Natural Language Processing (CSE 517): Neural Language Models

Noah Smith

University of Washington
nasmith@cs.washington.edu

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Quick Review

A language model is a probability distribution over $\mathcal{V}^\dagger$.

Typically p decomposes into probabilities $p(x_i \mid \boldsymbol{h}_i)$.

- n-gram: $\boldsymbol{h}_i$ is $(\mathsf{n}-1)$ previous symbols
- class-based: further decomposition $p(x_i \mid \mathsf{cl}(x_i)) \cdot p(\mathsf{cl}(x_i) \mid \boldsymbol{h}_i)$
  - previous $(\mathsf{n}-1)$ symbols' *classes* predict class of x_i
  - class of x_i predicts x_i
- log-linear: featurized representation of $\langle \boldsymbol{h}_i, x_i \rangle$

Today: neural language models

Neural Network: Definitions

Warning: there is no widely accepted standard notation!

A feedforward neural network $n_{\boldsymbol{\nu}}$ is defined by:

- A function family that maps parameter values to functions of the form $n : \mathbb{R}^{d_{in}} \to \mathbb{R}^{d_{out}}$; typically:
  - Non-linear
  - Differentiable with respect to its inputs
  - "Assembled" through a series of affine transformations and non-linearities, composed together
  - Symbolic inputs handled through lookups.
- Parameter values $\boldsymbol{\nu}$
  - Typically a collection of scalars, vectors, and matrices
  - We often assume they are linearized into $\mathbb{R}^D$

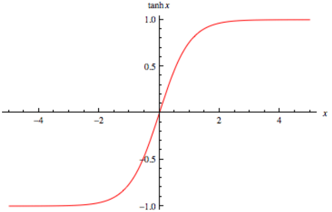
A Couple of Useful Functions

- $\text{softmax} : \mathbb{R}^k \to \mathbb{R}^k$

$$\langle x_1, x_2, \ldots, x_k \rangle \mapsto \left\langle \frac{e^{x_1}}{\sum_{j=1}^{k} e^{x_j}}, \frac{e^{x_2}}{\sum_{j=1}^{k} e^{x_j}}, \ldots, \frac{e^{x_k}}{\sum_{j=1}^{k} e^{x_j}} \right\rangle$$

- $\tanh : \mathbb{R} \to [-1, 1]$

$$x \mapsto \frac{e^x - e^{-x}}{e^x + e^{-x}}$$



Generalized to be *elementwise*, so that it maps $\mathbb{R}^k \to [-1, 1]^k$.

- Others include: ReLUs, logistic sigmoids, PReLUs, ...

Feedforward Neural Network Language Model

(Bengio et al., 2003)

Define the n-gram probability as follows:

$$p(\cdot \mid \langle h_1, \ldots, h_{\mathsf{n}-1} \rangle) = n_{\boldsymbol{\nu}}\left(\langle \mathbf{e}_{h_1}, \ldots, \mathbf{e}_{h_{\mathsf{n}-1}} \rangle\right) =$$

$$\operatorname{softmax}\left(\underset{V}{\mathbf{b}} + \sum_{j=1}^{\mathsf{n}-1} \underset{V}{\mathbf{e}_{h_j}}^{\top} \underset{V \times d}{\mathbf{V}} \underset{d \times V}{\mathbf{A}_{j,*,*}} + \underset{V \times H}{\mathbf{W}} \tanh\left(\underset{H}{\mathbf{u}} + \sum_{j=1}^{\mathsf{n}-1} \mathbf{e}_{h_j}^{\top} \mathbf{V} \underset{d \times H}{\mathbf{T}_{j,*,*}} \right) \right)$$

where each $\mathbf{e}_* \in \mathbb{R}^V$ is a one-hot vector and H is the number of "hidden units" in the neural network (a "hyperparameter").

