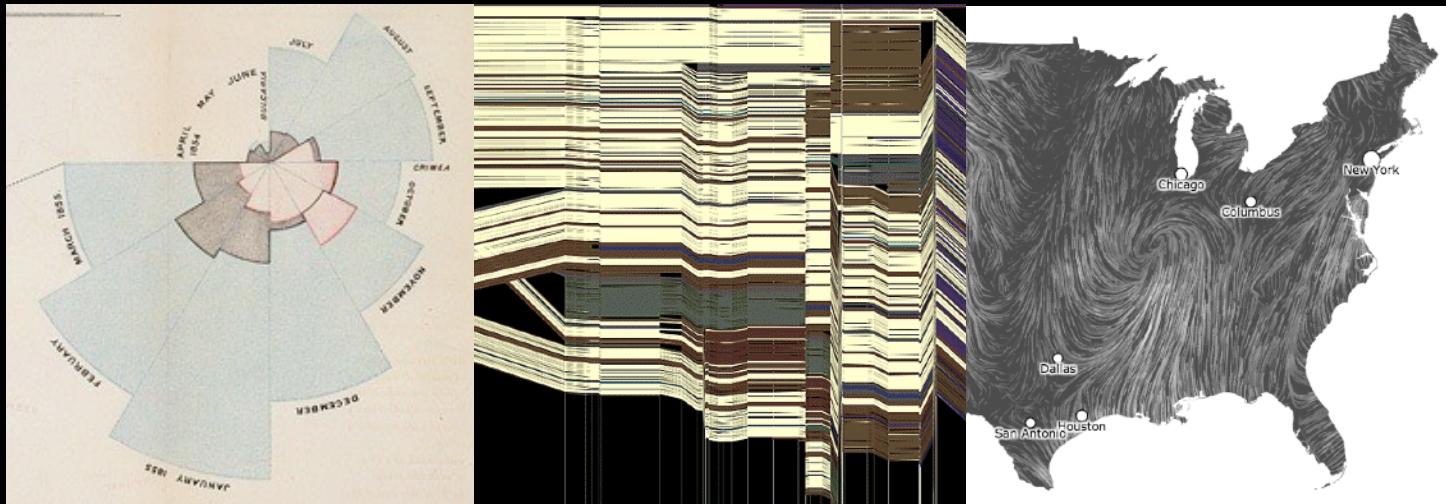


CSE 512 - Data Visualization

# Visual Encoding



Jeffrey Heer University of Washington

# The Big Picture

task

questions, goals  
assumptions

data

physical data type  
conceptual data type

domain

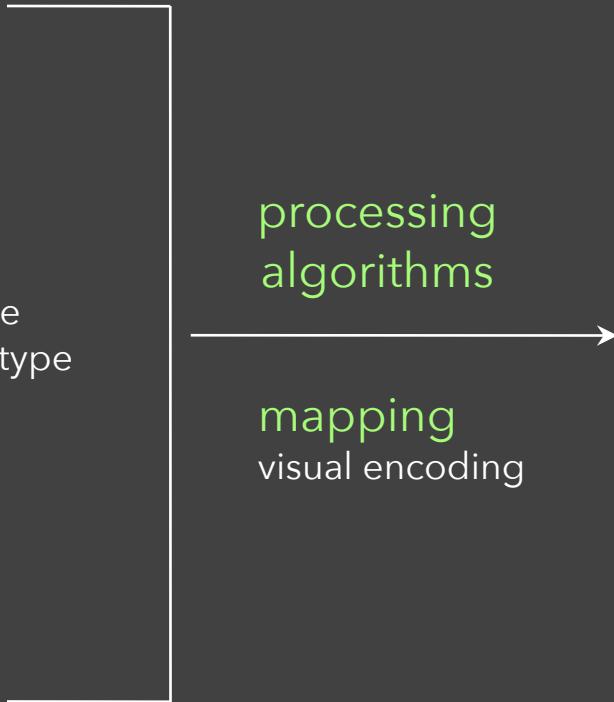
metadata  
semantics  
conventions

processing  
algorithms

mapping  
visual encoding

image

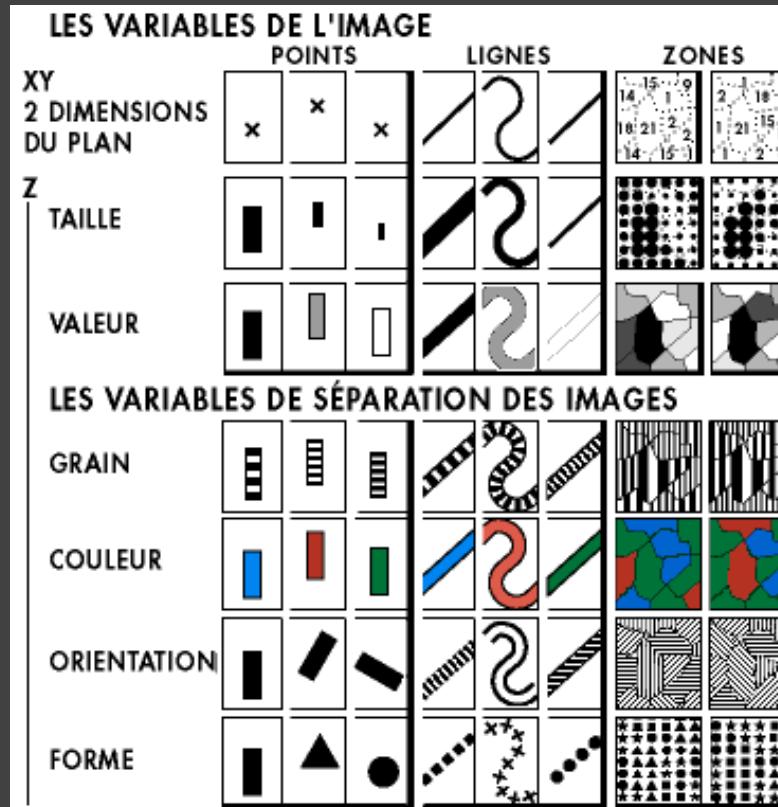
visual channel  
graphical marks



# Formalizing Design

# Which Channel to Use?

Position (x 2)  
Size  
Value  
Texture  
Color  
Orientation  
Shape



# Choosing Visual Encodings

Assume  $k$  visual encodings and  $n$  data attributes.

We would like to pick the “best” encoding among a combinatorial set of possibilities of size  $(n+1)^k$

## **Principle of Consistency**

The properties of the image (visual variables) should match the properties of the data.

## **Principle of Importance Ordering**

Encode the most important information in the most effective way.

# Bertin's Levels of Organization

Position	<table border="1"><tr><td>N</td><td>O</td><td>Q</td></tr></table>	N	O	Q	<b>Nominal</b>
N	O	Q			
Size	<table border="1"><tr><td>N</td><td>O</td><td>Q</td></tr></table>	N	O	Q	<b>Ordinal</b>
N	O	Q			
Value	<table border="1"><tr><td>N</td><td>O</td><td>Q</td></tr></table>	N	O	Q	<b>Quantitative</b> Note: <b>Q</b> ⊂ <b>O</b> ⊂ <b>N</b>
N	O	Q			
Texture	<table border="1"><tr><td>N</td><td>o</td><td></td></tr></table>	N	o		
N	o				
Color	<table border="1"><tr><td>N</td><td></td><td></td></tr></table>	N			
N					
Orientation	<table border="1"><tr><td>N</td><td></td><td></td></tr></table>	N			
N					
Shape	<table border="1"><tr><td>N</td><td></td><td></td></tr></table>	N			
N					

# Information in Hue and Lightness

Lightness ("value") is perceived as ordered

∴ Encode ordinal variables (O)



∴ Encode continuous variables (Q) [not as well]



Hue is normally perceived as unordered

∴ Encode nominal variables (N) using color



# Design Criteria [Mackinlay 86]

## Expressiveness

A set of facts is *expressible* in a visual language if the sentences (i.e. the visualizations) in the language express all the facts in the set of data, and only the facts in the data.

## Effectiveness

A visualization is more *effective* than another visualization if the information conveyed by one visualization is more readily perceived than the information in the other visualization.

# Design Criteria [Mackinlay 86]

## Expressiveness

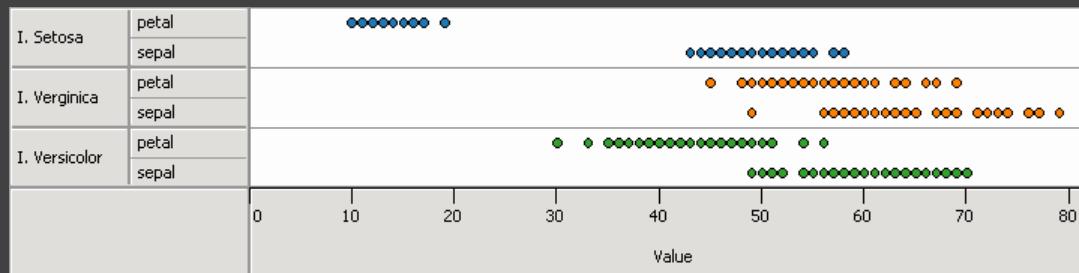
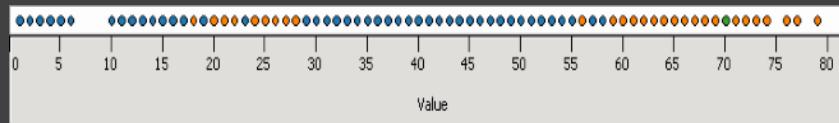
A set of facts is *expressible* in a visual language if the sentences (i.e. the visualizations) in the language express all the facts in the set of data, and only the facts in the data.

## Effectiveness

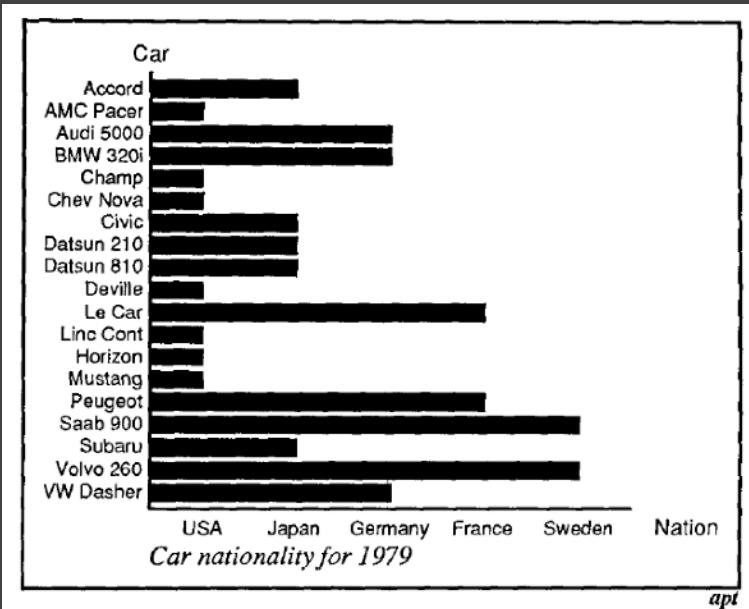
A visualization is more *effective* than another visualization if the information conveyed by one visualization is more readily perceived than the information in the other visualization.

