

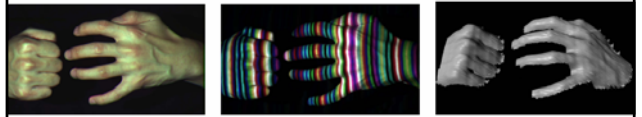
## Announcements

- Project 3 extension: **Wednesday at noon**
- Final project proposal extension: **Friday at noon**
  - > **consult with Steve, Rick, and/or Ian now!**
- Project 2 artifact winners...

### Readings

- S. M. Seitz and C. R. Dyer, [Photorealistic Scene Reconstruction by Voxel Coloring](#), *International Journal of Computer Vision*, 35(2), 1999, pp. 151-173.
  - > <http://www.cs.washington.edu/homes/seitz/papers/ijcv99.pdf>

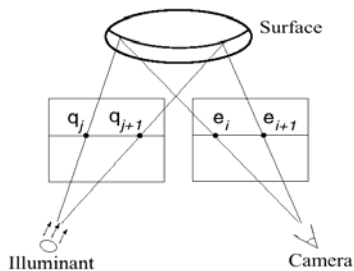
## Active stereo with structured light



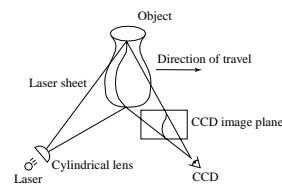
Project “structured” light patterns onto the object

- simplifies the correspondence problem

## Active stereo with structured light



## Laser scanning



<http://graphics.stanford.edu/projects/mich/>

Optical triangulation

- Project a single stripe of laser light
- Scan it across the surface of the object
- This is a very precise version of structured light scanning

## 3D cameras



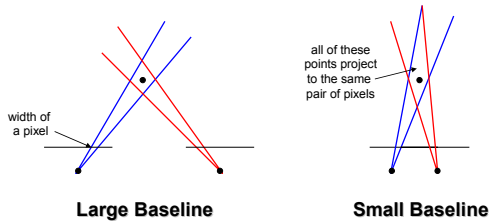
Portable 3D laser scanner (this one by Minolta)



## Multiview stereo



## Choosing the stereo baseline



What's the optimal baseline?

- Too small: large depth error
- Too large: difficult search problem

## The Effect of Baseline on Depth Estimation

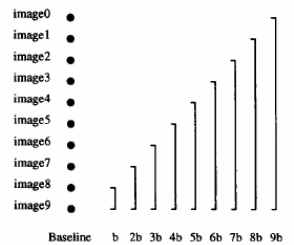
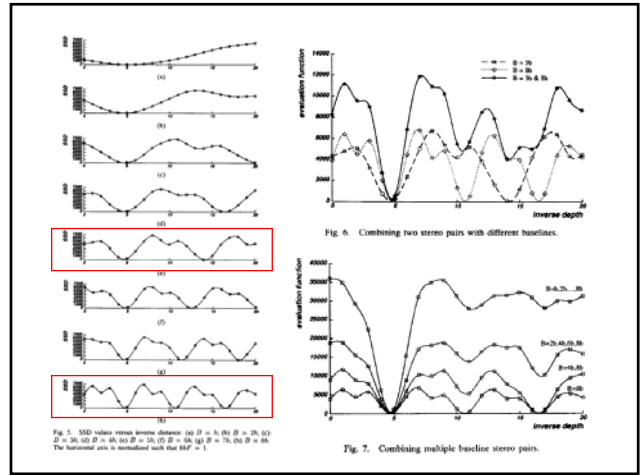
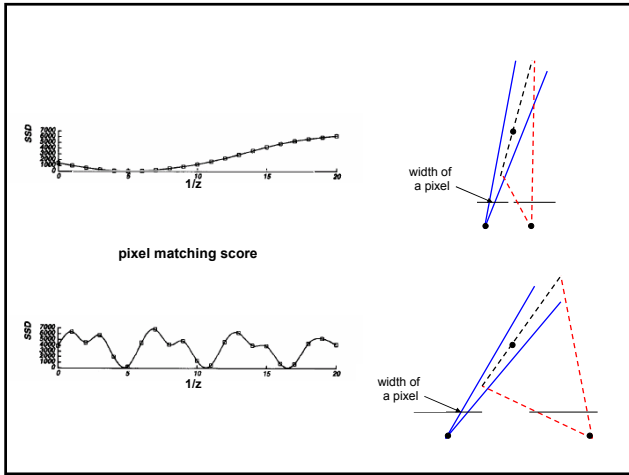