Parameters $\boldsymbol{\nu}$ include:

- $\mathbf{V} \in \mathbb{R}^{V \times d}$, which are called "embeddings" (row vectors), one for every word in $\mathcal{V}$
- Feedforward NN parameters $\mathbf{b} \in \mathbb{R}^V$, $\mathbf{A} \in \mathbb{R}^{(\mathsf{n}-1) \times d \times V}$, $\mathbf{W} \in \mathbb{R}^{V \times H}$, $\mathbf{u} \in \mathbb{R}^H$, $\mathbf{T} \in \mathbb{R}^{(\mathsf{n}-1) \times d \times H}$

Breaking It Down

Look up each of the history words $h_j, \forall j \in \{1, \ldots, \mathsf{n} - 1\}$ in $\mathbf{V}$; keep two copies.

$$\underset{V}{\mathbf{e}_{h_j}}^\top \underset{V \times d}{\mathbf{V}}$$

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Breaking It Down

Look up each of the history words $h_j, \forall j \in \{1, \ldots, \mathsf{n} - 1\}$ in $\mathbf{V}$; keep two copies. Rename the embedding for h_j as $\mathbf{v}_{h_j}$.

$$\mathbf{e}_{h_j}{}^\top \mathbf{V} = \mathbf{v}_{h_j}$$

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Breaking It Down

Apply an affine transformation to the second copy of the history-word embeddings ($\mathbf{u}$, $\mathbf{T}$)

$$\mathbf{v}_{h_j}$$

$$\underset{H}{\mathbf{u}} + \sum_{j=1}^{\mathsf{n}-1} \mathbf{v}_{h_j} \underset{d \times H}{\mathbf{T}_{j,*,*}}$$

Breaking It Down

Apply an affine transformation to the second copy of the history-word embeddings ($\mathbf{u}$, $\mathbf{T}$) and a $\tanh$ nonlinearity.

$$\mathbf{v}_{h_j}$$

$$\tanh\left(\mathbf{u} + \sum_{j=1}^{\mathsf{n}-1} \mathbf{v}_{h_j} \, \mathbf{T}_{j,*,*} \right)$$

Breaking It Down

Apply an affine transformation to everything ($\mathbf{b}$, $\mathbf{A}$, $\mathbf{W}$).

$$\underset{V}{\mathbf{b}} + \sum_{j=1}^{\mathsf{n}-1} \mathbf{v}_{h_j} \underset{d \times V}{\mathbf{A}_{j,*,*}}$$
$$+ \underset{V \times H}{\mathbf{W}} \tanh\left(\mathbf{u} + \sum_{j=1}^{\mathsf{n}-1} \mathbf{v}_{h_j} \mathbf{T}_{j,*,*} \right)$$

Breaking It Down

Apply a softmax transformation to make the vector sum to one.

$$\mathrm{softmax}\left(\mathbf{b} + \sum_{j=1}^{\mathsf{n}-1} \mathbf{v}_{h_j}\ \mathbf{A}_{j,*,*} \right.$$
$$\left. + \mathbf{W}\ \tanh\left(\mathbf{u} + \sum_{j=1}^{\mathsf{n}-1} \mathbf{v}_{h_j}\ \mathbf{T}_{j,*,*} \right) \right)$$

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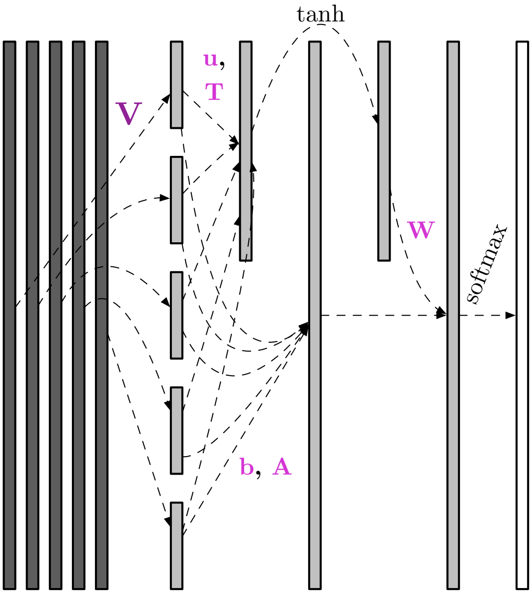
Like a log-linear language model with two kinds of features:

- Concatenation of context-word embeddings vectors $\mathbf{v}_{h_*}$
- $\tanh$-affine transformation of the above

New parameters arise from (i) embeddings and (ii) affine transformation "inside" the nonlinearity.

Visualization



Number of Parameters

$$D = \underbrace{Vd}_{\mathbf{V}} + \underbrace{V}_{\mathbf{b}} + \underbrace{(\mathsf{n}-1)dV}_{\mathbf{A}} + \underbrace{VH}_{\mathbf{W}} + \underbrace{H}_{\mathbf{u}} + \underbrace{(\mathsf{n}-1)dH}_{\mathbf{T}}$$

For Bengio et al. (2003):

- $V \approx 18000$ (after OOV processing)
- $d \in \{30, 60\}$
- $H \in \{50, 100\}$
- $\mathsf{n} - 1 = 5$

So $D = 461V + 30100$ parameters, compared to $O(V^{\mathsf{n}})$ for classical n-gram models.

- Forcing $\mathbf{A} = \mathbf{0}$ eliminated $300V$ parameters and performed a bit better, but was slower to converge.
- If we averaged $\mathbf{v}_{h_*}$ instead of concatenating, we'd get to $221V + 6100$ (this is a variant of "continuous bag of words," Mikolov et al., 2013).

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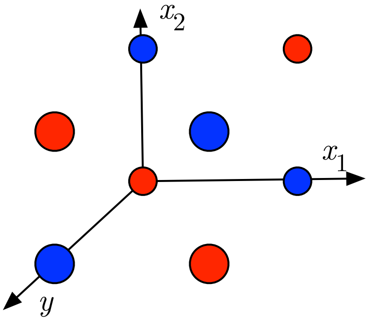
XOR Example



Correct tuples are marked in red; incorrect tuples are marked in blue.

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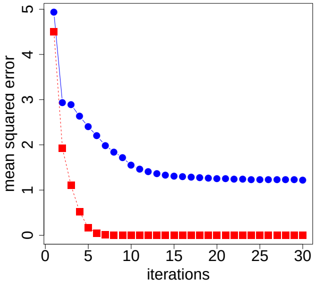
  - Suppose $y = \mathrm{xor}(x_1, x_2)$; this can't be expressed as a linear function of x_1 and x_2. But:

$$z = x_1 \cdot x_2$$
$$y = x_1 + x_2 - 2z$$

xor Example ($D = 13$)

Credit: Chris Dyer (`https://github.com/clab/cnn/blob/master/examples/xor.cc`)



$$\min_{\mathbf{v},a,\mathbf{W},\mathbf{b}} \sum_{x_1 \in \{0,1\}} \sum_{x_2 \in \{0,1\}} \left(\mathrm{xor}(x_1, x_2) - \underset{3}{\mathbf{v}}^\top \left(\underset{3 \times 2}{\mathbf{W}} \underset{2}{\mathbf{x}} + \underset{3}{\mathbf{b}} \right) + a \right)^2$$

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- Modern answer: representations of words and histories are tuned to the prediction problem.
- Word embeddings: a powerful idea ...

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- Deerwester et al. (1990) explored dimensionality reduction techniques for information retrieval-style querying of text collections.
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  - Why "semantics"?

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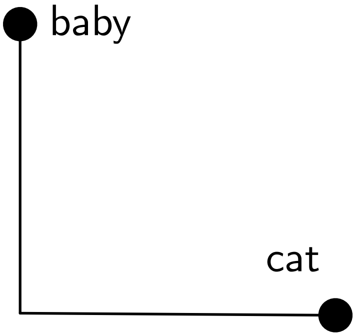
  - Why "semantics"?
- Something like this also turns up in traditional linguistic theories, e.g., marking nouns as "animate" or not.

