Natural Language Processing (CSE 517): Dependency Syntax and Parsing

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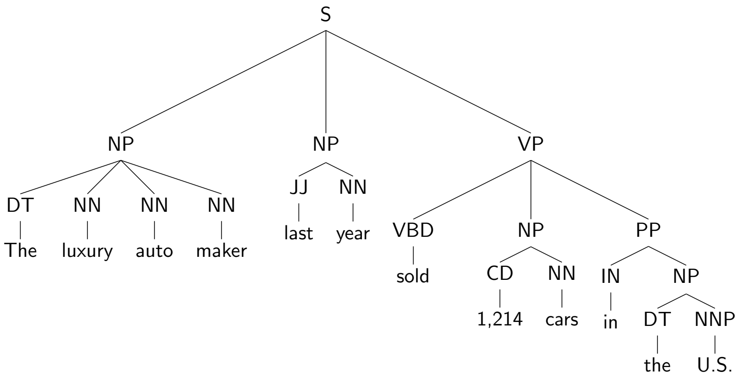
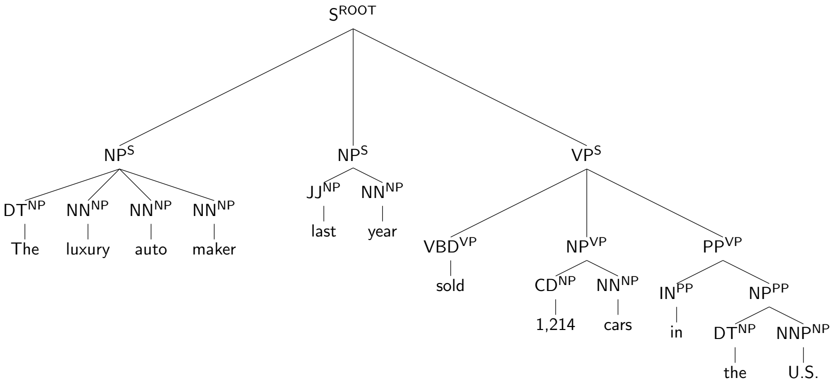
Recap: Phrase Structure



Parent Annotation

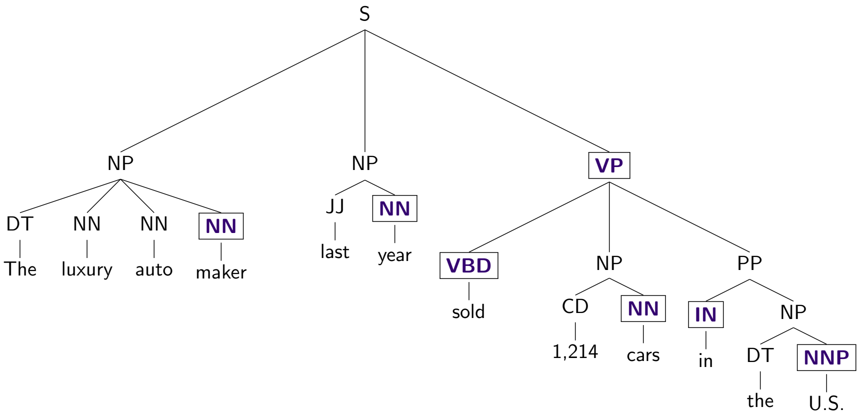
(Johnson, 1998)



Increases the "vertical" Markov order:

$$p(\text{children} \mid \text{parent}, \text{grandparent})$$

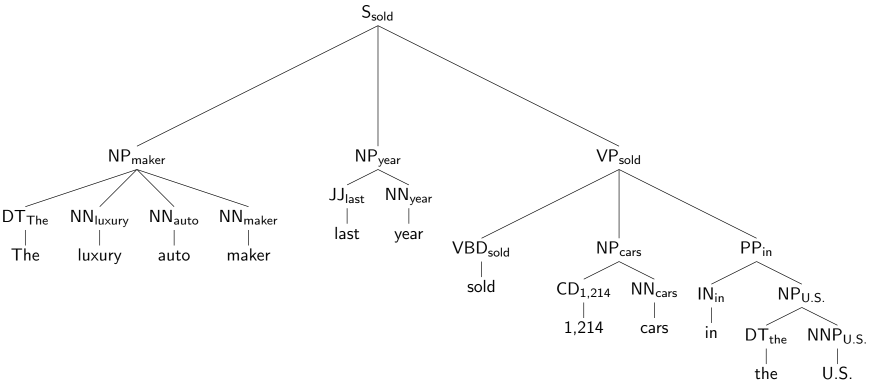
Headedness



Suggests “horizontal” markovization:

$$p(\text{children} \mid \text{parent}) = p(\text{head} \mid \text{parent}) \cdot \prod_i p(i\text{th sibling} \mid \text{head}, \text{parent})$$

Lexicalization



Each node shares a **lexical head** with its head child.