# Can not express the facts

A multivariate relation may be *inexpressive* in a single horizontal dot plot because multiple records are mapped to the same position.



# Expresses facts not in the data



A length is interpreted as a quantitative value.

# Design Criteria [Mackinlay 86]

## Expressiveness

A set of facts is *expressible* in a visual language if the sentences (i.e. the visualizations) in the language express all the facts in the set of data, and only the facts in the data.

## Effectiveness

A visualization is more *effective* than another visualization if the information conveyed by one visualization is more readily perceived than the information in the other visualization.

# Design Criteria [Mackinlay 86]

## Expressiveness

A set of facts is *expressible* in a visual language if the sentences (i.e. the visualizations) in the language express all the facts in the set of data, and only the facts in the data.

## Effectiveness

A visualization is more *effective* than another visualization if the information conveyed by one visualization is more readily perceived than the information in the other visualization.

# **Design Criteria *Translated***

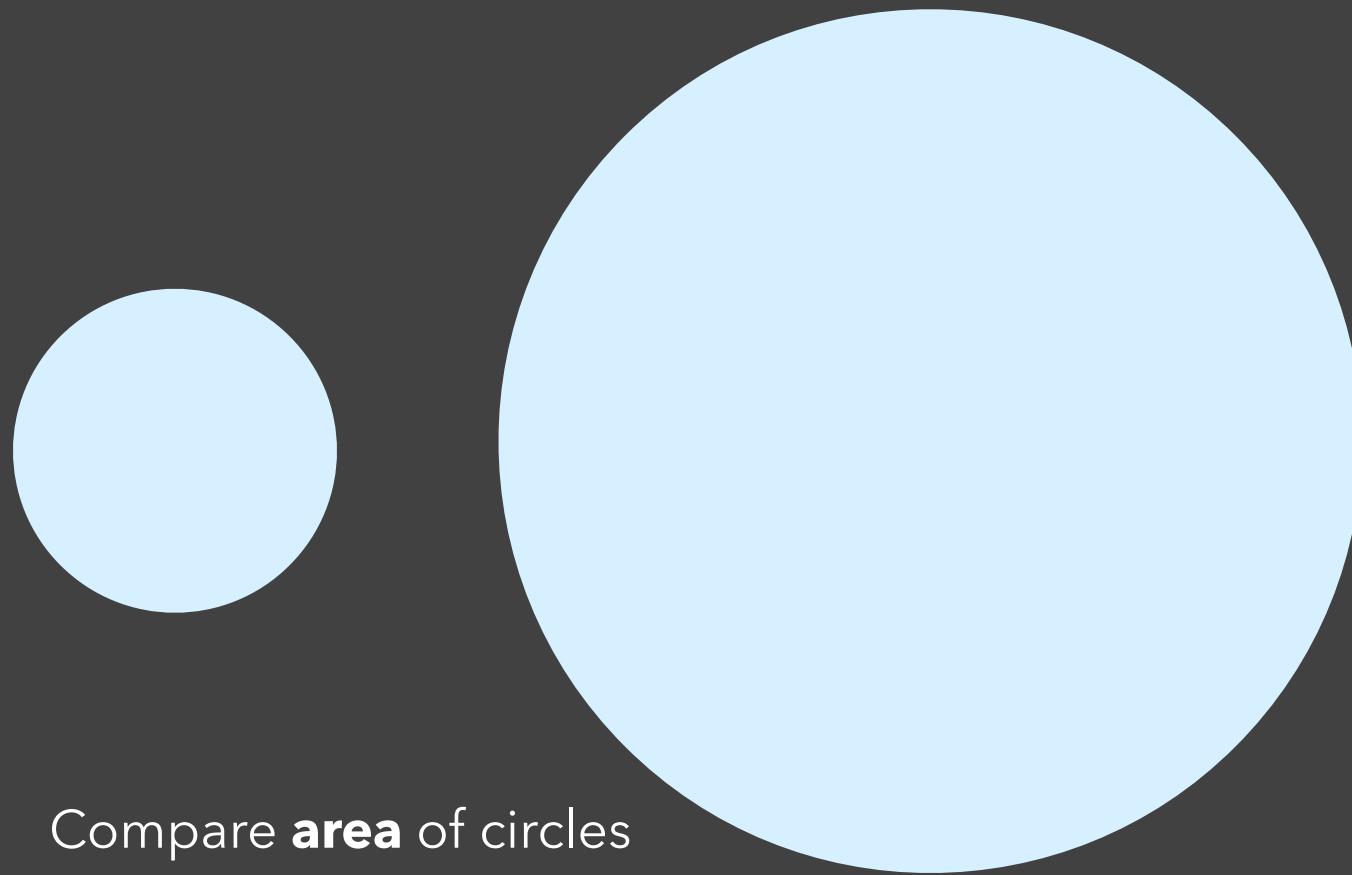
**Tell the truth and nothing but the truth**

(don't lie, and don't lie by omission)

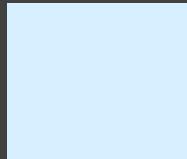
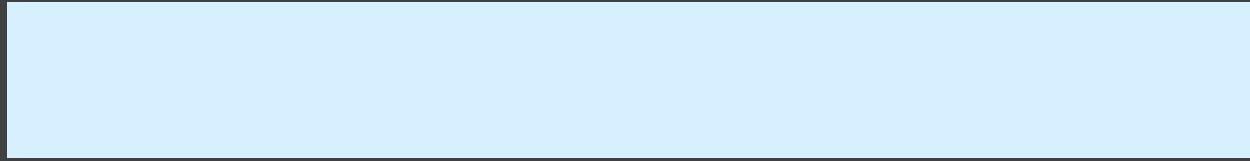
**Use encodings that people decode better**

(where better = faster and/or more accurate)

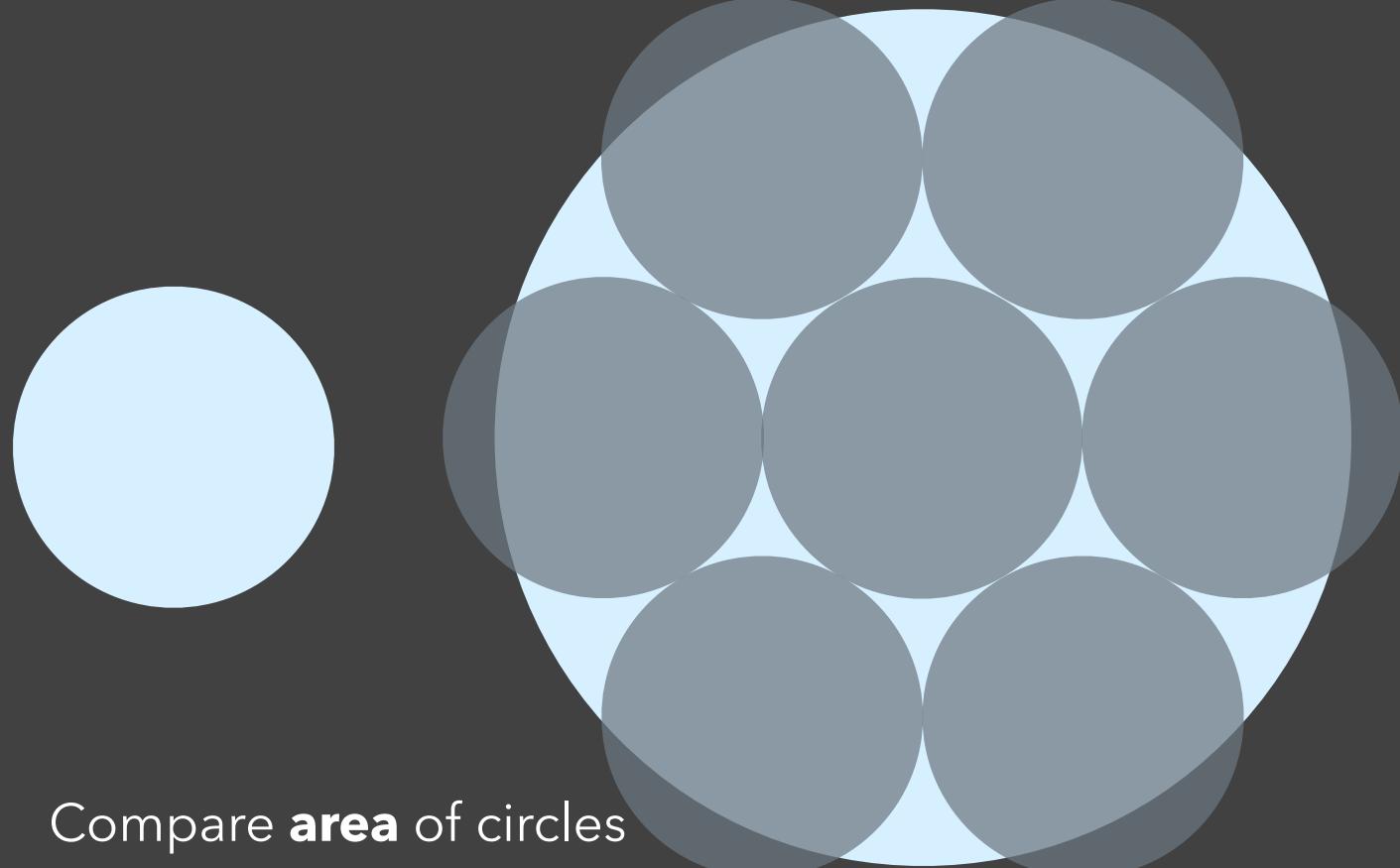
# A Quick Experiment...



