $\Gamma_1 \neq \Gamma_2$.

(c) Give a $\Gamma$, $e$, $\tau_1$, and $\tau_2$ such that $\Gamma \vdash e : \tau_1$ and $\Gamma \vdash e : \tau_2$ and $\tau_1 \neq \tau_2$. 
8. Consider a $\lambda$-calculus with tuples (i.e., “pairs with any number of fields”), so we have expressions $(e_1, e_2, ..., e_n)$ and $e.i$ and types $\tau_1 \ast \tau_2 \ast \ldots \ast \tau_n$. For each of our subtyping rules for records, explain whether or not an analogous rule for tuples makes sense.
9. Assume a typed lambda-calculus with records, references, and subtyping. For each of the following, describe exactly the conditions under which the subtyping claim holds.

Example question: \( \{l_1 : \tau_1, \ l_2 : \tau_2\} \leq \{l_1 : \tau_3, \ l_2 : \tau_4\} \)

Example answer: “when \( \tau_1 \leq \tau_3 \) and \( \tau_2 \leq \tau_4 \)”

Your answer should be “fully reduced” in the sense that if you say \( \tau \leq \tau' \), then \( \tau \) or \( \tau' \) or both should be \( \tau_i \) for some number \( i \) where \( \tau_i \) appears in the question.

*Note: We did not discuss much (at all?) in P505 that references are like records with one mutable field.*

(a) \( (\{l_1: \tau_1, l_2: \tau_2\}) \rightarrow \text{int} \leq (\{l_1: \tau_3, l_2: \tau_4\}) \rightarrow \text{int} \)

(b) \( \{l_1 : (\tau_1 \text{ ref})\} \leq \{l_1 : \tau_2\} \)

(c) \( (\tau_1 \rightarrow \tau_2) \rightarrow (\tau_3 \rightarrow \tau_4) \leq (\tau_5 \rightarrow \tau_6) \rightarrow (\tau_7 \rightarrow \tau_8) \)

(d) \( (\tau_1 \rightarrow \tau_2) \text{ ref} \leq (\tau_3 \rightarrow \tau_4) \text{ ref} \)
10. Consider this Caml syntax for a λ-calculus:

```caml
type exp = Var of string
  | Lam of string * exp
  | Apply of exp * exp
  | Int of int
  | Pair of exp * exp
  | First of exp
  | Second of exp
```

(a) Write a Caml function `swap` of type `exp->exp` that changes all `Pair` expressions by switching the order of the subexpressions, changes all `First` expressions into `Second` expressions, and changes all `Second` expressions into `First` expressions.

(b) True or false: Given an implementation of the λ-calculus, `interp(swap(e))` is always that same as `interp(e)`.

(c) True or false: Given an implementation of the λ-calculus, if `interp(swap(e))` returns `Int i`, then `interp(e)` returns `Int i`. 
11. Assume a class-based object-oriented language as in class, and a program that contains the call 
\texttt{e.f((C)e1)} where \texttt{e1} is a (compile-time) subtype of \texttt{C} and the whole call type-checks.

(a) If calls are resolved with static overloading, is it possible that removing the cast \texttt{C} (i.e., changing the call to \texttt{e.f(e1)}) could cause the program to still type-check but behave differently? Explain.

(b) If calls are resolved with static overloading and we have multiple inheritance, is it possible that removing the cast \texttt{C} (i.e., changing the call to \texttt{e.f(e1)}) could cause the program to no longer type-check? Explain.

(c) If calls are resolved with multimethods, is it possible that removing the cast \texttt{C} (i.e., changing the call to \texttt{e.f(e1)}) could cause the program to behave differently? Explain.
12. Consider these definitions in a class-based OO language:

```java
class C1 {
    int g() { return 0; }
    int f() { return g(); }
}
class C2 extends C1 {
    int g() { return 1; }
}
class C1 {
    int g() { return 0; }
    int f() { return g(); }
}
class D1 {
    private C1 x = new C1();
    int g() { return 0; }
    int f() { return x.f(); }
}
class D2 extends D1 {
    int g() { return 1; }
}
class Main {
    int m1(C1 x) { return x.f(); }
    int m2(C2 x) { return x.f(); }
    int m3(D1 x) { return x.f(); }
    int m4(D2 x) { return x.f(); }
}
```

Assume this is not the entire program, but the rest of the program does not declare subclasses of the classes above.