Figure 2: An example scene. The grid pattern in the background has ambiguity of matching.



## Multibaseline Stereo

### Basic Approach

- Choose a reference view
- Use your favorite stereo algorithm BUT
  - > replace two-view SSD with SSD over all baselines

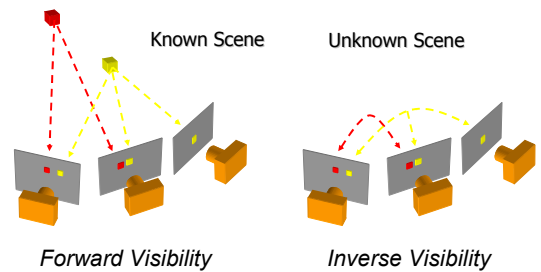
### Limitations

- Must choose a reference view (bad)
- Visibility!

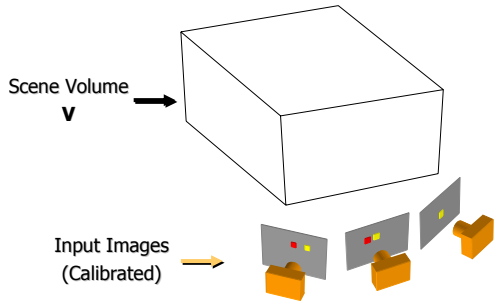
CMU's 3D Room Video

## The visibility problem

Which points are visible in which images?

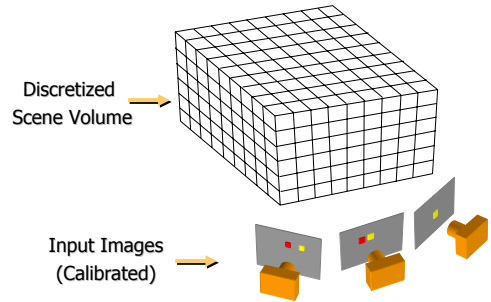


## Volumetric stereo



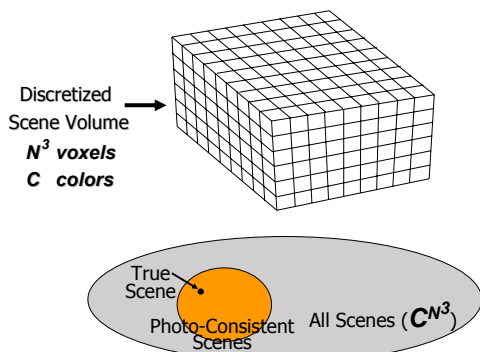
**Goal:** Determine occupancy, "color" of points in  $V$

## Discrete formulation: Voxel Coloring



**Goal:** Assign RGBA values to voxels in  $V$   
*photo-consistent* with images

## Complexity and computability



## Issues

### Theoretical Questions

- Identify class of *all* photo-consistent scenes

### Practical Questions

- How do we compute photo-consistent models?

