

## Announcements

- Final project proposal: **today at noon**
- Final project presentations: **next Wednesday in class**  
> ~5 min ppt talk
- Project 2 artifact winners...

### Readings

- Seitz et al., A Comparison and Evaluation of Multi-View Stereo Reconstruction Algorithms, CVPR 2006, pp. 519-526  
> [http://vision.middlebury.edu/mview/seitz\\_mview\\_cvpr06.pdf](http://vision.middlebury.edu/mview/seitz_mview_cvpr06.pdf)

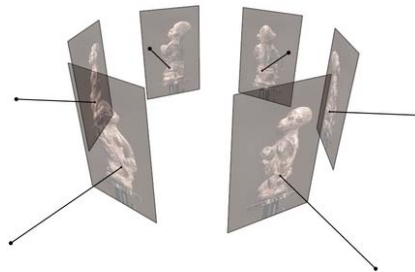
## Multi-view Stereo



## Multi-view Stereo

Input: calibrated images from several viewpoints

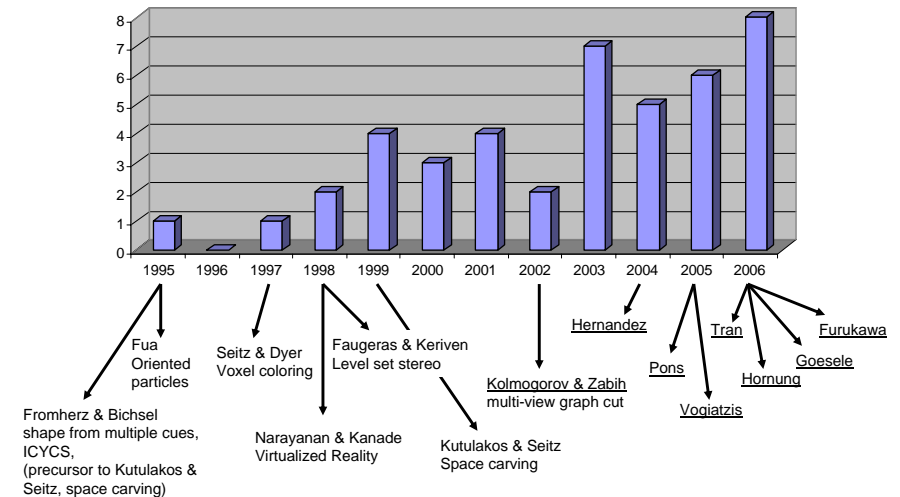
Output: 3D object model

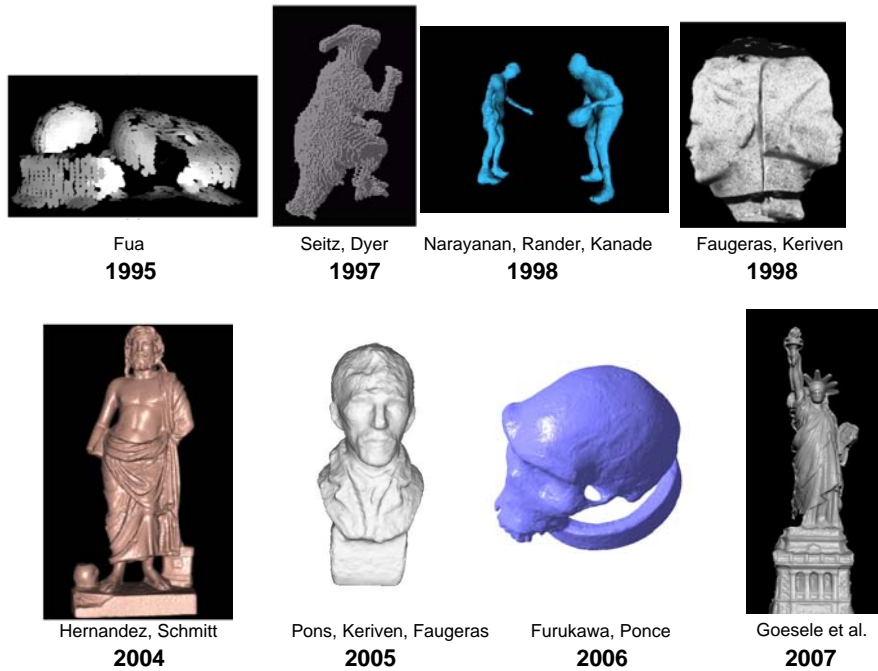


Figures by Carlos Hernandez

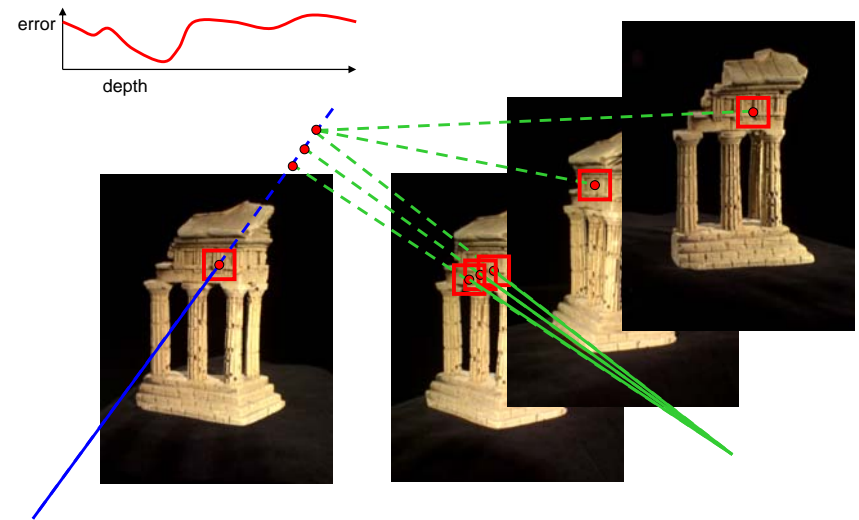
## History

number of papers in CVPR, ECCV, and ICCV, by year

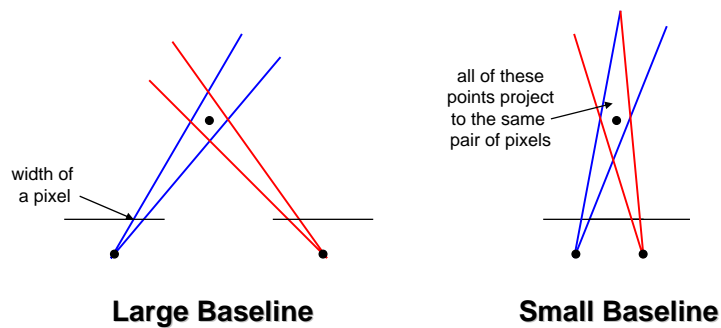




## Stereo: basic idea



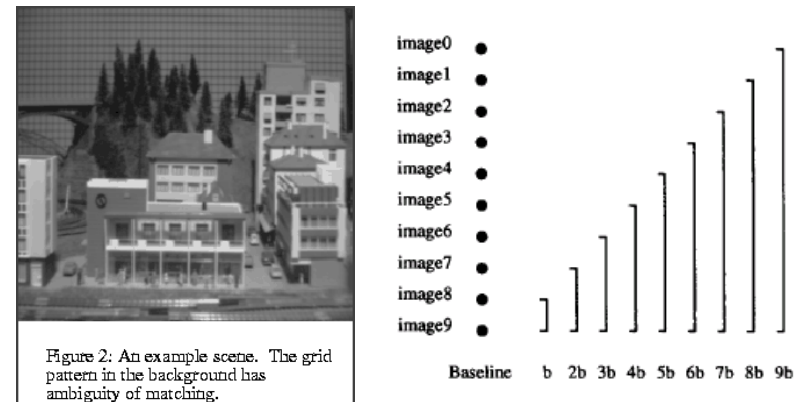
## Choosing the stereo baseline

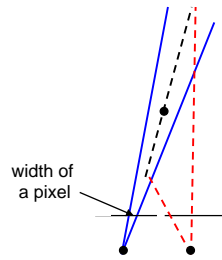
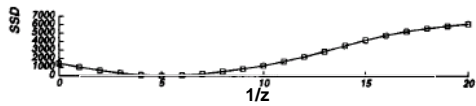


What's the optimal baseline?

- Too small: large depth error
- Too large: difficult search problem