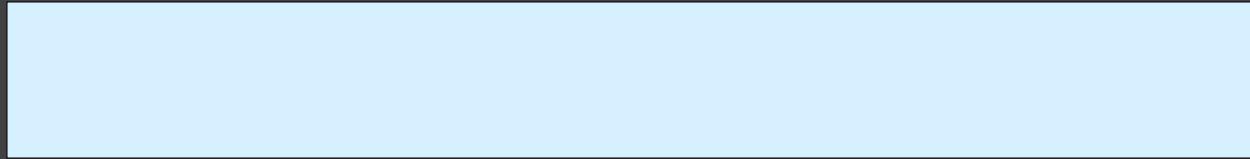
Compare **area** of circles



Compare **length** of bars

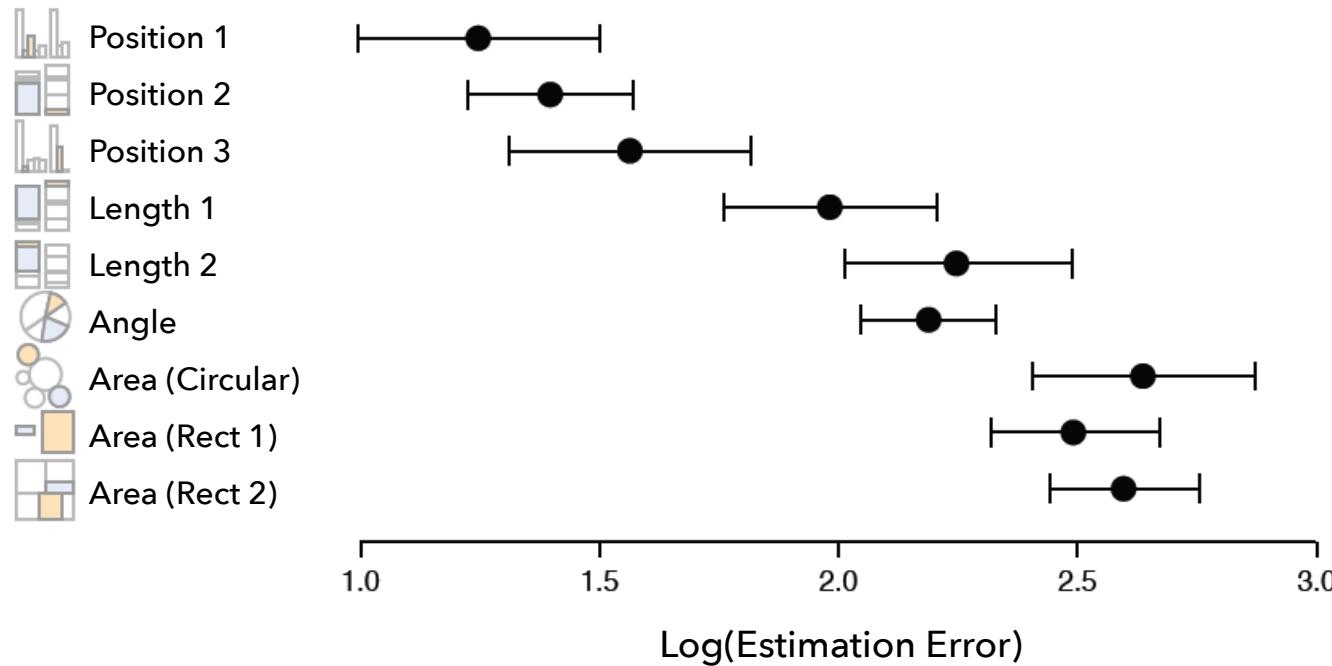


Compare **area** of circles

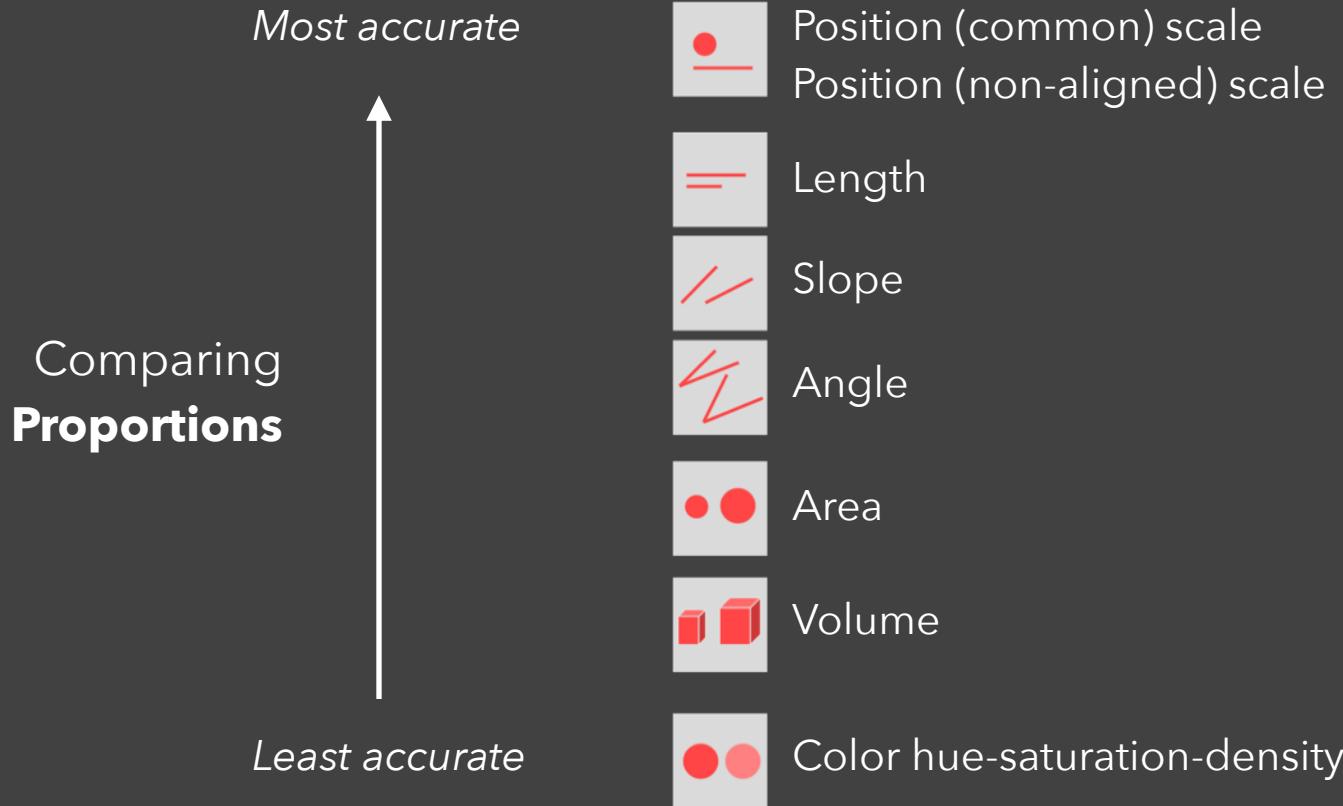


Compare **length** of bars

# Accuracy of Visual Decoding



# Ranking Visual Encodings



# Effectiveness Rankings [Mackinlay 86]

QUANTITATIVE	ORDINAL	NOMINAL
Position	Position	Position
Length	Density (Value)	Color Hue
Angle	Color Sat	Texture
Slope	Color Hue	Connection
Area (Size)	Texture	Containment
Volume	Connection	Density (Value)
Density (Value)	Containment	Color Sat
Color Sat	Length	Shape
Color Hue	Angle	Length
Texture	Slope	Angle
Connection	Area (Size)	Slope
Containment	Volume	Area
Shape	Shape	Volume

Conjectured effectiveness of encodings by data type

# Effectiveness Rankings [Mackinlay 86]

## QUANTITATIVE

**Position**

Length

Angle

Slope

Area (Size)

Volume

Density (Value)

Color Sat

Color Hue

Texture

Connection

Containment

Shape

## ORDINAL

**Position**

Density (Value)

Color Sat

Color Hue

Texture

Connection

Containment

Length

Angle

Slope

Area (Size)

Volume

Shape

## NOMINAL

**Position**

Color Hue

Texture

Connection

Containment

Density (Value)

Color Sat

Shape

Length

Angle

Slope

Area

Volume

Conjectured effectiveness of encodings by data type

# Effectiveness Rankings [Mackinlay 86]

## QUANTITATIVE

Position  
Length  
Angle  
Slope  
Area (Size)  
Volume  
Density (Value)  
**Color Sat**  
Color Hue  
Texture  
Connection  
Containment  
Shape

## ORDINAL

Position  
Density (Value)  
**Color Sat**  
Color Hue  
Texture  
Connection  
Containment  
Length  
Angle  
Slope  
Area (Size)  
Volume  
Shape

## NOMINAL

Position  
Color Hue  
Texture  
Connection  
Containment  
Density (Value)  
**Color Sat**  
Shape  
Length  
Angle  
Slope  
Area  
Volume

Conjectured effectiveness of encodings by data type

# Effectiveness Rankings [Mackinlay 86]

## QUANTITATIVE

Position  
Length  
Angle  
Slope  
Area (Size)  
Volume  
Density (Value)  
Color Sat  
**Color Hue**  
Texture  
Connection  
Containment  
Shape

## ORDINAL

Position  
Density (Value)  
Color Sat  
**Color Hue**  
Texture  
Connection  
Containment  
Length  
Angle  
Slope  
Area (Size)  
Volume  
Shape

## NOMINAL

Position  
**Color Hue**  
Texture  
Connection  
Containment  
Density (Value)  
Color Sat  
Shape  
Length  
Angle  
Slope  
Area  
Volume

Conjectured effectiveness of encodings by data type

# Mackinlay's Design Algorithm

**APT** - "A Presentation Tool", 1986

**User formally specifies data model and type**

Input: ordered list of data variables to show

**APT searches over design space**

Test expressiveness of each visual encoding

Generate encodings that pass test

Rank by perceptual effectiveness criteria

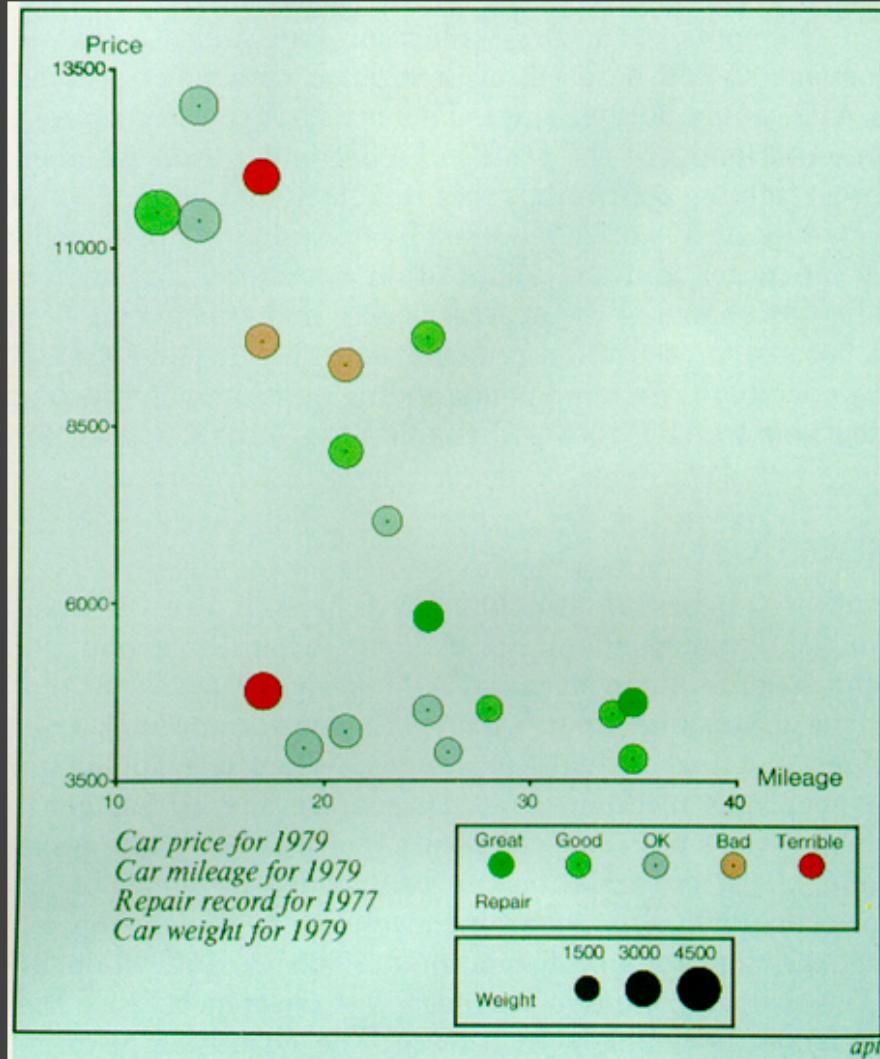
**Output the “most effective” visualization**

# APT

Automatically  
generate chart  
for car data

Input variables:

1. Price
2. Mileage
3. Repair
4. Weight



# Limitations of APT

**Does not cover many visualization techniques**

Networks, hierarchies, maps, diagrams

Also: 3D structure, animation, illustration, ...