Dependencies

Informally, you can think of **dependency** structures as a transformation of phrase-structures that

- maintains the word-to-word relationships induced by lexicalization,
- adds labels to them, and
- eliminates the phrase categories.

There are also linguistic theories built on dependencies (Tesnière, 1959; Mel'čuk, 1987), as well as treebanks corresponding to those.

- Free(r)-word order languages (e.g., Czech)

Dependency Tree: Definition

Let $\boldsymbol{x} = \langle x_1, \ldots, x_n \rangle$ be a sentence. Add a special ROOT symbol as "x_0."

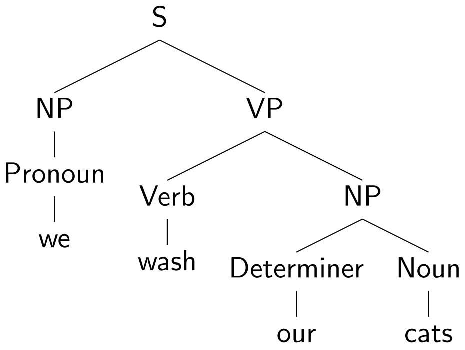
A dependency tree consists of a set of tuples $\langle p, c, \ell \rangle$, where

- $p \in \{0, \ldots, n\}$ is the index of a parent
- $c \in \{1, \ldots, n\}$ is the index of a child
- $\ell \in \mathcal{L}$ is a label

Different annotation schemes define different label sets $\mathcal{L}$, and different constraints on the set of tuples. Most commonly:

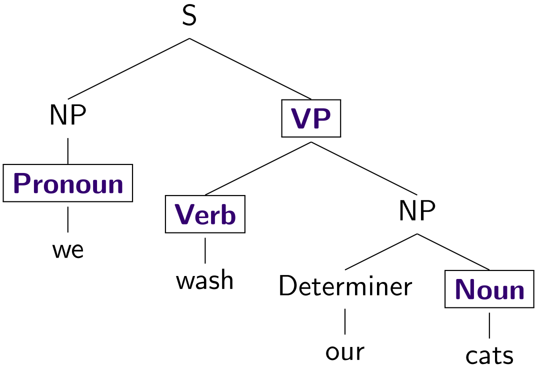
- The tuple is represented as a directed edge from x_p to x_c with label ℓ.
- The directed edges form an arborescence (directed tree) with x_0 as the root (sometimes denoted ROOT).

Example



Phrase-structure tree.

Example



Phrase-structure tree with heads.

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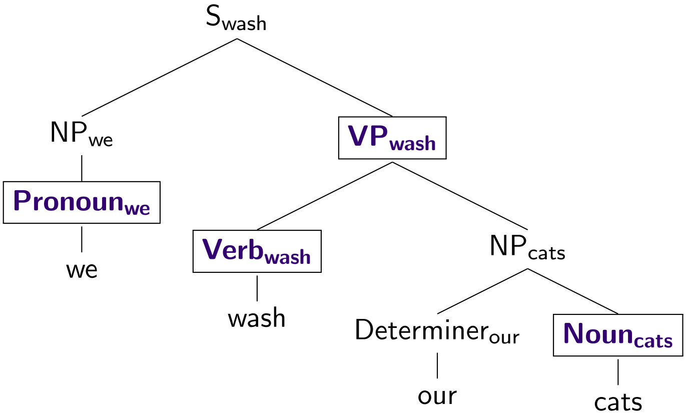
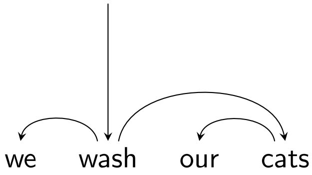


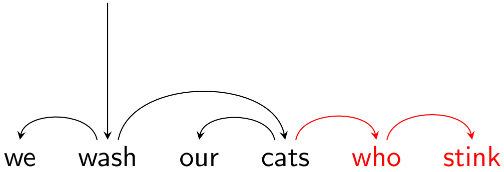
Phrase-structure tree with heads, lexicalized.

Example



“Bare bones” dependency tree.