## The Effect of Baseline on Depth Estimation





pixel matching score

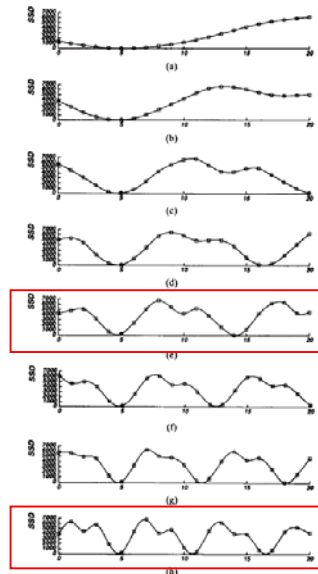
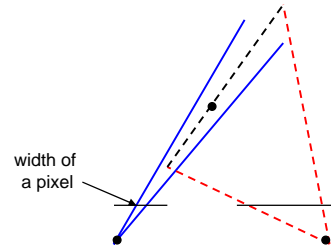
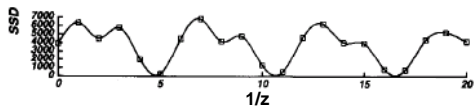


Fig. 5. SSD values versus inverse distance: (a)  $D = b$ ; (b)  $B = 2b$ ; (c)  $D = 3b$ ; (d)  $D = 4b$ ; (e)  $D = 5b$ ; (f)  $D = 6b$ ; (g)  $D = 7b$ ; (h)  $D = 8b$ . The horizontal axis is normalized such that  $8\Delta F = 1$ .

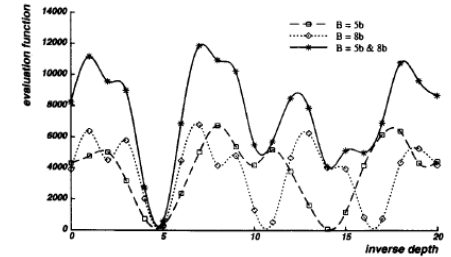


Fig. 6. Combining two stereo pairs with different baselines.

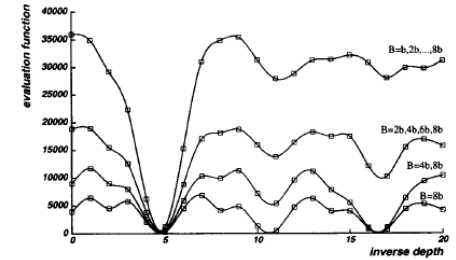


Fig. 7. Combining multiple baseline stereo pairs.

## Multibaseline Stereo

### Basic Approach

- Choose a reference view
- Use your favorite stereo algorithm BUT
  - > replace two-view SSD with SSSD over all baselines

### Limitations

- Only gives a depth map (not an "object model")
- Won't work for widely distributed views:

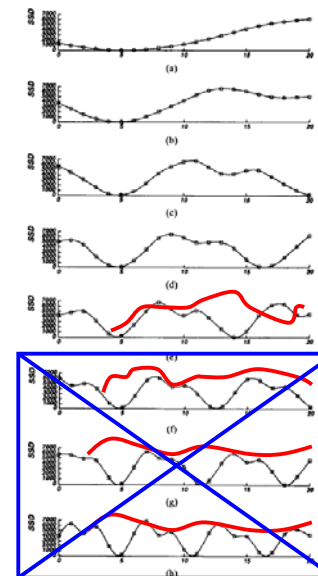


Fig. 5. SSD values versus inverse distance: (a)  $D = b$ ; (b)  $B = 2b$ ; (c)  $D = 3b$ ; (d)  $D = 4b$ ; (e)  $D = 5b$ ; (f)  $D = 6b$ ; (g)  $D = 7b$ ; (h)  $D = 8b$ . The horizontal axis is normalized such that  $8\Delta F = 1$ .