**Does not consider interaction**

**Does not consider semantics / conventions**

**Assumes single visualization as output**

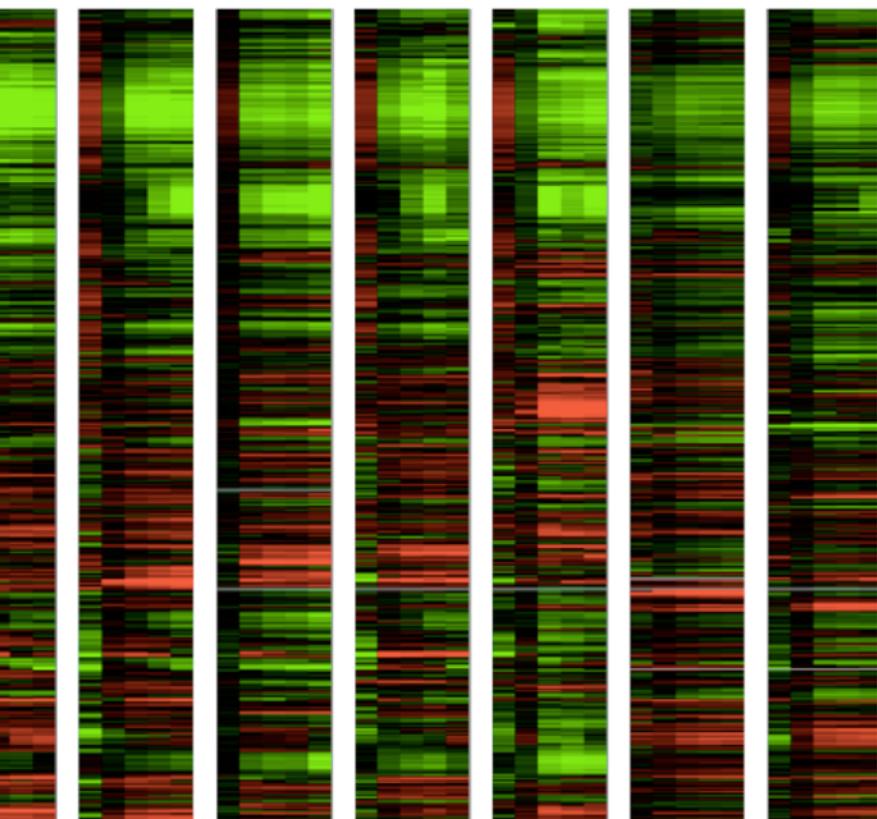
Still an active area of research, e.g., the

**Draco visualization design knowledge base**

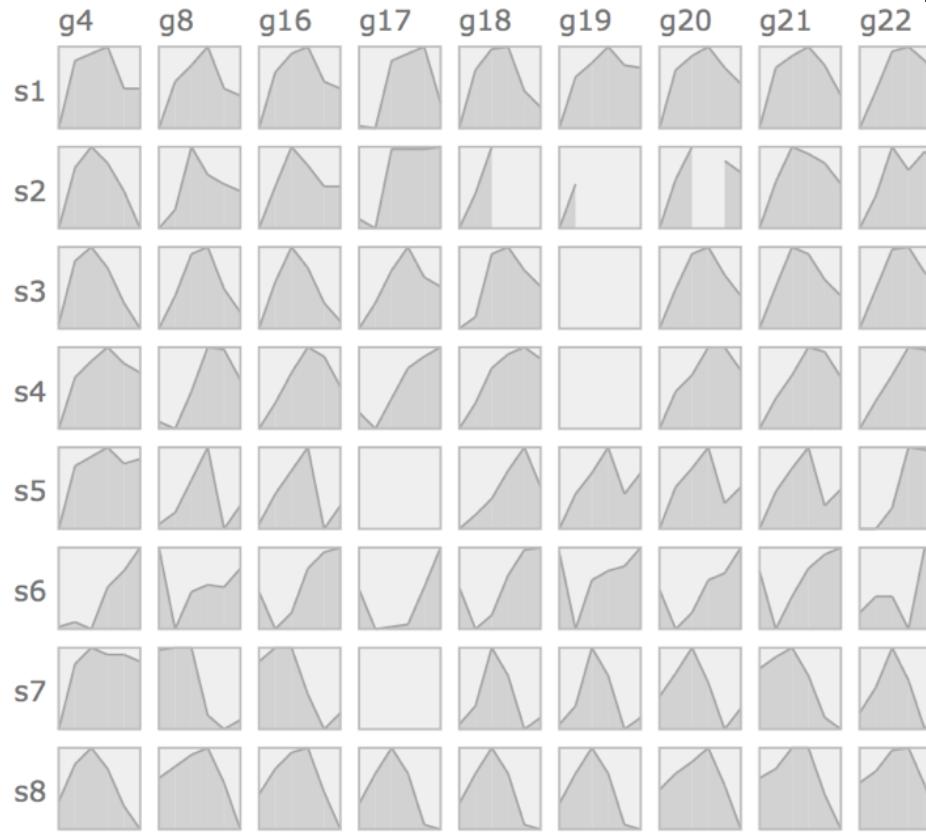
# Design Examples

# Gene Expression Time-Series [Meyer et al. 2011]

Color Encoding



Position Encoding



# Effectiveness Rankings

## QUANTITATIVE

### **Position**

Length

Angle

Slope

Area (Size)

Volume

### **Density (Value)**

Color Sat

### **Color Hue**

Texture

Connection

Containment

Shape

## ORDINAL

Position

Density (Value)

Color Sat

Color Hue

Texture

Connection

Containment

Length

Angle

Slope

Area (Size)

Volume

Shape

## NOMINAL

Position

Color Hue

Texture

Connection

Containment

Density (Value)

Color Sat

Shape

Length

Angle

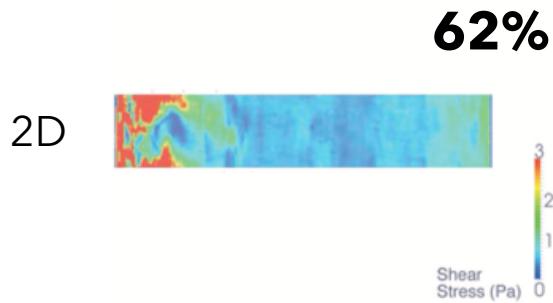
Slope

Area

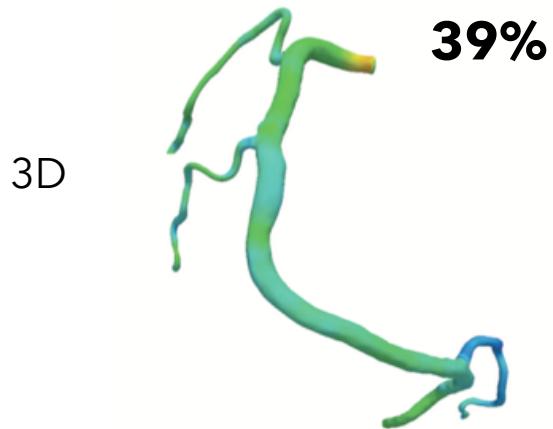
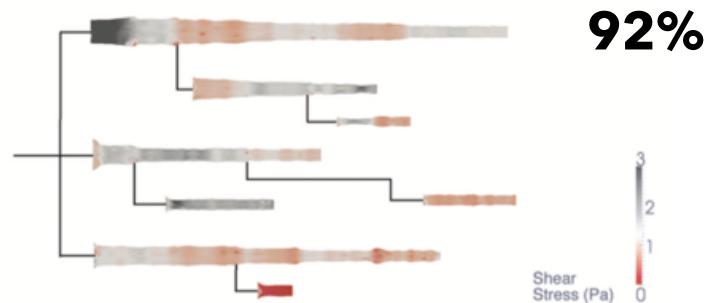
Volume

# Artery Visualization [Borkin et al. 2011]

Rainbow Palette



Diverging Palette



# Effectiveness Rankings

## QUANTITATIVE

### **Position ↗**

Length  
Angle  
Slope  
Area (Size)  
Volume

### **Density (Value)**

### **Color Sat**

### **Color Hue**

Texture  
Connection  
Containment  
Shape

## ORDINAL

Position  
Density (Value)  
Color Sat  
Color Hue  
Texture

### **Connection**

Containment  
Length  
Angle  
Slope  
Area (Size)  
Volume  
Shape

## NOMINAL

Position  
Color Hue  
Texture  
Connection  
Containment  
Density (Value)  
Color Sat  
Shape  
Length  
Angle  
Slope  
Area  
Volume

