Name $\qquad$
There are 8 questions worth a total of 100 points. Please budget your time so you get to all of the questions. Keep your answers brief and to the point.

You may refer to the following references:
Your primary compiler textbook(s)
Course lecture slides and notes
Exam topic list
x86-64 Instructions and ABI (Univ. of Chicago handout) MiniJava Grammar

No other books or other materials, including old exams or homework. You may use electronic copies of the materials accessed from the exam resources page on the course web site, but you may not access any other information on the internet, or other resources on your computer.

Please wait to turn the page until everyone is told to begin.

Score $\qquad$
1 / 10

2 $\qquad$ / 10

3 $\qquad$ / 18

4 $\qquad$ / 8

5 / 10

6 / 18
$\qquad$

8 $\qquad$ / 14

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Question 1. (10 points) Regular expressions. (a) (5 points) Give a regular expression that generates strings representing currency amounts formatted as follows: each string starts with the character ' $\$$ ' followed by comma-separated groups of decimal digits followed by a '.' and two decimal digits. Each group of digits to the left of the decimal point consists of three digits except for the leftmost one, which might only have one or two digits. Examples: $\$ 0.00, \$ 12,345.67, \$ 0,000,000.00$. Strings that are not in this set: $\$ .00$ (no digit to the left of '.'), $\$ 1234.56$ (no comma between 1 and 2), $\$ 0$ (no '.' followed by two digits), $\$ 1.5$ (only one digit following the '.'), $\$ 12,34,567.89$ (only two digits ' 34 ' between two commas), $\$, 123.45$ (no digit to the left of the comma).

Ground rules (the fine print): You may only use the basic operations of concatenation, choice (|), and repetition $\left(^{*}\right.$ ) plus the derived operators? and +, and simple character classes like [abc09] and [^a-z]. You may use abbreviations like vowels = [aeiou]. You may not use more complex operators found in various software tools that handle extended regular expressions and should not use ' $\backslash$ ' or other escape characters.
(b) (5 points) Draw a DFA that accepts currency amounts as defined above.

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Question 2. (10 points) CFGs and ambiguity. Consider the following grammar that generates all sequences of balanced parentheses, including the empty string. Examples: ()$,(()),(())(())),()()()$, etc.
$S::=(S)|S S| \varepsilon$
(a) (5 points) Show that this grammar is ambiguous.
(b) (5 points) Give an unambiguous grammar that generates the same set of strings as the original grammar.

Question 3. (18 points) The more-or-less-same-old LR-parsing question. Consider the following grammar, which is meant to represent expressions with optional parentheses and type casts.
0. $\exp ^{\prime}::=\exp \$$

1. exp $::=\mathrm{id}$
2. exp::= ( exp )
3. exp::= ( type ) exp
4. type $::=\mathrm{id}$
(a) (10 points) Draw the $\operatorname{LR}(0)$ state machine for this grammar. (You do not need to include the table with shift/reduce and goto actions, although you can write that out later if you find it useful to answer other parts of the question.)

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Question 3. (cont.) Grammar repeated for reference
0. $\exp ^{\prime}::=\exp \$$

1. exp $::=\mathrm{id}$
2. exp $:=(\exp )$
3. exp $::=($ type $)$ exp
4. type $::=\mathrm{id}$
(b) (4 points) Compute First, Follow, and Nullable for each of the non-terminals in this grammar.
(c) (2 points) Is this grammar $\operatorname{LR}(0)$ ? Why or why not?
(d) (2 points) Is this grammar SLR? Why or why not?

Question 4. (8 points) (LL parsing/grammars) Consider the following grammar:
0. $S^{\prime}::=S \$$

1. $S::=\mathrm{w} D \mathrm{y}$
2. $D::=D \mathrm{x}$
3. $D::=\mathrm{z}$

Is this a $\operatorname{LL}(1)$ grammar suitable for top-down predictive parsing? If yes, give a specific technical justification for your answer. If not, give a grammar that generates the same language and is LL(1) if that is possible. If no LL(1) grammar can generate the same language produced by the original grammar, give an explanation of why this is not possible.

Question 5. (10 points) Abstract syntax and semantics. Suppose we have the following assignment statement in a MiniJava program:

$$
\mathrm{x}=\text { this.m(17, } \mathrm{p} \& \& q) ;
$$

(a) (5 points) Draw an abstract syntax tree (AST) for this statement in the blank space at the bottom of the page. You are not expected to remember the exact names of the classes or node types in the MiniJava AST package or your project code, but your AST should have the appropriate level of detail that would be found there and should use reasonable names for the nodes if you don't remember the specific MiniJava ones.
(b) (5 points) After you have drawn your AST, annotate it by outlining the semantic and type checks that would need to be done at each point in the AST to verify that this statement is a semantically as well as syntactically legal MiniJava statement.