## Problem: *visibility*

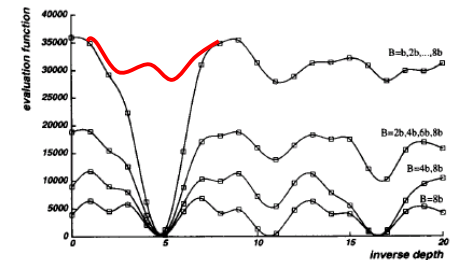


Fig. 7. Combining multiple baseline stereo pairs.

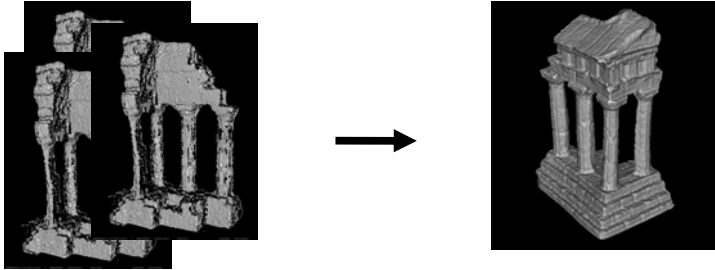
## Some Solutions

- Match only nearby photos [Narayanan 98]
- Use NCC instead of SSD, ignore NCC values > threshold [Hernandez & Schmitt 03]

## Merging Depth Maps

vrp [Curless and Levoy 1996]

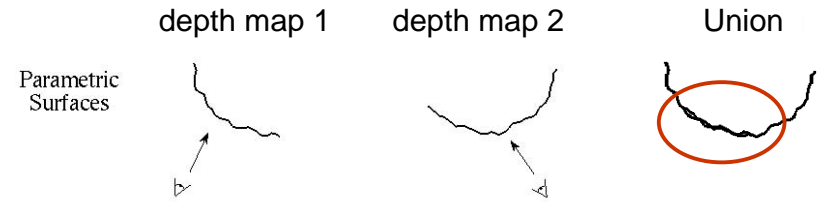
- compute weighted average of depth maps



set of depth maps  
(one per view)

merged surface  
mesh

## Merging depth maps

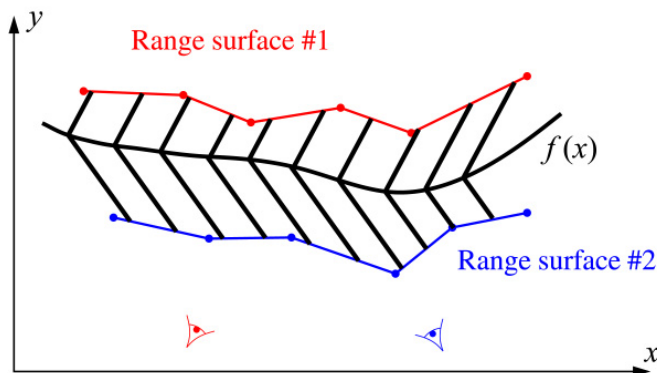


Naïve combination (union) produces artifacts

Better solution: find “average” surface

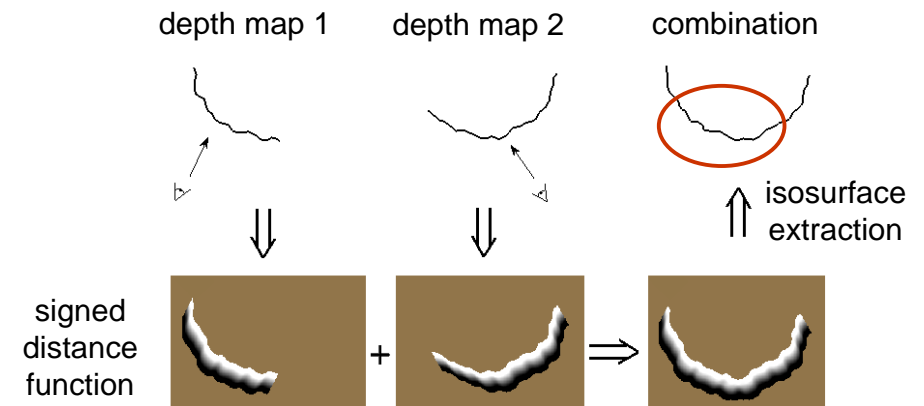
- Surface that minimizes sum (of squared) distances to the depth maps

## Least squares solution



$$E(f) = \sum_{i=1}^N \int d_i^2(x, f) dx$$

## VRIP [Curless & Levoy 1996]



## Merging Depth Maps: Temple Model



input image



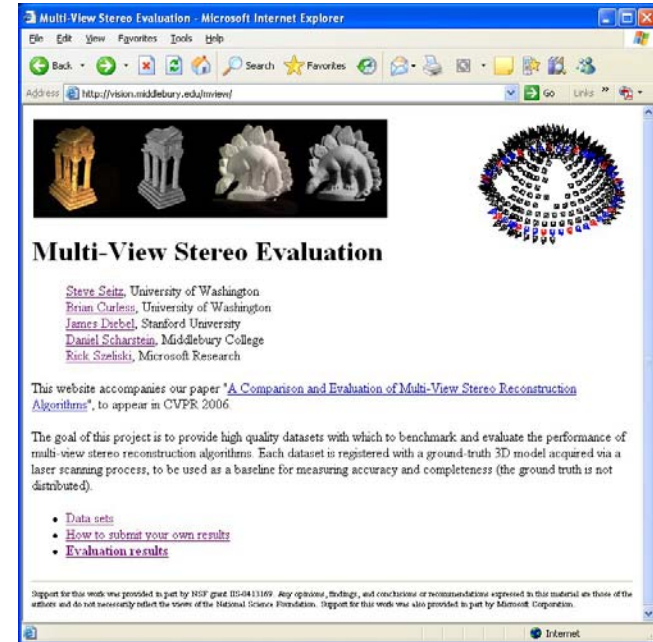
317 images  
(hemisphere)



ground truth model

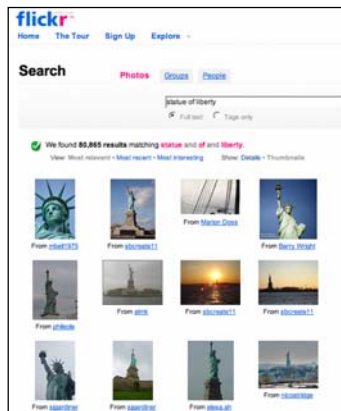
[Goesele, Curless, Seitz, 2006](#)