Example



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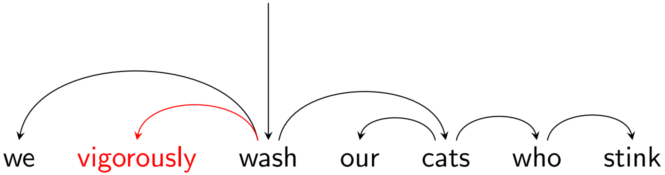
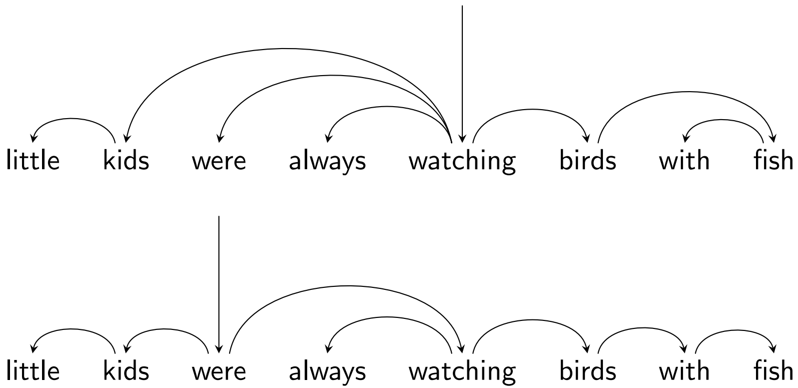
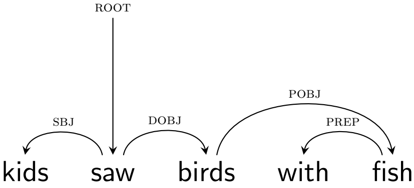


Content Heads vs. Function Heads

Credit: Nathan Schneider



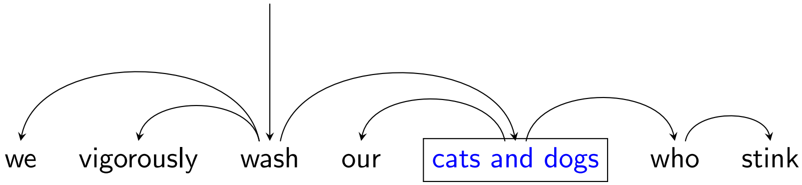
Labels



Key dependency relations captured in the labels include: subject, direct object, preposition object, adjectival modifier, adverbial modifier.

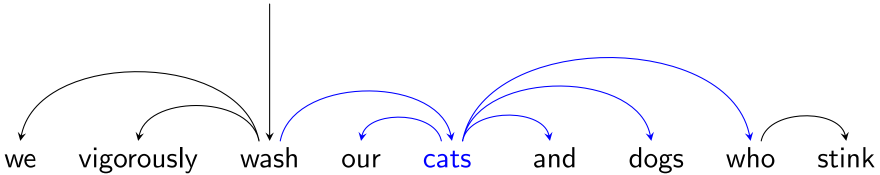
In this lecture, I will mostly not discuss labels, to keep the algorithms simpler.

Coordination Structures



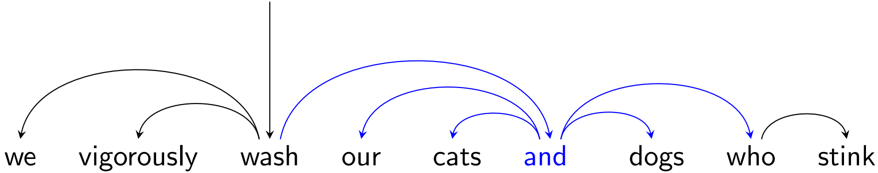
The bugbear of dependency syntax.

Example



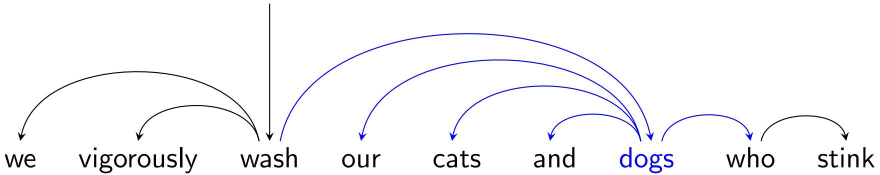
Make the first conjunct the head?

Example



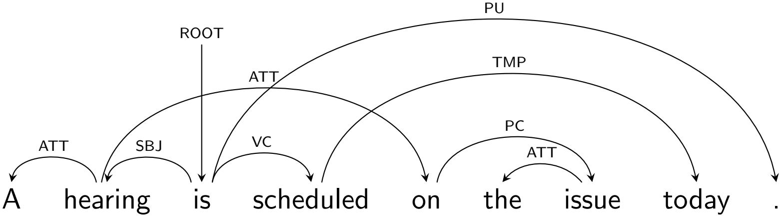
Make the coordinating conjunction the head?

Example



Make the second conjunct the head?

Nonprojective Example



Dependency Schemes

- Direct annotation.
- Transform the treebank: define "head rules" that can select the head child of any node in a phrase-structure tree and label the dependencies.
  - More powerful, less local rule sets, possibly collapsing some words into arc labels.
  - Stanford dependencies are a popular example (de Marneffe et al., 2006).
  - Only results in projective trees.
- Rule based dependencies, followed by manual correction.

Approaches to Dependency Parsing

1. Transition-based parsing with a stack.
2. Chu-Liu-Edmonds algorithm for arborescences (directed graphs).
3. Dynamic programming with the Eisner algorithm.