Words as Vectors: Example



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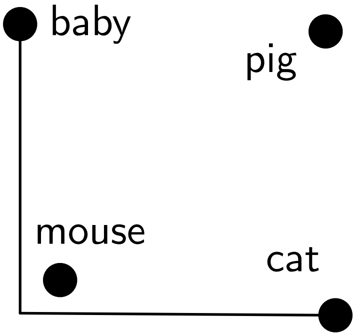

Parameter Estimation

Bad news for neural language models:

- Log-likelihood function is not convex.
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Good news:

- $\nu_{\boldsymbol{\nu}}$ is differentiable with respect to $\mathbf{V}$ (from which its inputs come) and $\boldsymbol{\nu}$ (its parameters), so gradient-based methods are available.

Lots more details in Bengio et al. (2003) and (for NNs more generally) in Goldberg (2015).

What's Coming Up

- The log-bilinear language model
- Recurrent neural network language models

Log-Bilinear Language Model

(Mnih and Hinton, 2007)

Define the n-gram probability as follows, for each $v \in \mathcal{V}$:

$$p(v \mid \langle h_1, \ldots, h_{\mathsf{n}-1} \rangle) = \frac{\exp\left(\sum_{j=1}^{\mathsf{n}-1} \left(\underbrace{\mathbf{v}_{h_j}}_{d}{}^{\top} \underbrace{\mathbf{A}_{j,*,*}}_{d \times d} + \underbrace{\mathbf{b}}_{d}{}^{\top} \right) \underbrace{\mathbf{v}_v}_{d} + c_v \right)}{\sum_{v' \in \mathcal{V}} \exp\left(\sum_{j=1}^{\mathsf{n}-1} \left(\underbrace{\mathbf{v}_{h_j}}_{d}{}^{\top} \underbrace{\mathbf{A}_{j,*,*}}_{d \times d} + \underbrace{\mathbf{b}}_{d}{}^{\top} \right) \underbrace{\mathbf{v}_{v'}}_{d} + c_v \right)}$$

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- Training this model involves a sum over the vocabulary (like log-linear models we saw last time).
- Later work explored variations to make learning faster (related to class-based models we saw earlier).

Observations about Neural Language Models (So Far)

- There's no knowledge built in that the most recent word $h_{\mathsf{n}-1}$ should generally be more informative than earlier ones.
  - This has to be learned.
- In addition to choosing n, also have to choose dimensionalities like d and H.
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- Parameters of these models are hard to interpret.
  - Example: ℓ_2-norm of $\mathbf{A}_{j,*,*}$ and $\mathbf{T}_{j,*,*}$ in the feedforward model correspond to the importance of history position j.
  - Individual word embeddings can be clustered and dimensions can be analyzed (e.g., Tsvetkov et al., 2015).
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Recurrent Neural Network

- Each input element is understood to be an element of a sequence: $\langle \mathbf{x}_1, \mathbf{x}_2, \ldots, \mathbf{x}_\ell \rangle$
- At each timestep t:
  - The tth input element $\mathbf{x}_t$ is processed alongside the previous state $\mathbf{s}_{t-1}$ to calculate the new **state** ($\mathbf{s}_t$).
  - The tth output is a function of the state $\mathbf{s}_t$.
  - The *same functions* are applied at each iteration:

$$\begin{aligned}\mathbf{s}_t &= f_{\text{recurrent}}(\mathbf{x}_t, \mathbf{s}_{t-1}) \\ \mathbf{y}_t &= f_{\text{output}}(\mathbf{s}_t)\end{aligned}$$

In RNN language models, words *and* histories are represented as vectors (respectively, $\mathbf{x}_t = \mathbf{e}_{x_t}$ and $\mathbf{s}_t$).