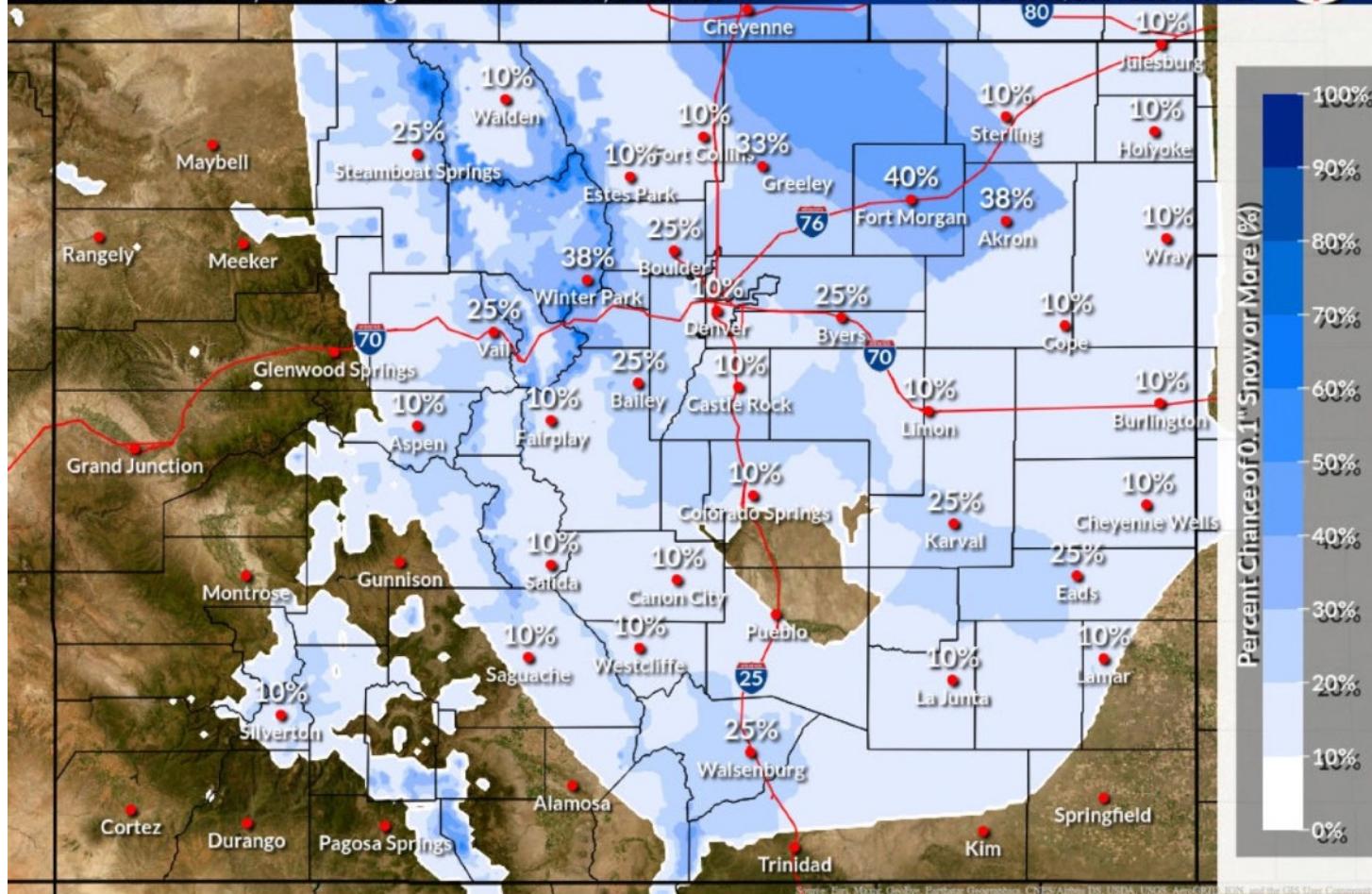
## Percent Chance of 0.1" Snow or More

Weather Forecast Office  
Denver/Boulder



Valid 5 AM Tue Dec 31, 2024 through 5 AM Wed Jan 01, 2025 MST

Issued Dec 31, 2024 2:52 AM MST



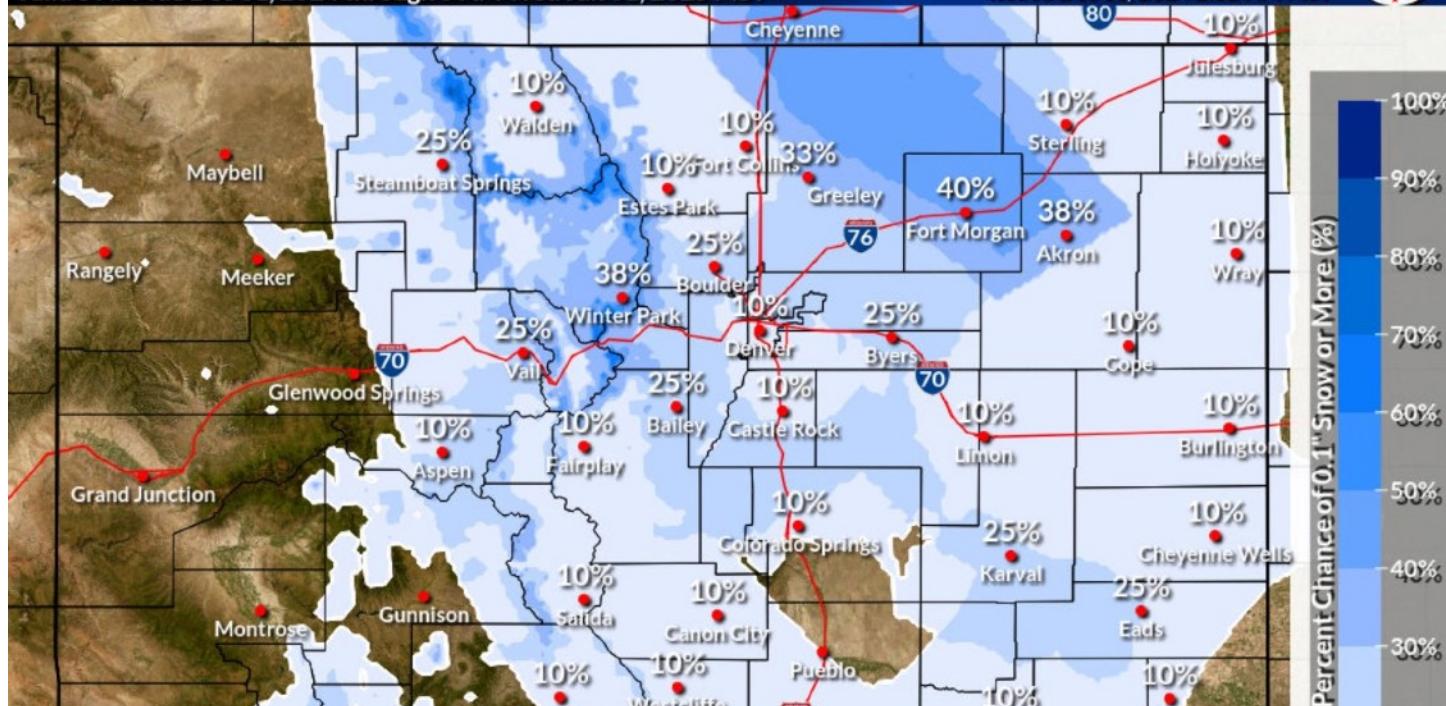
# Percent Chance of 0.1" Snow or More

Weather Forecast Office  
Denver/Boulder



Valid 5 AM Tue Dec 31, 2024 through 5 AM Wed Jan 01, 2025 MST

Issued Dec 31, 2024 2:52 AM MST



Percent Chance of 0.1" Snow or More (%)

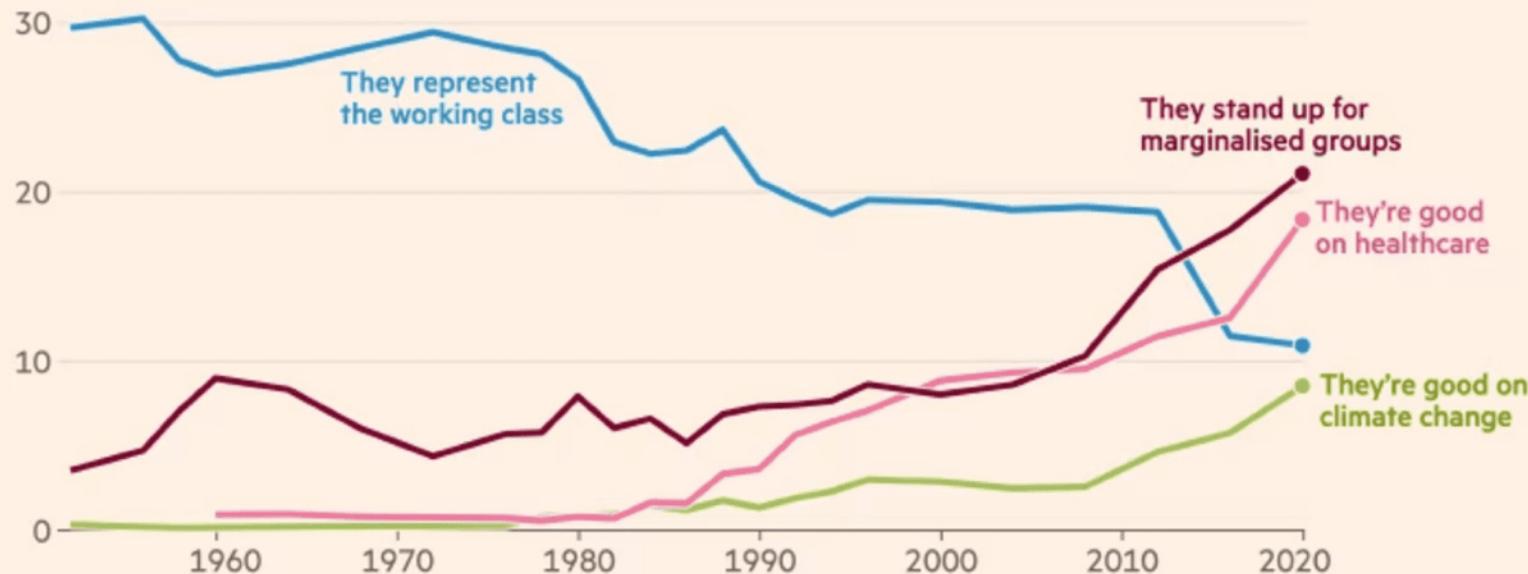
White is the least snow?  
Conflict between "dark is more" and color/concept association.