## Voxel coloring solutions

### 1. C=2 (shape from silhouettes)

- Volume intersection [Baumgart 1974]
  - > For more info: *Rapid octree construction from image sequences*. R. Szeliski, CVGIP: Image Understanding, 58(1):23-32, July 1993. (this paper is apparently not available online) or
  - > W. Matusik, C. Buehler, R. Raskar, L. McMillan, and S. J. Gortler, *Image-Based Visual Hulls*, SIGGRAPH 2000 ( [pdf 1.6 MB](#) )

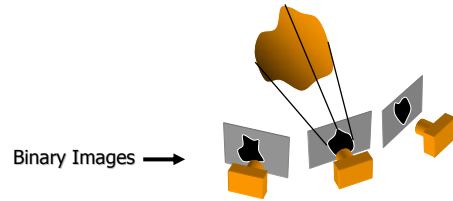
### 2. C unconstrained, viewpoint constraints

- Voxel coloring algorithm [Seitz & Dyer 97]

### 3. General Case

- Space carving [Kutulakos & Seitz 98]

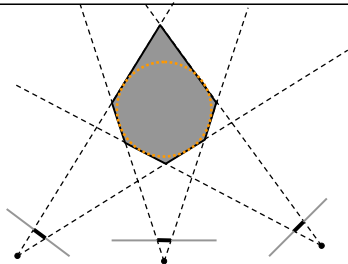
## Reconstruction from Silhouettes (C = 2)



### Approach:

- *Backproject* each silhouette
- Intersect backprojected volumes

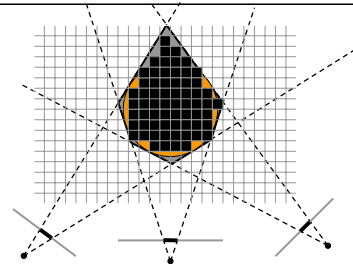
## Volume intersection



### Reconstruction Contains the True Scene

- But is generally not the same
- In the limit (all views) get *visual hull*
  - > Complement of all lines that don't intersect S

## Voxel algorithm for volume intersection



### Color voxel black if on silhouette in every image

- $O(N^3)$ , for M images,  $N^3$  voxels
- Don't have to search  $2^{N^3}$  possible scenes!

## Properties of Volume Intersection

### Pros

- Easy to implement, fast
- Accelerated via octrees [Szeliski 1993] or interval techniques [Matusik 2000]

### Cons

- No concavities
- Reconstruction is not photo-consistent
- Requires identification of silhouettes

## Voxel Coloring Solutions

### 1. $C=2$ (silhouettes)

- Volume intersection [Baumgart 1974]

### 2. $C$ unconstrained, viewpoint constraints

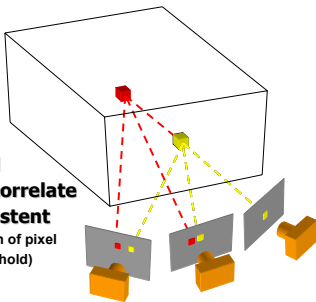
- Voxel coloring algorithm [Seitz & Dyer 97]  
> For more info: <http://www.cs.washington.edu/homes/seitz/papers/icv99.pdf>

### 3. General Case

- Space carving [Kutulakos & Seitz 98]

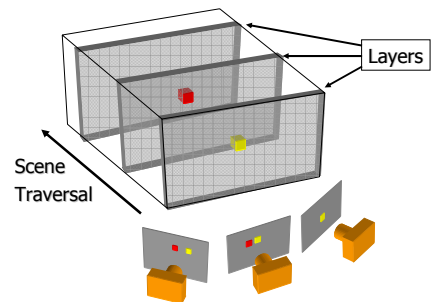
## Voxel Coloring Approach

1. Choose voxel
2. Project and correlate
3. Color if consistent  
(standard deviation of pixel colors below threshold)



**Visibility Problem:** in which images is each voxel visible?

## Depth Ordering: visit occluders first!

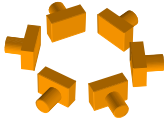


**Condition:** depth order is the *same for all input views*

## Panoramic Depth Ordering

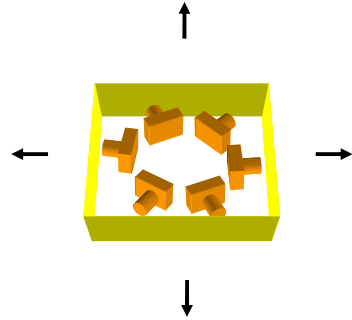
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- Cameras oriented in many different directions
- Planar depth ordering does not apply