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Question 6. (18 points) A little x86-64 hacking. A clever way to implement a function to calculate $n$ ! is as follows:

```
int fact(int n) {
    return factaux(n, 1);
}
// return n! * acc
int factaux(int n, int acc) {
    if (n < 2)
        return acc;
    else
        return factaux(n-1, n*acc);
}
```

(For programming language geeks - yes, this is a tail-recursive version of the factorial function. Feel free to ignore this observation and just get on with the question.)

Your job is to translate these two functions into x86-64 assembly language using the gcc/AT\&T/Linux assembler syntax and the x86-64 register and function call conventions that we have used in our code examples.

You must implement the code for fact exactly as given using the standard x86-64 function call and stack frame conventions. But, if you want, you can take advantage of the observation that factaux is basically implementing a loop, where each time the function calls itself recursively it simply goes back to the beginning of factaux after updating the parameters $n$ and acc to be $n-1$ and $n *$ acc respectively. So, if you want, you can implement factaux using a loop, or you can implement the recursive function calls as written, or otherwise hand-optimize the code - whichever is easiest and fastest during an exam.

We suggest you use the remainder of this page for scratch work, and then write the actual code on the next page.
(write your code on next page - feel free to detach this page while you're working.)

Question 6. (cont.) Write your x86-64 versions of fact and factaux below.

The next two questions concern the following control flow graph:


Question 7. (12 points) Dataflow analysis. Recall from lecture that live-variable analysis determines for each point $p$ in a program which variables are live at that point. A live variable $v$ at point $p$ is one where there exists a path from point $p$ to another point $q$ where $v$ is used without $v$ being redefined anywhere along that path. The sets for the live variable dataflow problem are:

```
use[b] = variables used in block b before any definition
def[b]= variables defined in block b and not later killed in b
in[b] = variables live on entry to block b
out[b] = variables live on exit from block b
```

The dataflow equations for live variables are

$$
\begin{aligned}
& \operatorname{in}[b]=\operatorname{use}[b] \cup(\operatorname{out}[b]-\operatorname{def}[b]) \\
& \operatorname{out}[b]=\cup_{\mathrm{s} \in \operatorname{succ}[b]} \operatorname{in}[s]
\end{aligned}
$$

On the next page, calculate the use and def sets for each block, then solve for the in and out sets of each block. A table is provided with room for the use and def sets for each block and up to three iterations of the main algorithm to solve for the in and out sets. If the algorithm does not converge after three iterations, use additional space until it does.

Hint: remember that live-variables is a backwards dataflow problem, so the algorithm should update the sets from the end of the flowgraph towards the beginning to reduce the total amount of work needed.

You may remove this page for reference while working these problems.

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Question 7. (cont.) Write the results of calculations for live variables in the chart below. Use the rest of the page for additional space if needed.

| Block | use | def | out (1) | in (1) | out (2) | in (2) | out (3) | in (3) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B3 |  |  |  |  |  |  |  |  |
| B2 |  |  |  |  |  |  |  |  |
| B1 |  |  |  |  |  |  |  |  |
| B0 |  |  |  |  |  |  |  |  |

Question 8. Dominators and SSA. (14 points) (a) (6 points) Using the same control flow graph from the previous problem, complete the following table. List for each node: the nodes that dominate it, the node that is its immediate dominator (if any), and the nodes that are in its dominance frontier (if any):

| Node | Dominators | IDOM | Dominance Frontier |
| :---: | :---: | :---: | :---: |
| B0 |  |  |  |
| B1 |  |  |  |
| B2 |  |  |  |
| B3 |  |  |  |

(b) (8 points) Now redraw the flowgraph in SSA (static single-assignment) form. You need to insert appropriate $\Phi$-functions where they are required and add appropriate version numbers to all variables. Do not insert $\Phi$-functions at the beginning of a block if they clearly would not be appropriate there, but we will not penalize extra $\Phi$-functions elsewhere if they are inserted correctly. You do not need to trace the steps of any particular algorithm to place the $\Phi$-functions as long as you add them to the flowgraph in appropriate places. Additional space is provided on the next page if needed.

Question 8. (cont.) Additional space if needed.