Michael Goesele



## Multi-view stereo from Internet Collections

[\[Goesele, Snavely, Curless, Hoppe, Seitz, ICCV 2007\]](#)



## Challenges

- appearance variation



- resolution

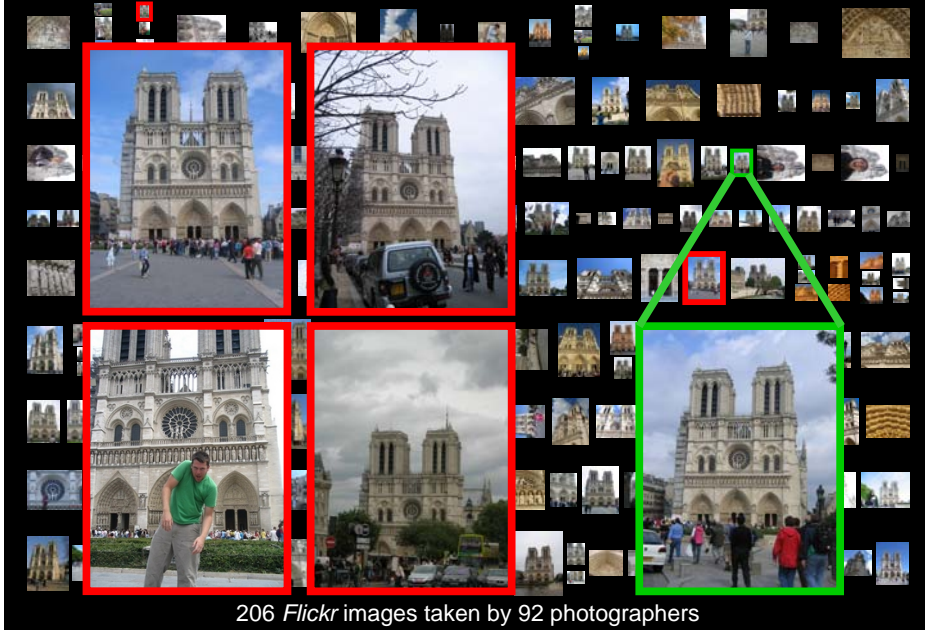


- massive collections

82,754 results for photos matching **notre** and **dame** and **paris**.



# Law of Large Image Collections



206 Flickr images taken by 92 photographers

4 best neighboring views

reference view

Local view selection

- Automatically select neighboring views for each **point** in the image
- Desiderata: good matches AND good baselines

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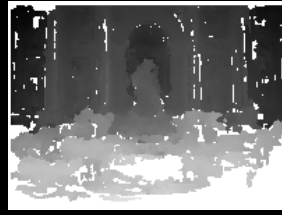
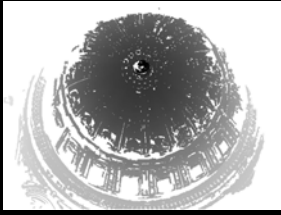
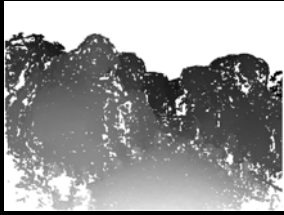
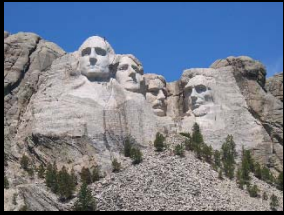
4 best neighboring views

reference view

Local view selection

- Automatically select neighboring views for each **point** in the image
- Desiderata: good matches AND good baselines

# Results



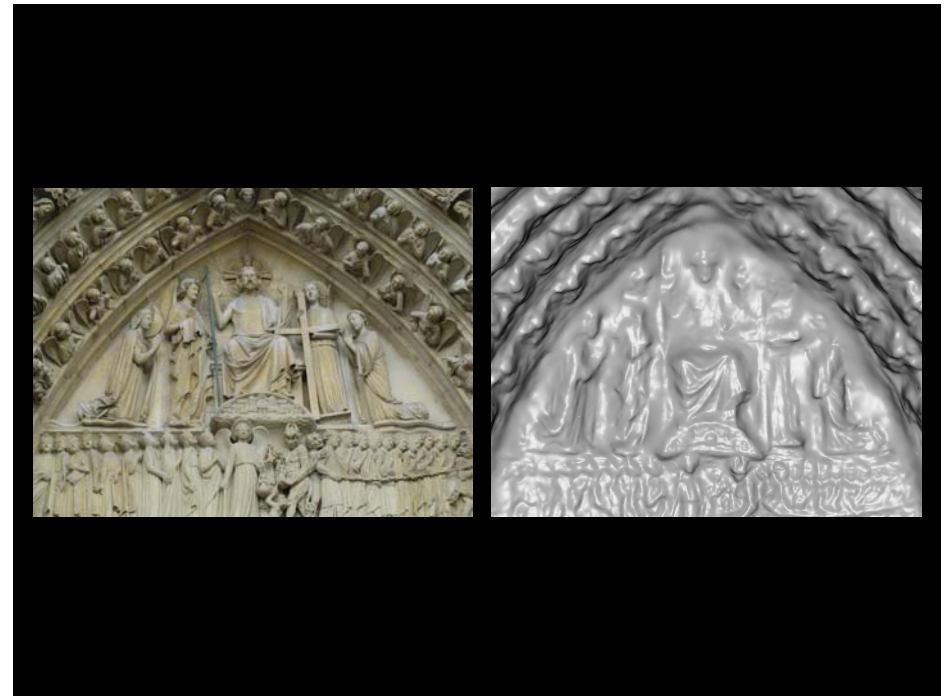
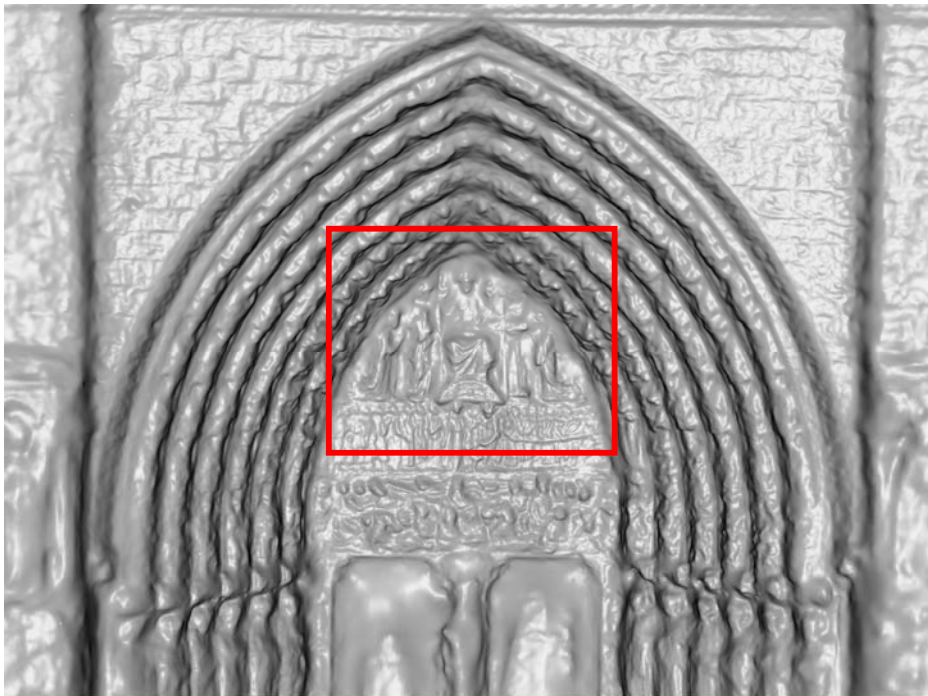
Mt. Rushmore  
160 images  
60 photographers