Transition-Based Parsing

- Dependency tree represented as a linear sequence of **transitions**.

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- Dependency tree represented as a linear sequence of **transitions**.
- Transitions: Simple operations to be executed on a **parser configuration**
- Parser Configuration: stack S and a buffer B.
- During parsing, apply a **classifier** to decide which transition to take next, greedily. No backtracking.

Transition-Based Parsing: Transitions

Parser Configuration:

- Initial Configuration: buffer contains $\boldsymbol{x}$ and the stack contains the ROOT.
- Final Configuration: Empty buffer and the stack contains the entire tree.

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Transitions : "arc-standard" transition set (Nivre, 2004):

- SHIFT the word at the front of the buffer B onto the stack S.
- RIGHT-ARC: $u = \text{pop}(S)$; $v = \text{pop}(S)$; $\text{push}(S, v \rightarrow u)$.
- LEFT-ARC: $u = \text{pop}(S)$; $v = \text{pop}(S)$; $\text{push}(S, v \leftarrow u)$.

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(For labeled parsing, add labels to the RIGHT-ARC and LEFT-ARC transitions.)

Transition-Based Parsing: Example

Buffer B:

we
vigorously
wash
our
cats
who
stink

Stack S:

ROOT

Actions:

Transition-Based Parsing: Example

Buffer B:

vigorously
wash
our
cats
who
stink

Stack S:

we
ROOT

Actions: SHIFT

Transition-Based Parsing: Example

Stack S:

vigorously
we
ROOT

Buffer B:

wash
our
cats
who
stink

Actions: SHIFT SHIFT

Transition-Based Parsing: Example

Stack S:

wash
vigorously
we
ROOT

Buffer B:

our
cats
who
stink

Actions: SHIFT SHIFT SHIFT

Transition-Based Parsing: Example

Stack S:

vigorously wash
we
ROOT

Buffer B:

our
cats
who
stink

Actions: SHIFT SHIFT SHIFT LEFT-ARC

Transition-Based Parsing: Example

Stack S:

we vigorously wash

ROOT

Buffer B:

our
cats
who
stink

Actions: SHIFT SHIFT SHIFT LEFT-ARC LEFT-ARC

Transition-Based Parsing: Example

Stack S:

our
we vigorously wash
ROOT

Buffer B:

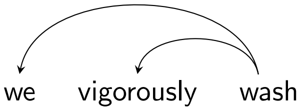
cats
who
stink

Actions: SHIFT SHIFT SHIFT LEFT-ARC LEFT-ARC SHIFT

Transition-Based Parsing: Example

Stack S:

cats
our
we vigorously wash
ROOT



Buffer B:

who
stink

Actions: SHIFT SHIFT SHIFT LEFT-ARC LEFT-ARC SHIFT SHIFT

Transition-Based Parsing: Example

Stack S:

our cats
we vigorously wash
ROOT

Buffer B:

who
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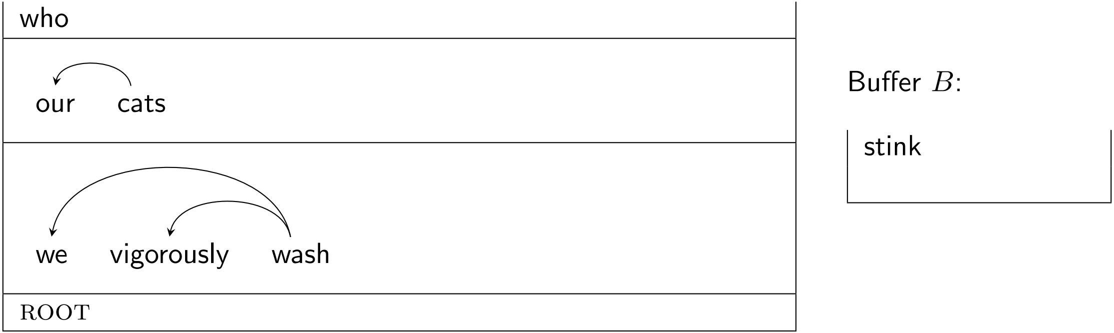
Actions: SHIFT SHIFT SHIFT LEFT-ARC LEFT-ARC SHIFT SHIFT LEFT-ARC

Transition-Based Parsing: Example

Stack S:



Actions: SHIFT SHIFT SHIFT LEFT-ARC LEFT-ARC SHIFT SHIFT LEFT-ARC
SHIFT

Transition-Based Parsing: Example

Stack S:

stink
who
our cats
we vigorously wash
ROOT

Buffer B:

Actions: SHIFT SHIFT SHIFT LEFT-ARC LEFT-ARC SHIFT SHIFT LEFT-ARC SHIFT SHIFT

Transition-Based Parsing: Example

Stack S:

who stink

our cats

we vigorously wash

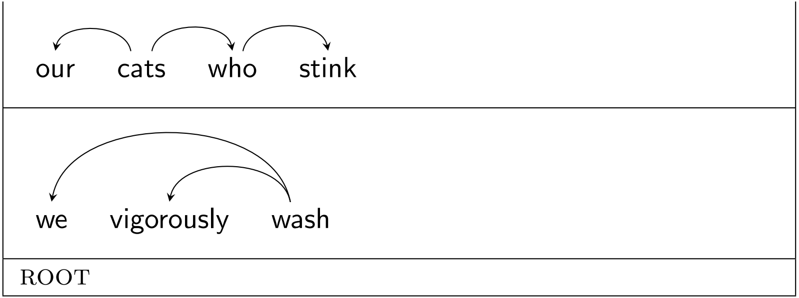
ROOT

Buffer B:

Actions: SHIFT SHIFT SHIFT LEFT-ARC LEFT-ARC SHIFT SHIFT LEFT-ARC SHIFT SHIFT RIGHT-ARC

Transition-Based Parsing: Example

Stack S:



Buffer B:

Actions: SHIFT SHIFT SHIFT LEFT-ARC LEFT-ARC SHIFT SHIFT LEFT-ARC SHIFT SHIFT RIGHT-ARC RIGHT-ARC

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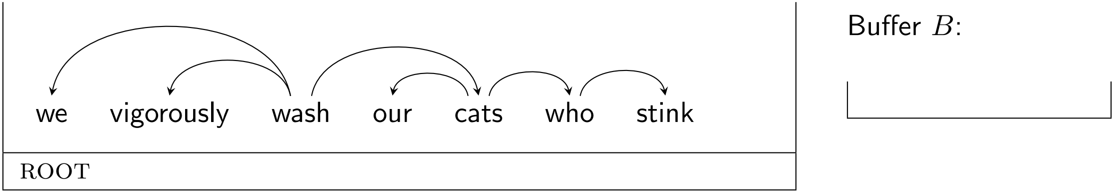

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Transition-Based Parsing: Example

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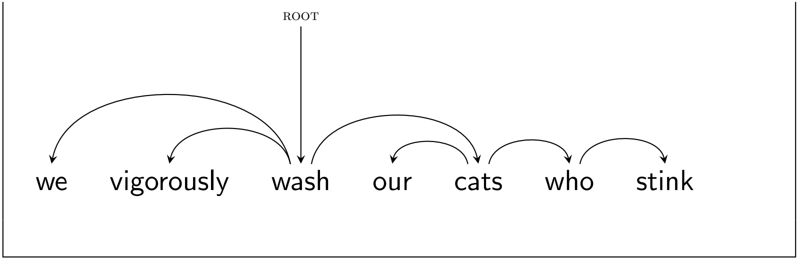

Buffer B:

Actions: SHIFT SHIFT SHIFT LEFT-ARC LEFT-ARC SHIFT SHIFT LEFT-ARC SHIFT SHIFT RIGHT-ARC RIGHT-ARC RIGHT-ARC RIGHT-ARC

The Core of Transition-Based Parsing: Classification

- At each iteration, choose among {SHIFT, RIGHT-ARC, LEFT-ARC}.
  (Actually, among all $\mathcal{L}$-labeled variants of RIGHT- and LEFT-ARC.)

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- Training data: "oracle" transition sequence that gives the right tree converts into $2 \cdot n$ pairs: $\langle$state, correct transition$\rangle$.
- Each word gets SHIFTed once and participates as a child in one ARC. **Linear time.**

Transition-Based Parsing: Remarks

- Can also be applied to phrase-structure parsing (e.g., Sagae and Lavie, 2006). Keyword: "shift-reduce" parsing.
- The algorithm for making decisions doesn't need to be greedy; can maintain multiple hypotheses.
  - E.g., **beam search**, which we'll discuss in the context of machine translation later.
- Potential flaw: the classifier is typically trained under the assumption that previous classification decisions were all *correct*.
  - As yet, no principled solution to this problem, but see "dynamic oracles" (Goldberg and Nivre, 2012).

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Acknowledgment

Slides are mostly adapted from those by Swabha Swayamdipta and Sam Thomson.

Features in Dependency Parsing

For transition-based parsing, we could use any past decisions to score the current decision:

$$s_{\text{global}}(\boldsymbol{y}) = s(\boldsymbol{a}) = \sum_{i=1}^{|\boldsymbol{a}|} s(a_i \mid \boldsymbol{a}_{0:i-1})$$

We gave up on any guarantee of finding the best possible $\boldsymbol{y}$ in favor of arbitrary features.

- For a neural network-based model that fully exploits this, see Dyer et al. (2015).

Graph-Based Dependency Parsing

Selects structures which are globally optimal.