Percent Chance of 0.1" Snow or More (%)

For the first time in at least 80 years, voters associate the Democrats more with sociocultural issues than with class and economic solidarity

Main reasons people say they like the Democratic party (% of all reasons given)



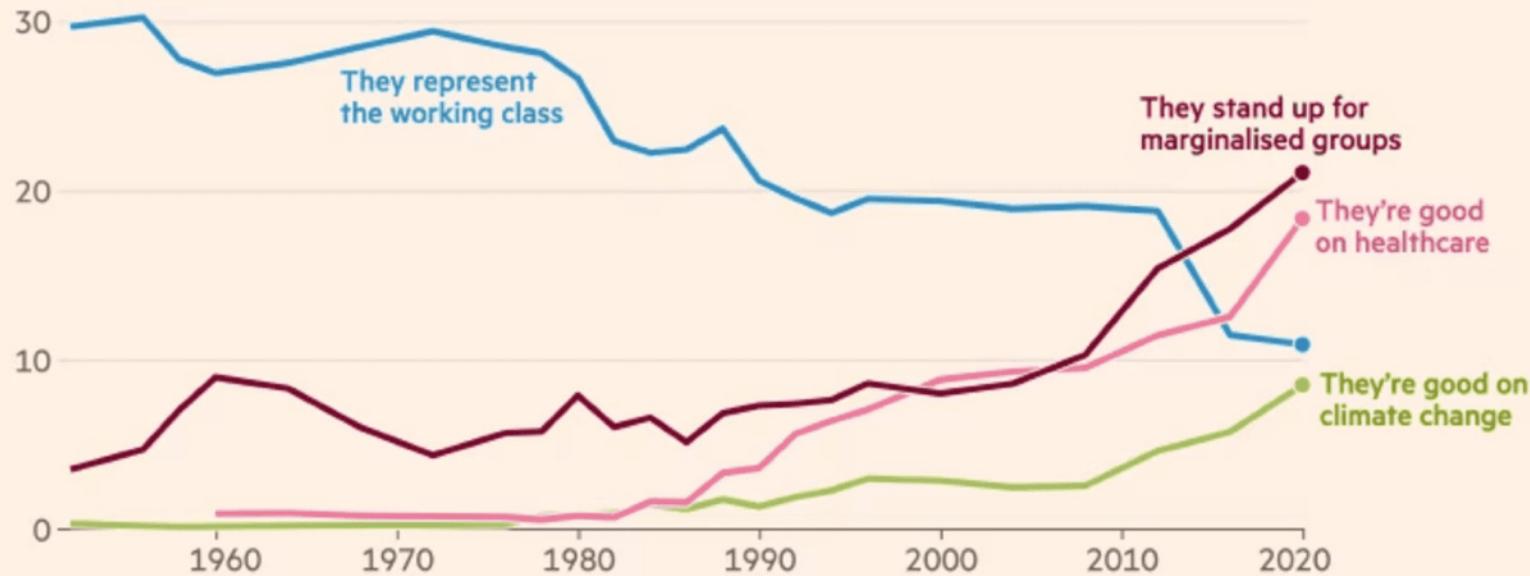
Source: FT analysis of American National Election Studies, based on Party Images in the American Electorate (Brewer, 2008)

FT graphic: John Burn-Murdoch / @jburnmurdoch

© FT

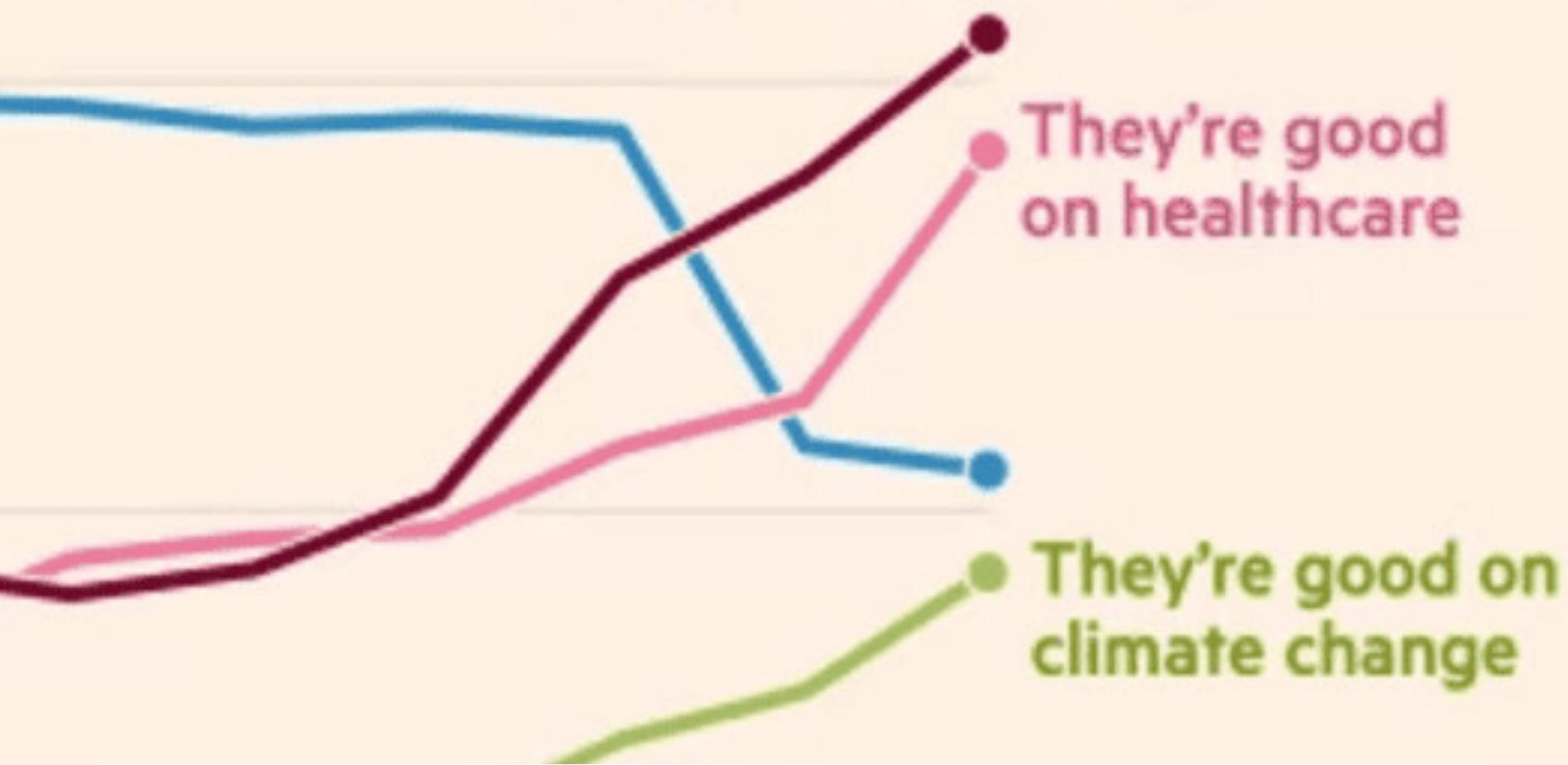
For the first time in at least 80 years, voters associate the Democrats more with sociocultural issues than with class and economic solidarity

Main reasons people say they like the Democratic party (% of all reasons given)



Direct labels, rather than legend. (But y-axis units?)

Title and subtitle convey context and steer interpretation.



Subtle outlines aid discrimination of line segments.

# A Design Space of Visual Encodings

# Mapping Data to Visual Variables

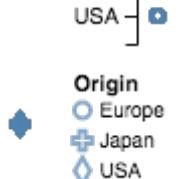
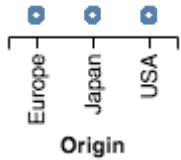
Assign **data fields** (e.g., with  $N$ ,  $O$ ,  $Q$  types) to **visual channels** ( $x$ ,  $y$ , *color*, *shape*, *size*, ...) for a chosen **graphical mark** type (*point*, *bar*, *line*, ...).

Additional concerns include choosing appropriate **encoding parameters** (*log scale*, *sorting*, ...) and **data transformations** (*bin*, *group*, *aggregate*, ...).

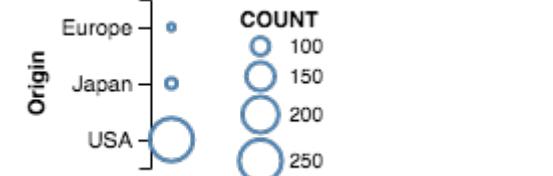
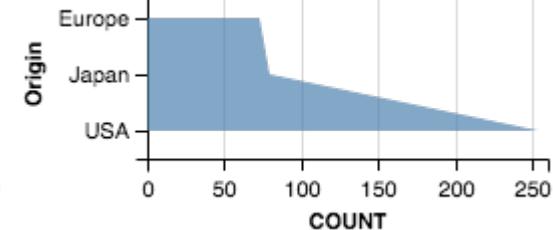
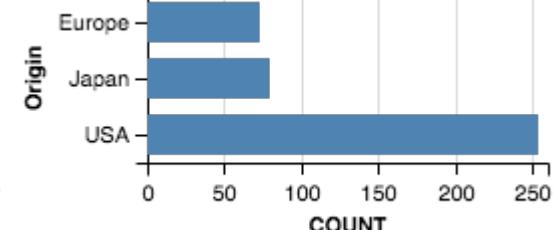
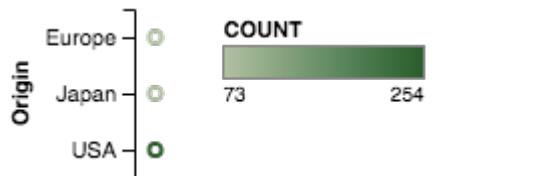
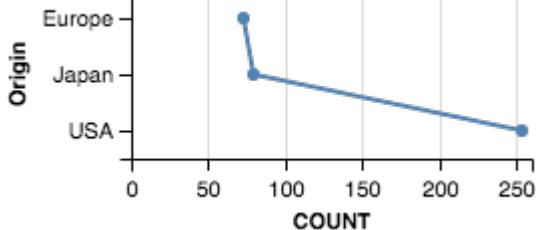
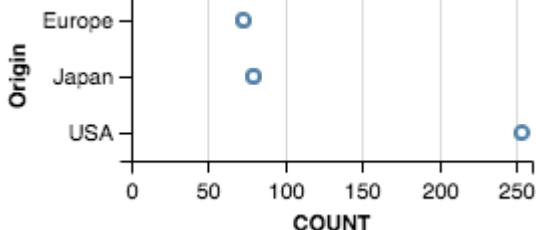
These options define a large combinatorial space, containing both useful and questionable charts!

# 1D: Nominal

Raw



Aggregate (Count)

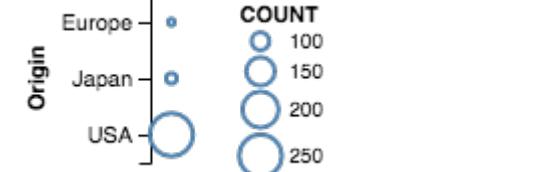
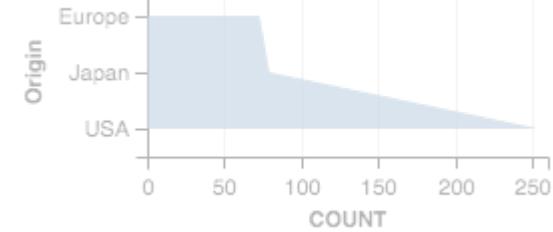
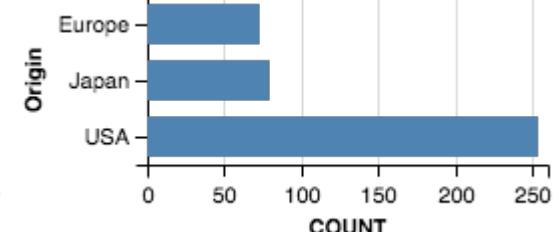
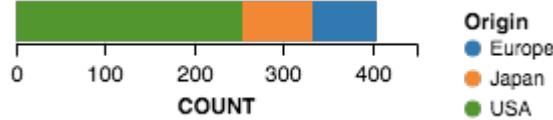
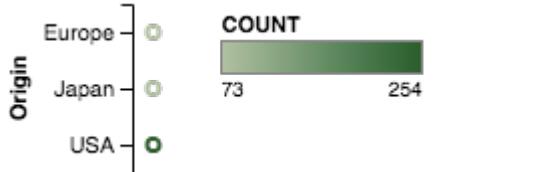
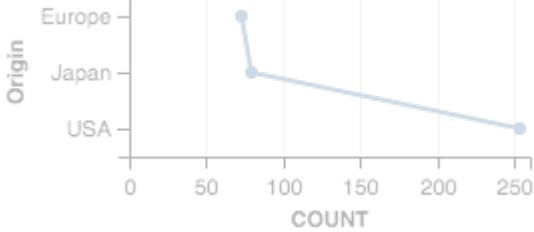
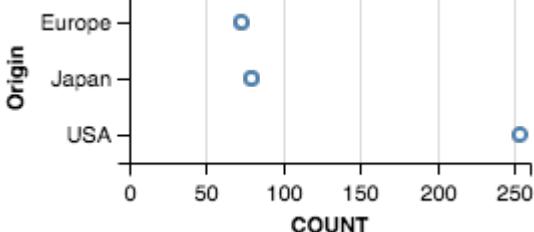