St. Peter  
151 images  
50 photographers

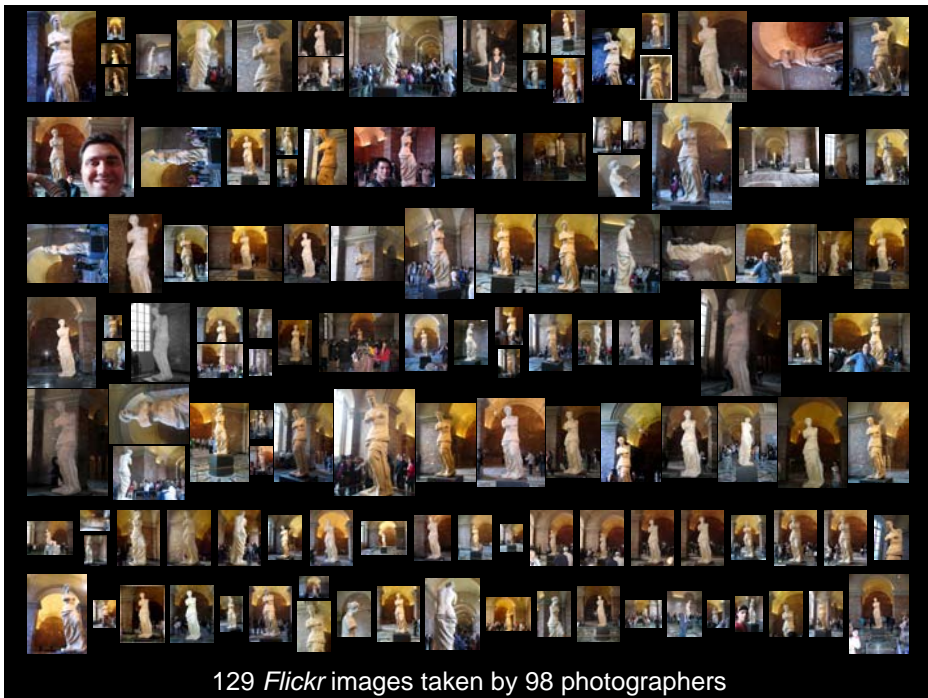
Trevi Fountain  
106 images  
51 photographers