**Explain your answers:**

(a) True or false: Changing the body of `m1` to `return 0` produces an equivalent `m1`.
(b) True or false: Changing the body of `m2` to `return 1` produces an equivalent `m2`.
(c) True or false: Changing the body of `m3` to `return 0` produces an equivalent `m3`.
(d) True or false: Changing the body of `m4` to `return 1` produces an equivalent `m4`.
(e) How do your answers change if the rest of the program might declare subclasses of the classes above (excluding `Main`)?
13. Suppose we change the semantics of Java so that method-lookup uses multimethods instead of static overloading.

True or false. Briefly explain your answers.

(a) If all methods in program \( P \) take 0 arguments (that is, all calls look like \( e.m() \)), then \( P \) definitely behaves the same after the change.

(b) If all methods in program \( P \) take 1 argument (that is, all calls look like \( e.m(e') \)), then \( P \) definitely behaves the same after the change.

(c) If a program \( P \) typechecks without ever using subsumption, then \( P \) definitely behaves the same after the change.

(d) Given an arbitrary program \( P \), it is decidable whether \( P \) behaves the same after the change.
14. Suppose we extend a class-based object-oriented language with a keyword `null`, which has type `NullType`, which is a subtype of any type.

(a) Explain why the subtyping described above is backwards. How does some popular language you know deal with this?

(b) With static overloading or multimethods (the issue is the same), show how `null` can lead to ambiguities.
15. Consider this code in a class-based OOP language with multiple inheritance. A subclass overrides a method by defining a method with the same name and arguments.

```plaintext
class A { }
class B extends A { unit m1() { print "m1B" } }
class C extends B { unit m1() { print "m1C" } }
class D extends A { }
class E extends C, D { }
class Main {
    unit m2(D c) { print "m2D"; }
    unit m2(C c) { print "m2C"; c.m1() }
    unit m2(B b) { print "m2B"; b.m1() }
    unit main() {
        E e = new E();
        e.m1(); /* 0 */
        ((B)e).m1(); // 1
        self.m2(e); // 2
        self.m2((D)e); // 3
        self.m2((C)e); // 4
        self.m2((B)e); // 5
    }
}
```

(a) Assume the language has static overloading. For each of the lines 0–5, determine if the method call is ambiguous (“no best match”) or not. If it is not, what does executing the call print?

(b) Assume the language has multimethods. For each of the lines 0–5, determine if the method call is ambiguous (“no best match”) or not. If it is not, what does executing the call print?
16. Here are two large-step interpreters for the untyped lambda-calculus. The one on the right uses parallelism. Recall Thread.join blocks until the thread described by its argument terminates. Only the lines between the (*----------*) comments differ.

```ocaml
type exp = Var of string | Lam of string*exp | Apply of exp * exp

let subst e1_with e2_for x = ... (* unimportant *)
exn = UnboundVar

let rec interp e = let rec interp e =
  match e with match e with
  Var _ -> raise UnboundVar Var x -> raise UnboundVar
  | Lam _ -> e | Lam _ -> e
  | Apply(e1,e2) -> | Apply(e1,e2) ->
  (*----------*) (*----------*)
  let v2r = ref (Var "dummy") in
  let t = Thread.create
  let v2 = interp e2 in
  let v1 = interp e1 in
  Thread.join t;
  let v2 = !v2r in
  let v2 = interp e2 in
  let v1 = interp e1 in
  Thread.join t;
  let v2 = !v2r in

  (*----------*) (*----------*)
  match v1 with match v1 with
  Lam(x,e3) -> interp(subst e3 v2 x) Lam(x,e3) -> interp(subst e3 v2 x)
  _ -> failwith "impossible" _ -> failwith "impossible"
```

(a) Describe an input to these functions for which the interpreter on the right would raise an exception and the interpreter on the left would not. (Note: Evaluation of expressions may not terminate.)