# Expressive?

Raw

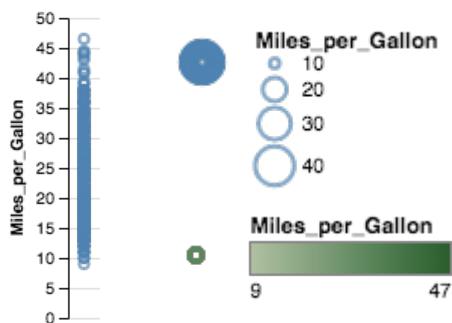
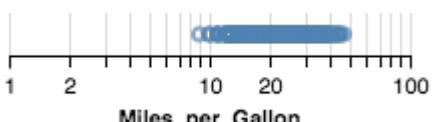
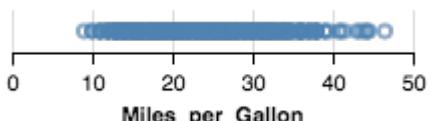
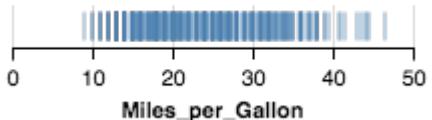


Aggregate (Count)

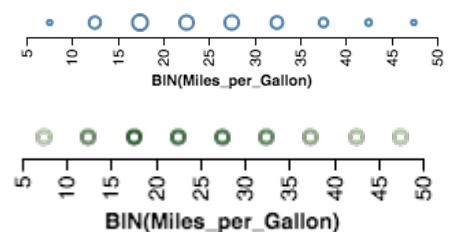
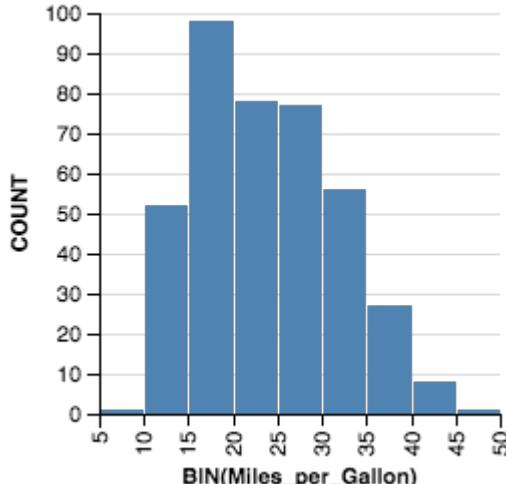


# 1D: Quantitative

Raw

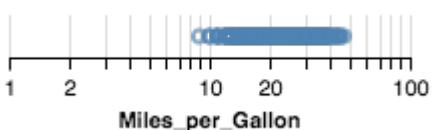
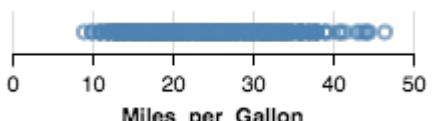
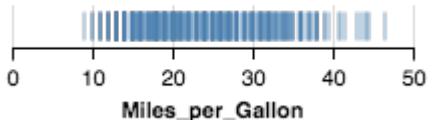


Aggregate (Count)

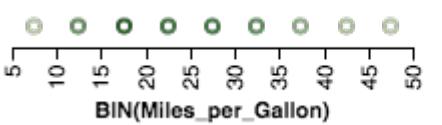
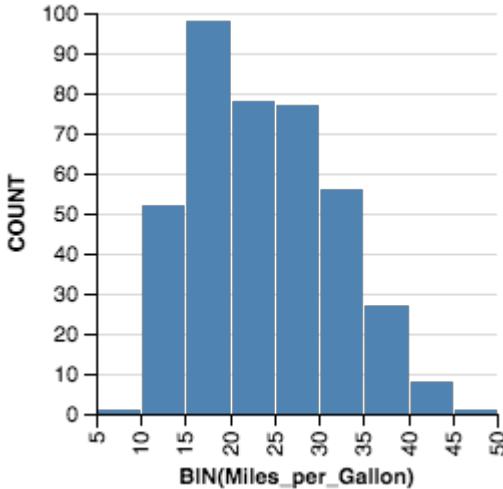


# Expressive?

Raw

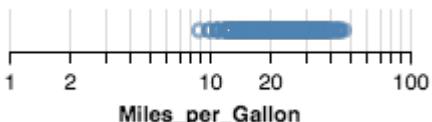
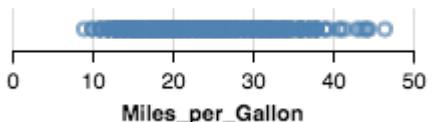
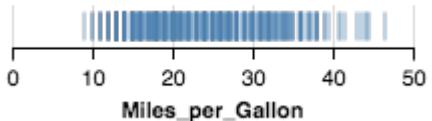


Aggregate (Count)

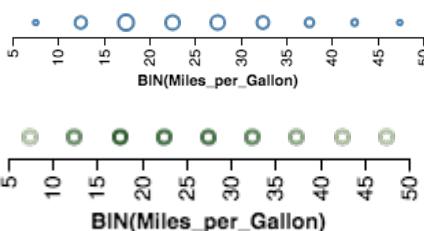
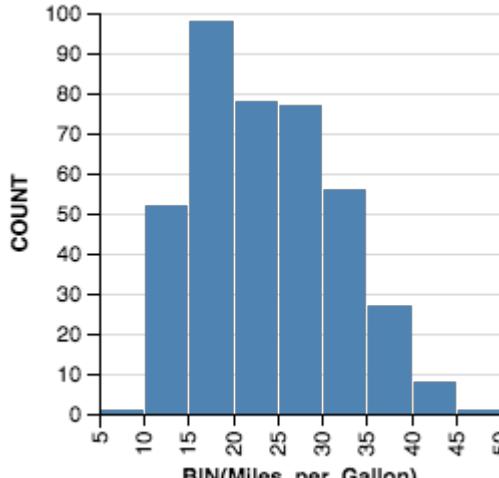


# Effective?

Raw



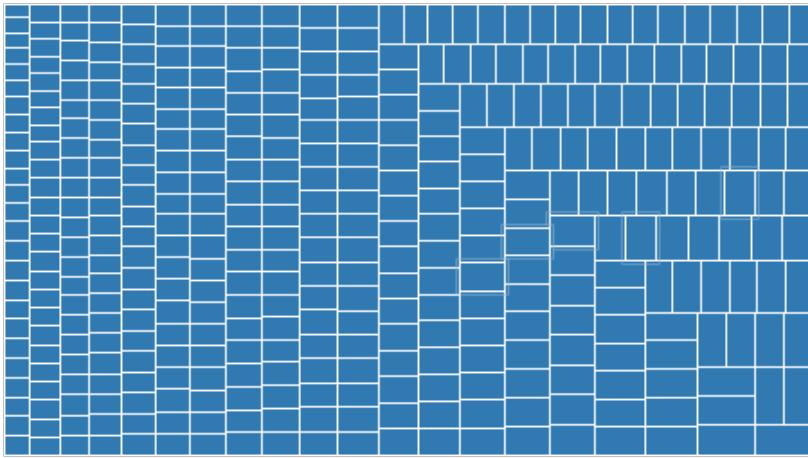
Aggregate (Count)