Notre Dame de Paris

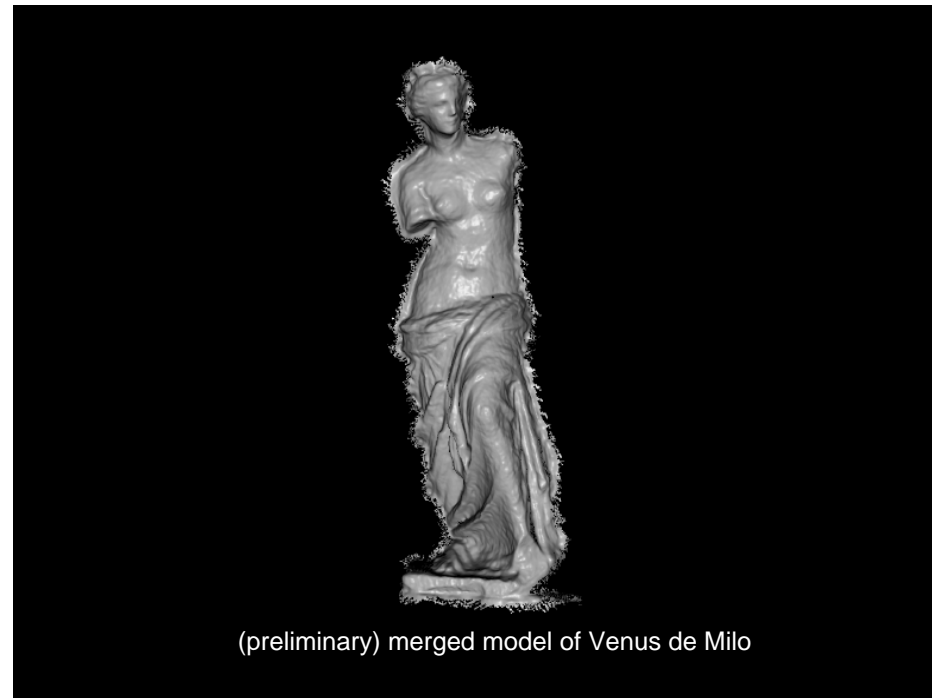
653 images  
313 photographers







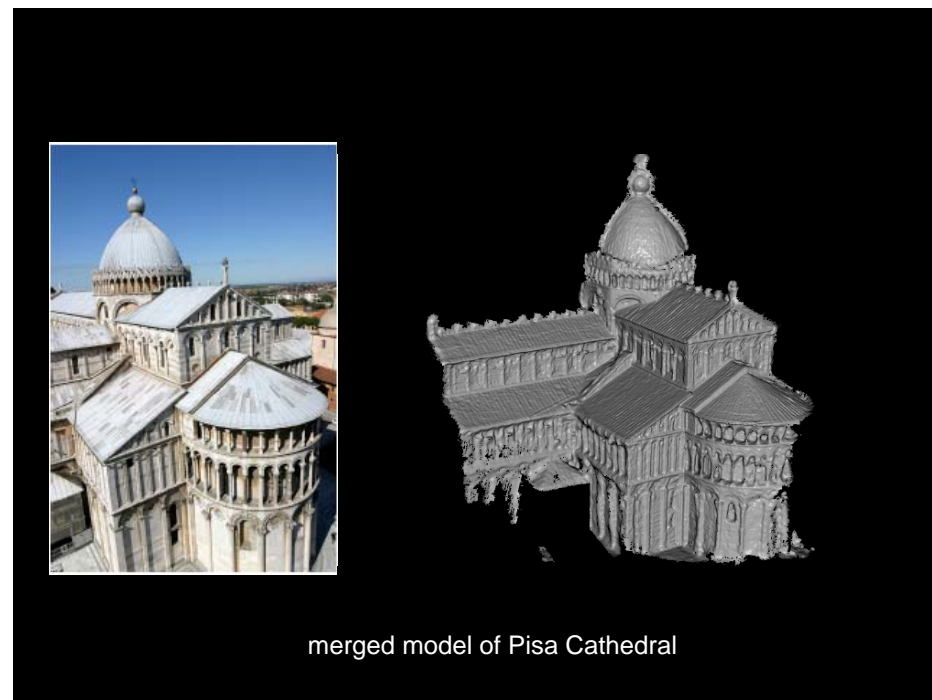
129 Flickr images taken by 98 photographers



(preliminary) merged model of Venus de Milo

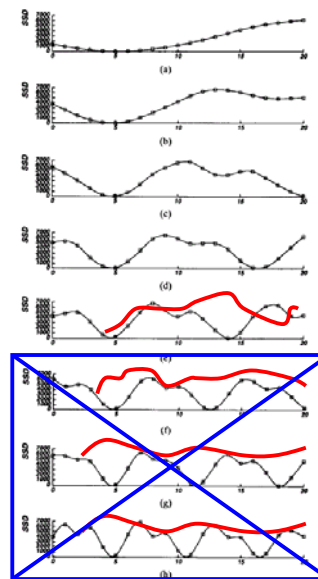
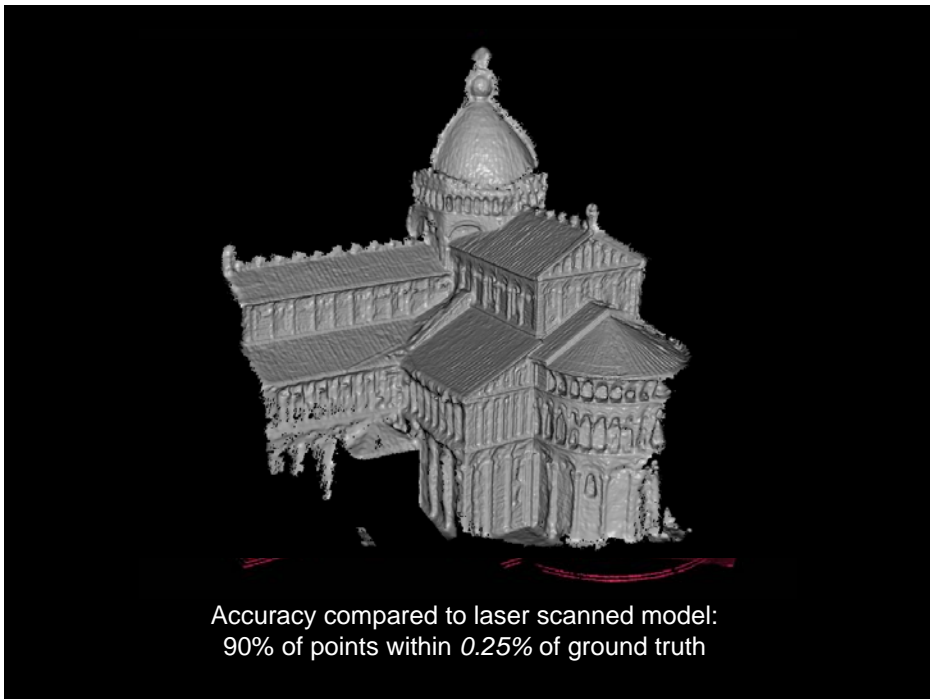