## Panoramic Depth Ordering

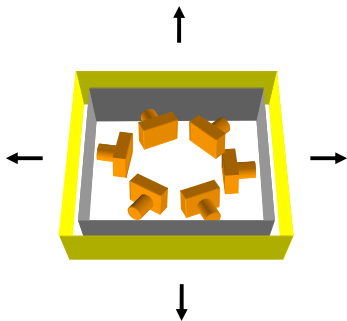
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**Layers radiate outwards from cameras**

## Panoramic Layering

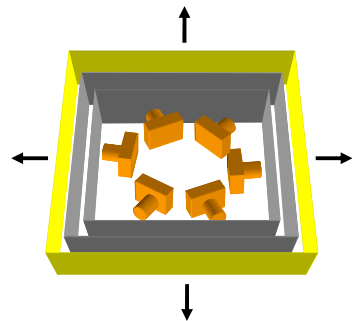
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**Layers radiate outwards from cameras**

## Panoramic Layering

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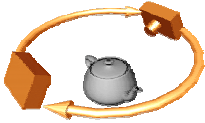


**Layers radiate outwards from cameras**

## Compatible Camera Configurations

### Depth-Order Constraint

- Scene outside convex hull of camera centers



*Inward-Looking*



*Outward-Looking*

## Calibrated Image Acquisition



*Calibrated Turntable*



**Selected Dinosaur Images**



**Selected Flower Images**

## Voxel Coloring Results (Video)



### **Dinosaur Reconstruction**

72 K voxels colored  
7.6 M voxels tested  
7 min. to compute  
on a 250MHz SGI

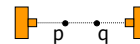


### **Flower Reconstruction**

70 K voxels colored  
7.6 M voxels tested  
7 min. to compute  
on a 250MHz SGI

## Limitations of Depth Ordering

A view-independent depth order may not exist



Need more powerful general-case algorithms

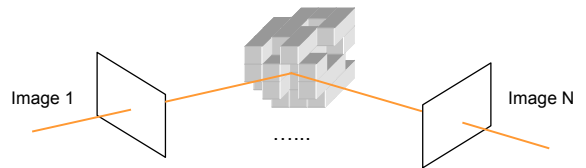
- Unconstrained camera positions
- Unconstrained scene geometry/topology



## Voxel Coloring Solutions

1.  $C=2$  (silhouettes)
  - Volume intersection [Baumgart 1974]
2.  $C$  unconstrained, viewpoint constraints
  - Voxel coloring algorithm [Seitz & Dyer 97]
3. General Case
  - Space carving [Kutulakos & Seitz 98]
  - > For more info: <http://www.cs.washington.edu/homes/seitz/papers/kutu-9cv00.pdf>

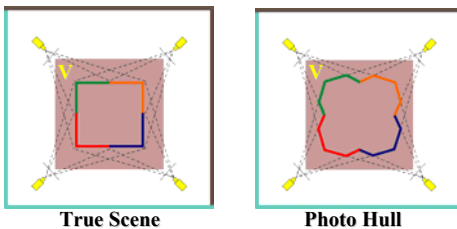
## Space Carving Algorithm



### Space Carving Algorithm

- Initialize to a volume  $V$  containing the true scene
- Choose a voxel on the current surface
- Project to visible input images
- Carve if not photo-consistent
- Repeat until convergence

## Which shape do you get?



- The **Photo Hull** is the **UNION** of all photo-consistent scenes in  $V$
- It is a photo-consistent scene reconstruction
  - Tightest possible bound on the true scene

## Space Carving Algorithm

### The Basic Algorithm is Unwieldy

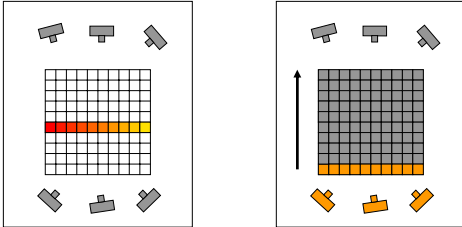
- Complex update procedure

### Alternative: Multi-Pass Plane Sweep

- Efficient, can use texture-mapping hardware
- Converges quickly in practice
- Easy to implement