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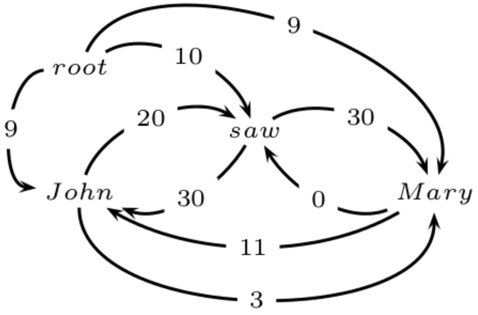
Start with a fully connected graph. Set of $O(n^2)$ edges, E.



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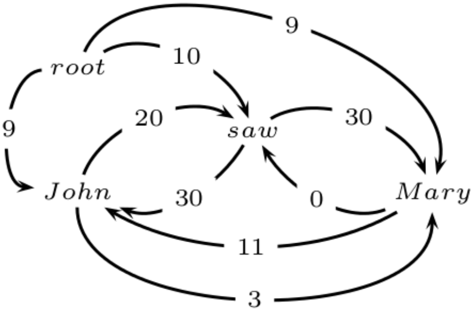

No incoming edges to x_0, ensuring that it will be the root.

First-Order Graph-Based (FOG) Dependency Parsing

(McDonald et al., 2005)

Every possible directed edge e between a parent p and a child c gets a local score, $s(e)$.

$$\boldsymbol{y}^* = \operatorname*{argmax}_{\boldsymbol{y} \subset E} s_{\mathsf{global}}(\boldsymbol{y}) = \operatorname*{argmax}_{\boldsymbol{y} \subset E} \sum_{e \in \boldsymbol{y}} s(e)$$

subject to the constraint that $\boldsymbol{y}$ is an *arborescence*

Classical algorithm to efficiently solve this problem: Chu and Liu (1965), Edmonds (1967)

Chu-Liu-Edmonds Intuitions

- Every non-root node needs exactly one incoming edge.

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High-level view of the algorithm:

1. For every c, pick an incoming edge (i.e., pick a parent)—greedily.
2. If this forms an arborescence, you are done!
3. Otherwise, it's because there's a cycle, C.
    - Arborescences can't have cycles, so some edge in C needs to be kicked out.
    - We also need to find an incoming edge for C.
    - Choosing the incoming edge for C determines which edge to kick out.

Chu-Liu-Edmonds: Recursive (Inefficient) Definition

def maxArborescence(V, E, ROOT):
  # returns best arborescence as a map from each node to its parent
  for c **in** $V \setminus$ ROOT:
    bestInEdge$[c] \leftarrow \text{argmax}_{e \in E : e = \langle p, c \rangle}\, e.s$ # i.e., $s(e)$

    if bestInEdge contains a cycle C:
      # build a new graph where C is contracted into a single node
      $v_C \leftarrow$ **new** Node()
      $V' \leftarrow V \cup \{v_C\} \setminus C$
      $E' \leftarrow \{$adjust(e, v_C) **for** $e \in E \setminus C\}$
      $A \leftarrow$ maxArborescence(V', E', ROOT)
      return $\{e.$original **for** $e \in A\} \cup C \setminus \{A[v_C]$.kicksOut$\}$
  # each node got a parent without creating any cycles
  return bestInEdge

Understanding Chu-Liu-Edmonds

There are two stages:

- **Contraction** (the stuff before the recursive call)
- **Expansion** (the stuff after the recursive call)

Chu-Liu-Edmonds: Contraction

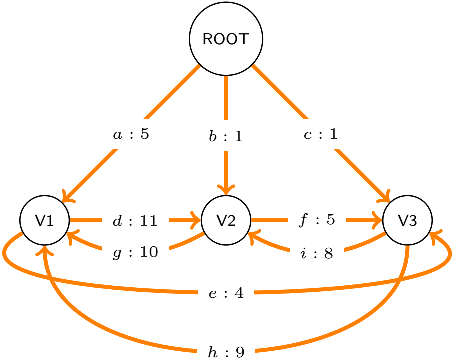
- For each non-ROOT node v, set bestInEdge$[v]$ to be its highest scoring incoming edge.
- If a cycle C is formed:
  - contract the nodes in C into a new node v_C

  adjust subroutine on next slide performs the following:
  - Edges incoming to any node in C now get destination v_C
  - For each node v in C, and for each edge e incoming to v from outside of C:
    - Set e.kicksOut to bestInEdge[v], and
    - Set $e.s$ to be $e.s - e$.kicksOut$.s$
  - Edges outgoing from any node in C now get source v_C
- Repeat until every non-ROOT node has an incoming edge and no cycles are formed

Chu-Liu-Edmonds: Edge Adjustment Subroutine

```
def adjust(e, v_C):
    e' ← copy(e)
    e'.original ← e
    if e.dest ∈ C:
        e'.dest ← v_C
        e'.kicksOut ← bestInEdge[e.dest]
        e'.s ← e.s − e'.kicksOut.s
    elif e.src ∈ C:
        e'.src ← v_C
    return e'
```