56 Flickr images taken by 8 photographers

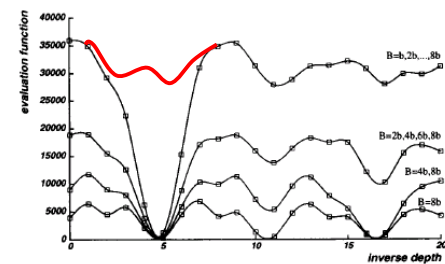


merged model of Pisa Cathedral





Problem: *visibility*

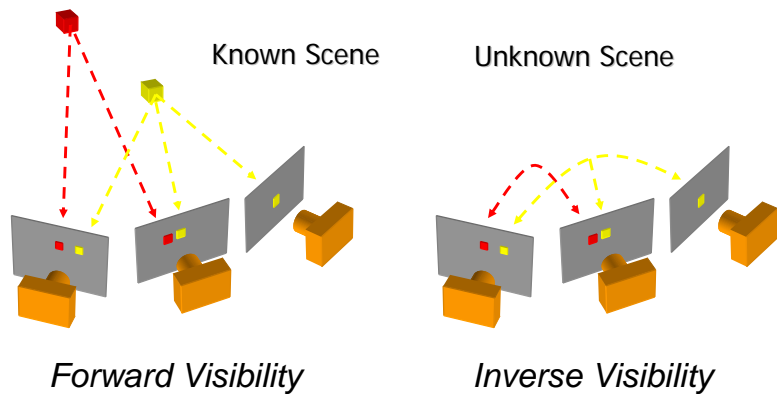


Some Solutions

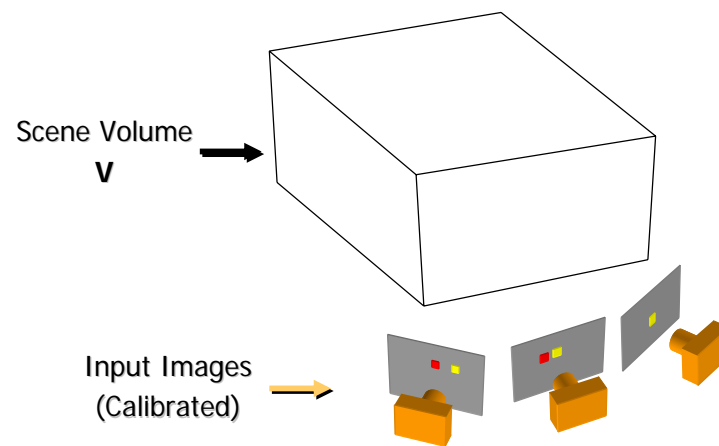
- Match only nearby photos [Narayanan 98]
- Use NCC instead of SSD, Ignore NCC values > threshold [Hernandez & Schmitt 03]

## The visibility problem

Which points are visible in which images?

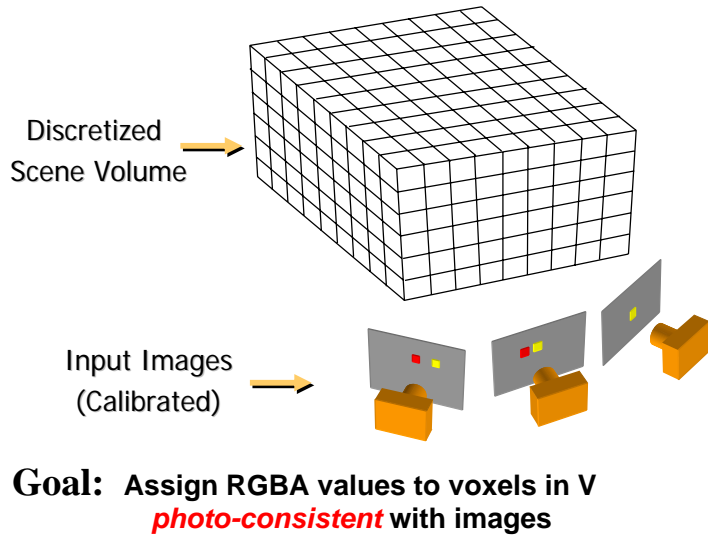


## Volumetric stereo

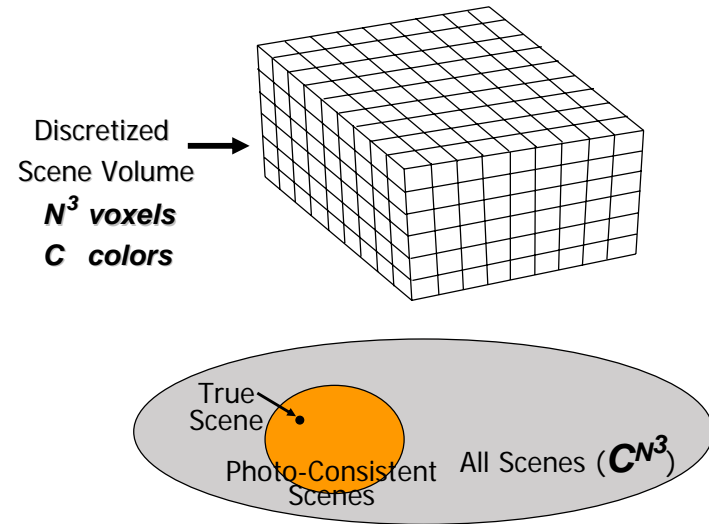


**Goal:** Determine occupancy, "color" of points in  $V$

## Discrete formulation: Voxel Coloring



## Complexity and computability



## Issues

### Theoretical Questions

- Identify class of *all* photo-consistent scenes

### Practical Questions

- How do we compute photo-consistent models?

## Voxel coloring solutions

### 1. $C=2$ (shape from silhouettes)

- Volume intersection [Baumgart 1974]
  - > For more info: *Rapid octree construction from image sequences*. R. Szeliski, CVGIP: Image Understanding, 58(1):23-32, July 1993. (this paper is apparently not available online) or
  - > W. Matusik, C. Buehler, R. Raskar, L. McMillan, and S. J. Gortler, *Image-Based Visual Hulls*, SIGGRAPH 2000 ([pdf 1.6 MB](#))

### 2. $C$ unconstrained, viewpoint constraints

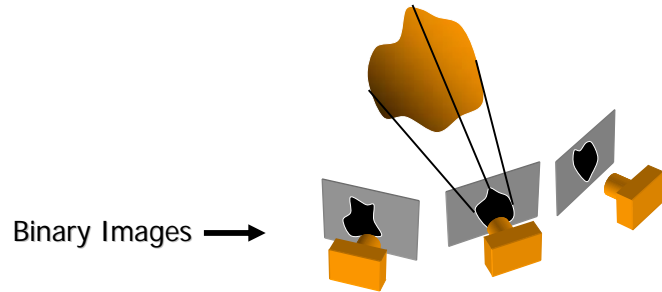
- Voxel coloring algorithm [Seitz & Dyer 97]

### 3. General Case

- Space carving [Kutulakos & Seitz 98]