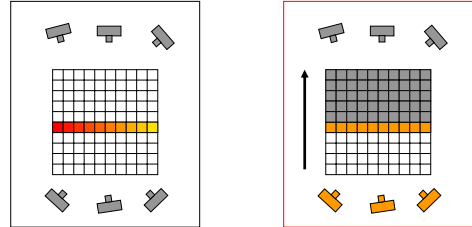
## Multi-Pass Plane Sweep

- Sweep plane in each of 6 principle directions
- Consider cameras on only one side of plane
- Repeat until convergence



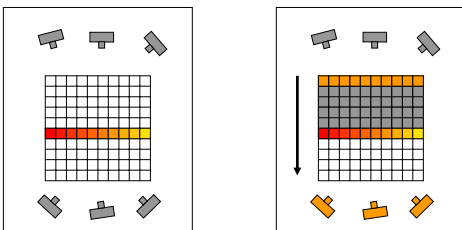
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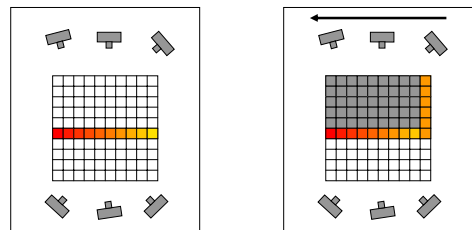
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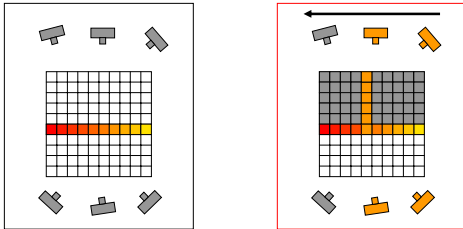
## Multi-Pass Plane Sweep

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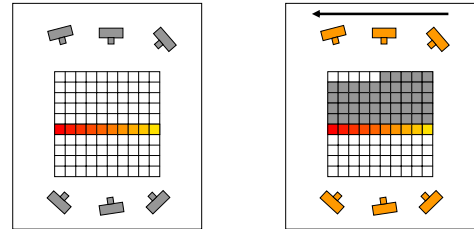
## Multi-Pass Plane Sweep

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## Multi-Pass Plane Sweep

- Sweep plane in each of 6 principle directions
- Consider cameras on only one side of plane
- Repeat until convergence



## Space Carving Results: African Violet



Input Image (1 of 45)



Reconstruction



Reconstruction



Reconstruction

## Space Carving Results: Hand



Input Image  
(1 of 100)



Views of Reconstruction

## Properties of Space Carving

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### Pros

- Voxel coloring version is easy to implement, fast
- Photo-consistent results
- No smoothness prior

### Cons

- Bulging
- No smoothness prior

## Alternatives to space carving

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### Optimizing space carving

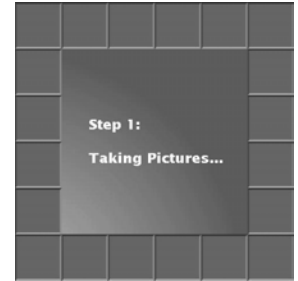
- recent surveys
  - >Slabaugh et al., 2001
  - >Dyer et al., 2001
- many others...

### Graph cuts

- Kolmogorov & Zabih

### Level sets

- introduce smoothness term
- surface represented as an implicit function in 3D volume
- optimize by solving PDE's



## Alternatives to space carving

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### Optimizing space carving

- recent surveys
  - >Slabaugh et al., 2001
  - >Dyer et al., 2001
- many others...