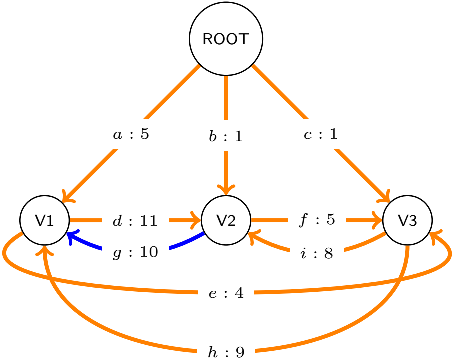
Contraction Example



	bestInEdge
V1	
V2	
V3	

	kicksOut
a	
b	
c	
d	
e	
f	
g	
h	
i	

Contraction Example



	bestInEdge
V1	g
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a	
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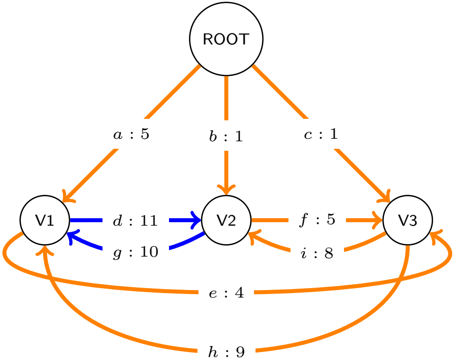

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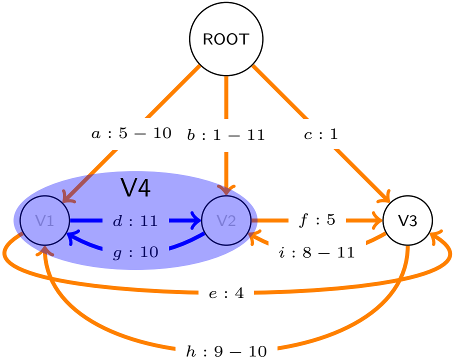

	bestInEdge
V1	g
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V3	

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a	g
b	d
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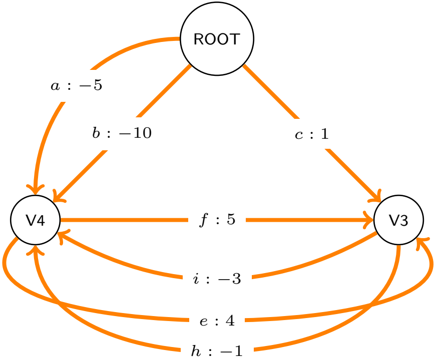

	bestInEdge
V1	g
V2	d
V3	
V4	

	kicksOut
a	g
b	d
c	
d	
e	
f	
g	
h	g
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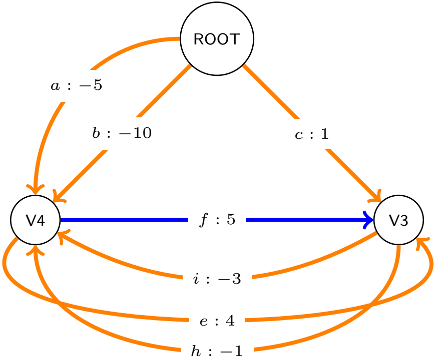
Contraction Example



	bestInEdge
V1	g
V2	d
V3	f
V4	

	kicksOut
a	g
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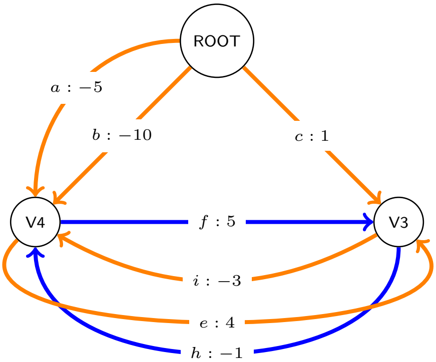

	bestInEdge
V1	g
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	kicksOut
a	g
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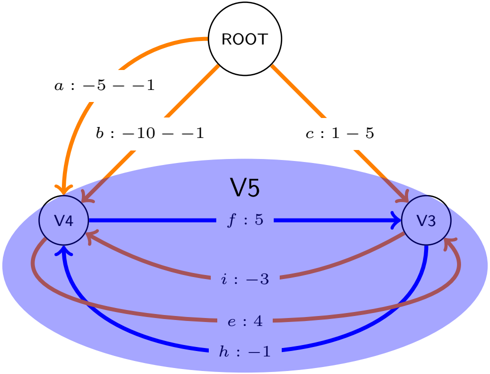
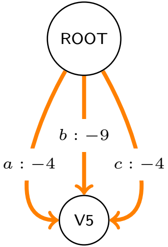


	bestInEdge
V1	g
V2	d
V3	f
V4	h
V5	

	kicksOut
a	g, h
b	d, h
c	f
d	
e	
f	
g	
h	g
i	d

Contraction Example



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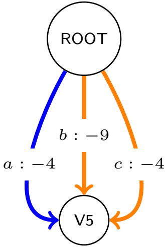