## Reconstruction from Silhouettes (C = 2)

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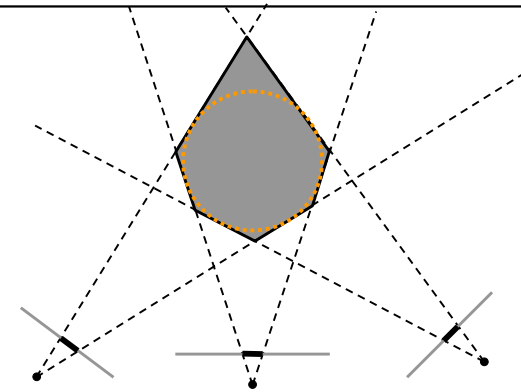


### Approach:

- *Backproject* each silhouette
- Intersect backprojected volumes

## Volume intersection

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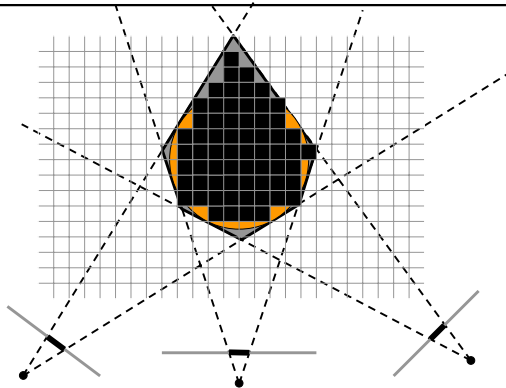


### Reconstruction Contains the True Scene

- But is generally not the same
- In the limit (all views) get *visual hull*
  - > Complement of all lines that don't intersect S

## Voxel algorithm for volume intersection

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### Color voxel black if on silhouette in every image

- $O(N^3)$ , for  $M$  images,  $N^3$  voxels
- Don't have to search  $2^{N^3}$  possible scenes!

## Properties of Volume Intersection

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### Pros

- Easy to implement, fast
- Accelerated via octrees [Szeliski 1993] or interval techniques [Matusik 2000]

### Cons

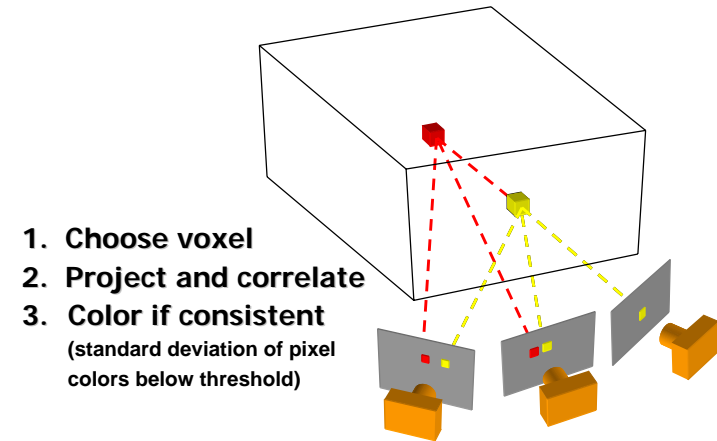
- No concavities
- Reconstruction is not photo-consistent
- Requires identification of silhouettes



## Voxel Coloring Solutions

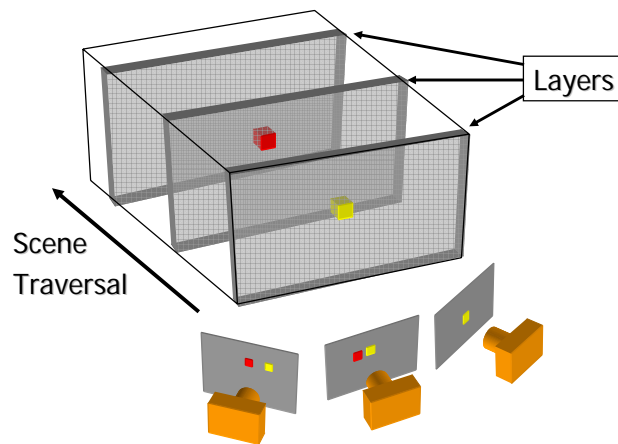
1.  $C=2$  (silhouettes)
  - Volume intersection [Baumgart 1974]
2.  $C$  unconstrained, viewpoint constraints
  - Voxel coloring algorithm [Seitz & Dyer 97]
    - > For more info: <http://www.cs.washington.edu/homes/seitz/papers/jicv99.pdf>
3. General Case
  - Space carving [Kutulakos & Seitz 98]

## Voxel Coloring Approach



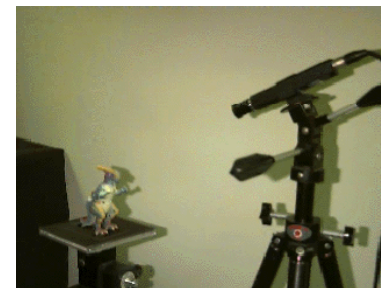
**Visibility Problem:** in which images is each voxel visible?

## Depth Ordering: visit occluders first!



**Condition:** depth order is the *same for all input views*

## Calibrated Image Acquisition



Calibrated Turntable



Selected Dinosaur Images



Selected Flower Images

## Voxel Coloring Results (Video)

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### Dinosaur Reconstruction

72 K voxels colored  
7.6 M voxels tested  
7 min. to compute  
on a 250MHz SGI



### Flower Reconstruction

70 K voxels colored  
7.6 M voxels tested  
7 min. to compute  
on a 250MHz SGI

## Improvements

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### Unconstrained camera viewpoints

- Space carving [[Kutulakos & Seitz 98](#)]

### Evolving a surface

- Level sets [[Faugeras & Keriven 98](#)]
- More recent [work](#) by Pons et al.

### Global optimization

- Graph cut approaches
  - > [[Kolmogoriv & Zabih, ECCV 2002](#)]
  - > [[Vogiatzis et al., PAMI 2007](#)]

### Modeling shiny (and other reflective) surfaces

- e.g., [Zickler et al., Helmholtz Stereopsis](#)

See today's reading for an overview of the state of the art