### Graph cuts

- Ramin Zabih's lecture

### Level sets

- introduce smoothness term
- surface represented as an implicit function in 3D volume
- optimize by solving PDE's



## Level sets vs. space carving

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### Advantages of level sets

- optimizes consistency with images + smoothness term
- excellent results for smooth things
- does not require as many images

### Advantages of space carving

- much simpler to implement
- runs faster (orders of magnitude)
- works better for thin structures, discontinuities

### For more info on level set stereo:

- Renaud Keriven's page:
  - > <http://cermics.enpc.fr/~keriven/stereo.html>

## Current/Future Trends

### Optimizing with visibility

- Kolmogorov & Zabih

## Current/Future Trends

### Real-time algorithms

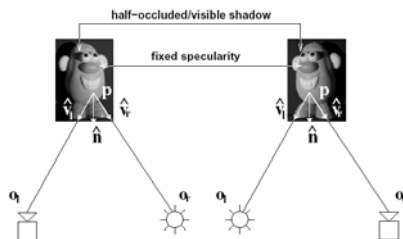
- e.g., Buehler et al., *image-based visual hulls*, SIGGRAPH 2000



## Current/Future Trends

### Modeling shiny things (BRDF's and materials)

- e.g., Zickler et al., *Helmholtz Stereopsis*



## References

### Volume Intersection

- Martin & Aggarwal, "Volumetric description of objects from multiple views", *Trans. Pattern Analysis and Machine Intelligence*, 5(2), 1991, pp. 150-158.
- Szeliski, "Rapid Octree Construction from Image Sequences", *Computer Vision, Graphics, and Image Processing: Image Understanding*, 58(1), 1993, pp. 23-32.
- Matusik, Buehler, Raskar, McMillan, and Gortler, "Image-Based Visual Hulls", *Proc. SIGGRAPH 2000*, pp. 369-374.

### Voxel Coloring and Space Carving

- Seitz & Dyer, "Photorealistic Scene Reconstruction by Voxel Coloring", *Intl. Journal of Computer Vision (IJCV)*, 1999, 35(2), pp. 151-173.
- Kutulakos & Seitz, "A Theory of Shape by Space Carving", *International Journal of Computer Vision*, 2000, 38(3), pp. 199-218.
- **Recent surveys**
  - > Slabaugh, Culbertson, Matzbender, & Schafer, "A Survey of Volumetric Scene Reconstruction Methods from Photographs", *Proc. workshop on Volume Graphics 2001*, pp. 81-100.  
<http://users.ece.gatech.edu/~slabaugh/personal/publications/vg01.pdf>
  - > Dyer, "Volumetric Scene Reconstruction from Multiple Views", *Foundations of Image Understanding*, L. S. Davis, ed., Kluwer, Boston, 2001, 469-489.  
<http://ftp.cs.wisc.edu/computer-vision/repository/PDF/dyer.2001.fia.pdf>

## References

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### Other references from this talk

- **Multibaseline Stereo:** Masatoshi Okutomi and Takeo Kanade. A multiple-baseline stereo. *IEEE Trans. on Pattern Analysis and Machine Intelligence (PAMI)*, 15(4), 1993, pp. 353–363.
- **Level sets:** Faugeras & Keriven, "Variational principles, surface evolution, PDE's, level set methods and the stereo problem", *IEEE Trans. on Image Processing*, 7(3), 1998, pp. 336-344.
- **Mesh based:** Fua & Leclerc, "Object-centered surface reconstruction: Combining multi-image stereo and shading", *IJCV*, 16, 1995, pp. 35-56.
- **3D Room:** Narayanan, Rander, & Kanade, "Constructing Virtual Worlds Using Dense Stereo", *Proc. ICCV*, 1998, pp. 3-10.
- **Graph-based:** Kolmogorov & Zabih, "Multi-Camera Scene Reconstruction via Graph Cuts", *Proc. European Conf. on Computer Vision (ECCV)*, 2002.
- **Helmholtz Stereo:** Zickler, Belhumeur, & Kriegman, "Helmholtz Stereopsis: Exploiting Reciprocity for Surface Reconstruction", *IJCV*, 49(2-3), 2002, pp. 215-227.