(b) Explain why moving the line “let v2r = ref (Var "dummy") in” out to the top-level (and removing the keyword “in”) would make the interpreter on the right behave unpredictably (even for inputs with no free variables).
17. (a) Write a Caml program using locks that will always deadlock, but only because the locks provided by the Mutex library are not reentrant. (If you forget the names of library functions, just make them up and explain; you’ll get full credit.)

(b) Write a Caml program that will always deadlock even if the locks provided by the Mutex library were reentrant. (Assume threads implicitly release all locks when they terminate.) (Note: The hard part is the word “always”.)
18. Use Concurrent ML to complete an implementation of “infinite” arrays (in the sense that no index is out of bounds), without using Caml’s references or arrays. More specifically, implement the **new_array** function for this code:

```
(* Interface *)
type 'a myarray
val new_array : 'a -> 'a myarray (* Initially, every index maps to 'a *)
val set : 'a myarray -> int -> 'a -> unit (* change value in index *)
val get : 'a myarray -> int -> 'a (* return current value in index *)

(* Implementation *)
open Event
open Thread
type 'a myarray = ((int * ('a channel)) channel) * ((int * 'a) channel)

let new_array init = (* for you *)
let set (_,c) i v =  
  sync (send c (i,v))
let get (c,_) i = 
  let ret = new_channel() in 
  sync (send c (i,ret));
  sync (receive ret)
```

Hints: Do **not** worry about being efficient. Have **set** work in $O(1)$ time and **get** work in (worst-case) $O(n)$ time where $n$ is the number of **set** operations preceding it. Use an association list. Sample solution is about 15 lines, including a short helper function for traversing a list. Use **choose** and **wrap**.
19. Consider this interface and partial Concurrent ML implementation:

```ml
(* Interface *)

type gt_or_tg (* "give then take or take then give" (forever) *)
val new_gt_or_tg : unit -> gt_or_tg
val give : gt_or_tg -> int -> unit
val take : gt_or_tg -> int

(* Implementation *)

open Event

type gt_or_tg = int channel
let give ch i = sync (send ch i)
let take ch = sync (receive ch)
let new_gt_or_tg () = (* for you *)
```

Implement `new_gt_or_tg` so that this library behaves as follows:

- Each `gt_or_tg` can handle gives and takes. The integer passed to `give` is ignored and the integer returned from `take` is arbitrary (0 is fine). (This is silly, but fine on an exam.)
- For a given `gt_or_tg` consider the calls to `give` or `take` using that `gt_or_tg`. The first such call to `return` (i.e., finish evaluation) can be a give or a take. But if the first call to return is a give then the second call to return must be a take, and if the first call to return is a take, then the second call to return must be a give. Similarly, the third, fifth, seventh, etc. call to return can be a give or a take, but the next call to return must be a call to the other function.
- There is no additional guarantee that calls return in any particular order. However, if there are the same number of calls to give and take, then all should return. (The natural solution would do this; this is a technicality so you can’t claim that a solution in which no call ever returns is correct.)

Hints:

- Use `choose` and `wrap`.
- Remember to put `sync` in all the right places.
- Sample solution is 10–11 lines.
20. Suppose a bug in a garbage collector causes it to always treat memory address 0xDEADBEF as a root. Give two separate reasons that this single bug could cause a program to leak an arbitrary amount of memory.
21. You can do this problem in one of Caml, C, C++, Java, or C#. Your choice does not really change the problem.

(a) Write a short program that will exhaust memory if there is no garbage collector but take almost no space if there is a garbage-collector.

(b) Write a short program that will exhaust memory even if there is a garbage collector. Create only small objects.