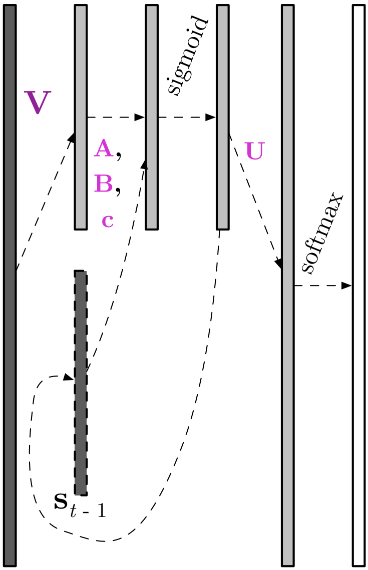
RNN Language Model

The original version, by Mikolov et al. (2010) used a "simple" RNN architecture along these lines:

$$
\begin{aligned}
\mathbf{s}_t = f_{\text{recurrent}}(\mathbf{e}_{x_t}, \mathbf{s}_{t-1}) &= \text{sigmoid}\left(\left(\mathbf{e}_{x_t}^\top \mathbf{V}\right)^\top \mathbf{A} + \mathbf{s}_{t-1}^\top \mathbf{B} + \mathbf{c}\right) \\
\mathbf{y}_t = f_{\text{output}}(\mathbf{s}_t) &= \text{softmax}\left(\mathbf{s}_t^\top \mathbf{U}\right) \\
p(v \mid x_1, \ldots, x_{t-1}) &= [\mathbf{y}_t]_v
\end{aligned}
$$

Note: this is *not* an n-gram (Markov) model!

Visualization



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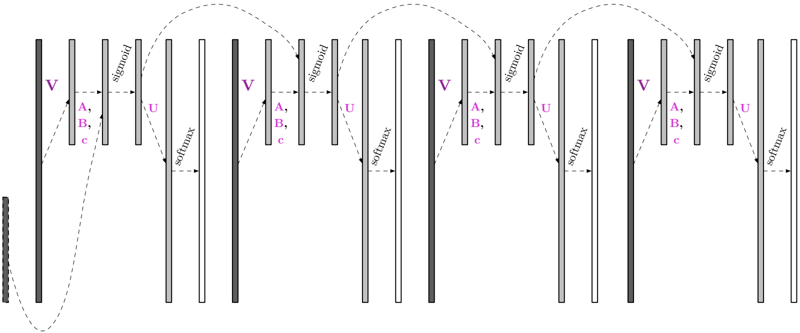

Improvements to RNN Language Models

The simple RNN is known to suffer from two related problems:

- "Vanishing gradients" during learning make it hard to propagate error into the distant past.
- State tends to change a lot on each iteration; the model "forgets" too much.

Some variants:

- "Stacking" these functions to make deeper networks.
- Sundermeyer et al. (2012) use "long short-term memories" (LSTMs) and Cho et al. (2014) use "gated recurrent units" (GRUs) to define $f_{\text{recurrent}}$.
- Mikolov et al. (2014) engineer the linear transformation in the simple RNN for better preservation.
- Jozefowicz et al. (2015) used randomized search to find even better architectures.

Comparison: Probabilistic vs. Connectionist Modeling

	Probabilistic	**Connectionist**
What do we engineer?	features, assumptions	architectures
Theory?	as N gets large	not really
Interpretation of parameters?	often easy	usually hard

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2003–2010		embedded vector
since 2010	unrestricted	embedded

- Next, we'll let go of the text-as-sequence idea and think about probabilistic models relating a word and its **cotext** (textual context).

Readings and Reminders

- Goldberg (2015), §0–4 and §10–13
- Possibly also useful (but not yet examined by me): Cho (2015)
- Submit a suggestion for an exam question by Friday at 5pm.

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