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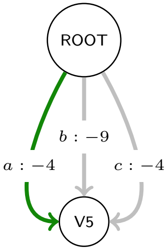
Chu-Liu-Edmonds: Expansion

After the contraction stage, every contracted node will have exactly one `bestInEdge`. This edge will kick out one edge inside the contracted node, breaking the cycle.

- Go through each `bestInEdge` e in the *reverse* order that we added them
- Lock down e, and remove every edge in `kicksOut`(e) from `bestInEdge`.

Expansion Example



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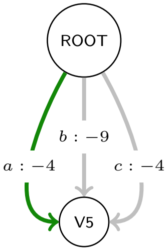

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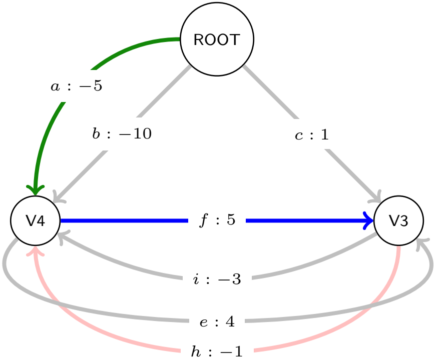

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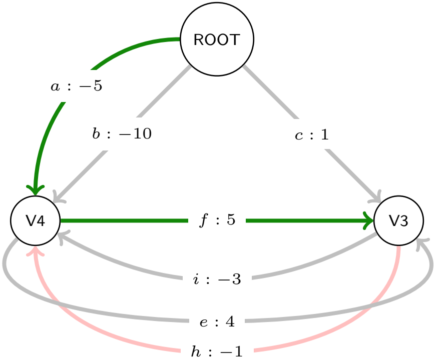

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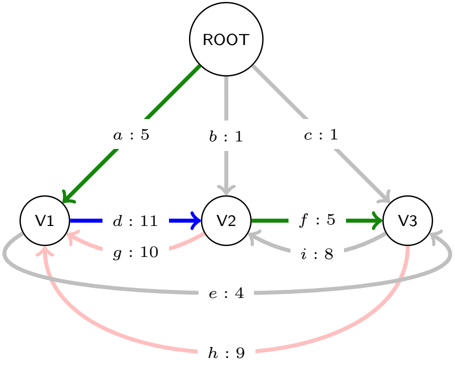

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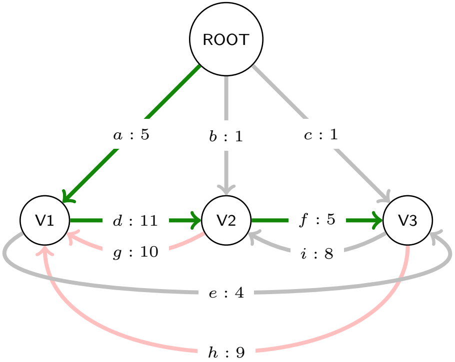

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Observation

The set of arborescences strictly includes the set of projective dependency trees.

Is this a good thing or a bad thing?

Chu-Liu-Edmonds: Notes

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- CLE is exact: it always recovers an optimal arborescence.
- What about labeled dependencies?
  - As a matter of preprocessing, for each $\langle p, c \rangle$, keep only the top-scoring labeled edge.
- Tarjan (1977) offered a more efficient, but unfortunately incorrect, implementation.
  Camerini et al. (1979) corrected it.
  The approach is not recursive; instead using a disjoint set data structure to keep track of collapsed nodes.
  Even better: Gabow et al. (1986) used a Fibonacci heap to keep incoming edges sorted, and finds cycles in a more sensible way. Also constrains root to have only one outgoing edge.
  With these tricks, $O(n^2 + n \log n)$ **runtime.**

More Details on Statistical Dependency Parsing

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- What about higher-order parsing? Requires approximate inference, e.g., dual decomposition (Martins et al., 2013).

Important Tradeoffs (and Not Just in NLP)

1. Two extremes:
   - Specialized algorithm that efficiently solves your problem, under your assumptions. E.g., Chu-Liu-Edmonds for FOG dependency parsing.
   - General-purpose method that solves many problems, allowing you to test the effect of different assumptions. E.g., dynamic programming, transition-based methods, some forms of approximate inference.

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2. Two extremes:
   - Fast (linear-time) but greedy
   - Model-optimal but slow
     - Dirty secret: the best way to get (English) dependency trees is to run phrase-structure parsing, then convert.

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