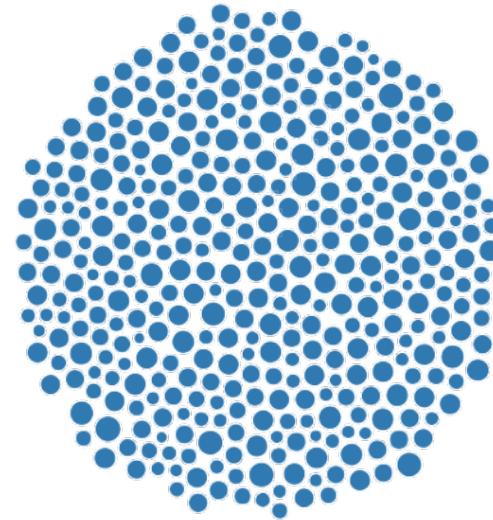
COUNT  
20  
40  
60  
80

COUNT  
1  
98

## Raw (with Layout Algorithm)

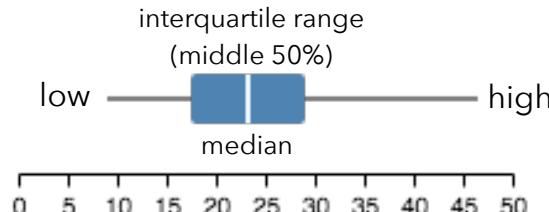


Treemap

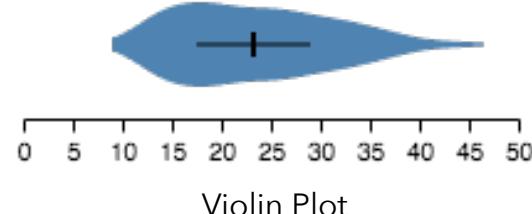


Bubble Chart

## Aggregate (Distributions)



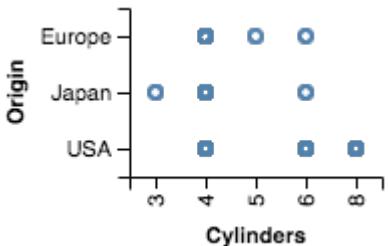
Box Plot



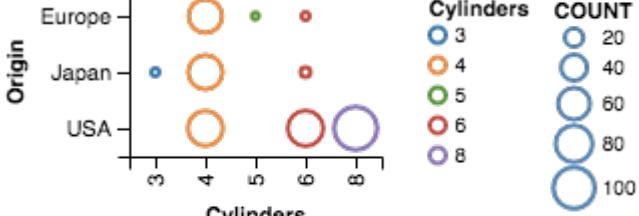
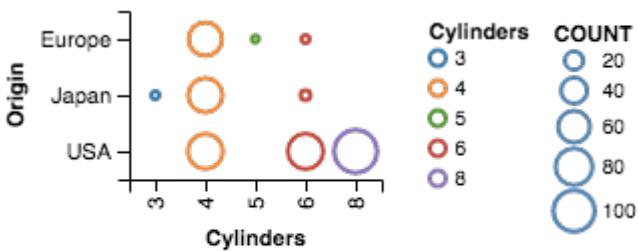
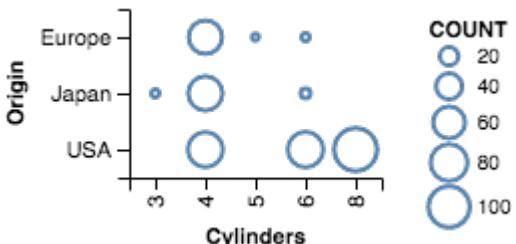
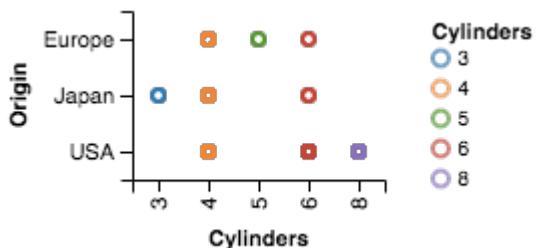
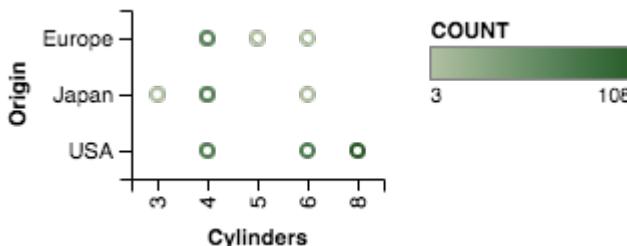
Violin Plot

# 2D: Nominal x Nominal

Raw

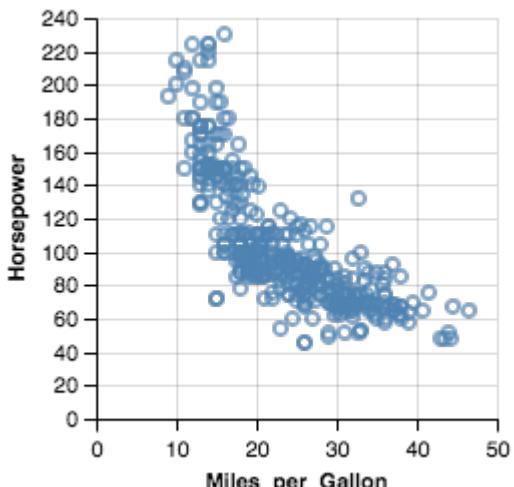


Aggregate (Count)

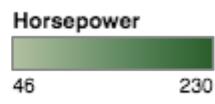
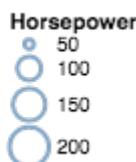
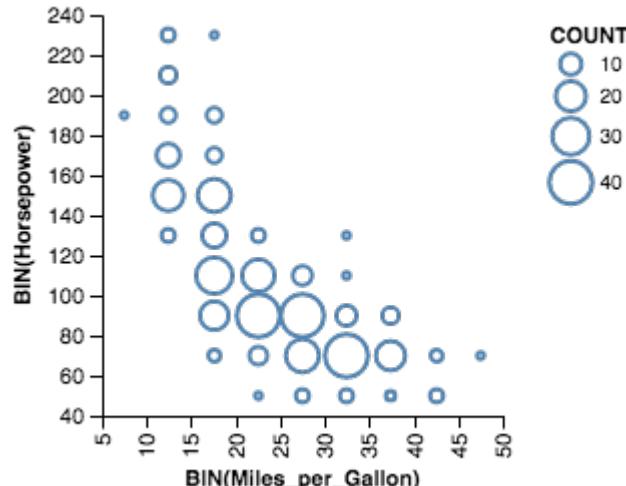


# 2D: Quantitative x Quantitative

Raw

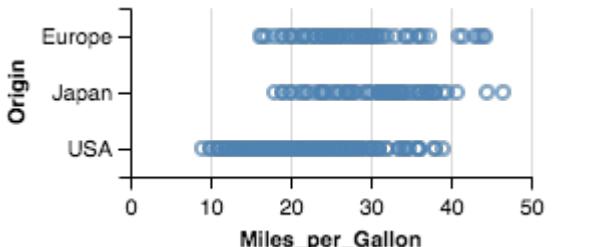


Aggregate (Count)

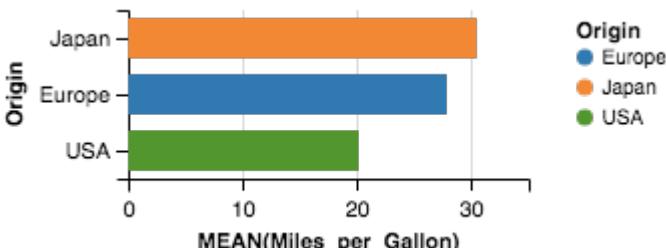
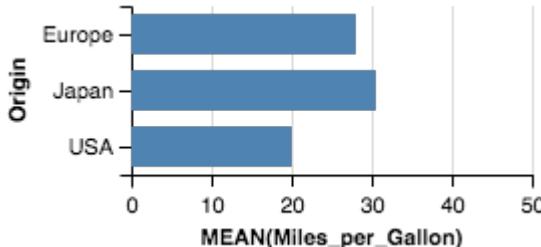


# 2D: Nominal x Quantitative

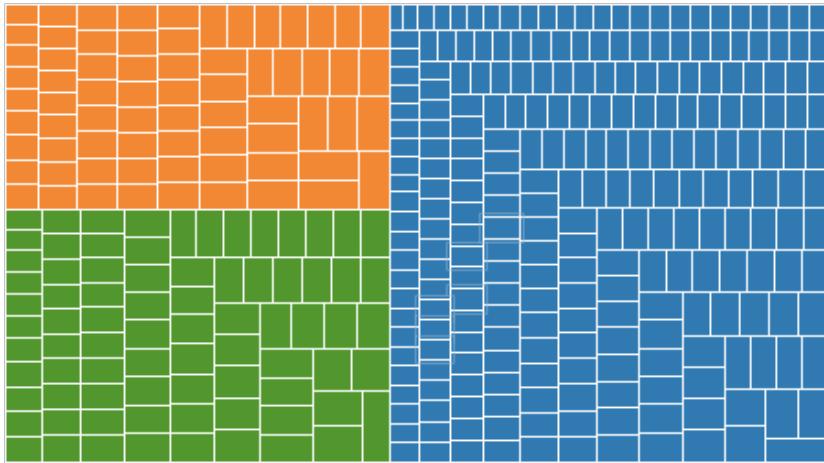
Raw



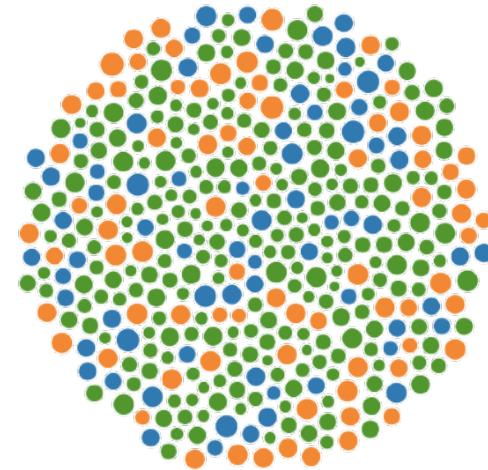
Aggregate (Mean)



## Raw (with Layout Algorithm)

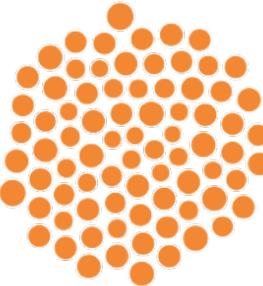
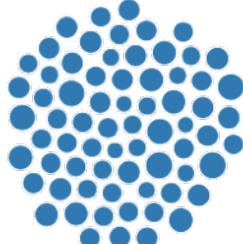


Treemap

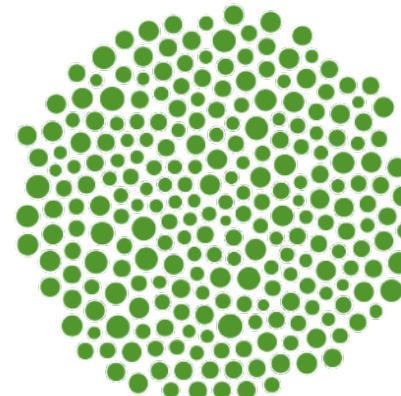


Bubble Chart

Origin  
● Europe  
● Japan  
● USA



Beeswarm Plot



# 3D and Higher

## Two variables [x, y]

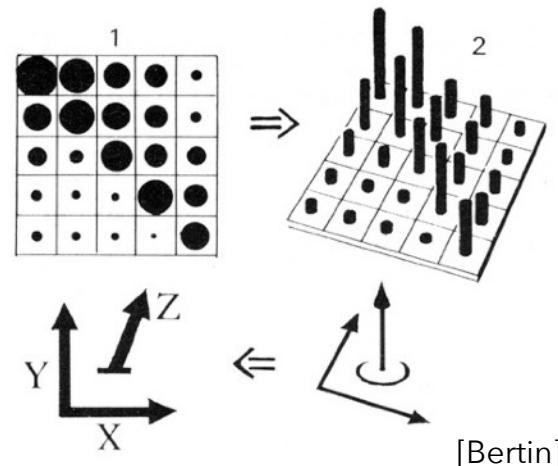
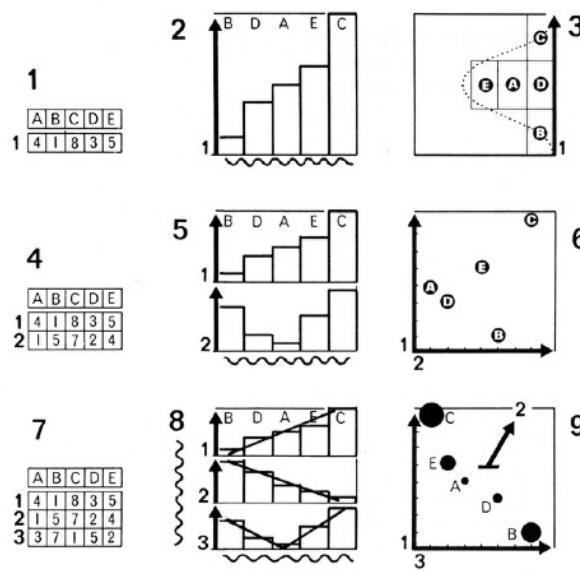
Can map to 2D points.

Scatterplots, maps, ...

## Third variable [z]

Often use one of size, color, opacity, shape, etc. Or, one can further partition space.

*What about 3D rendering?*



# wind map

[Viegas & Wattenberg]

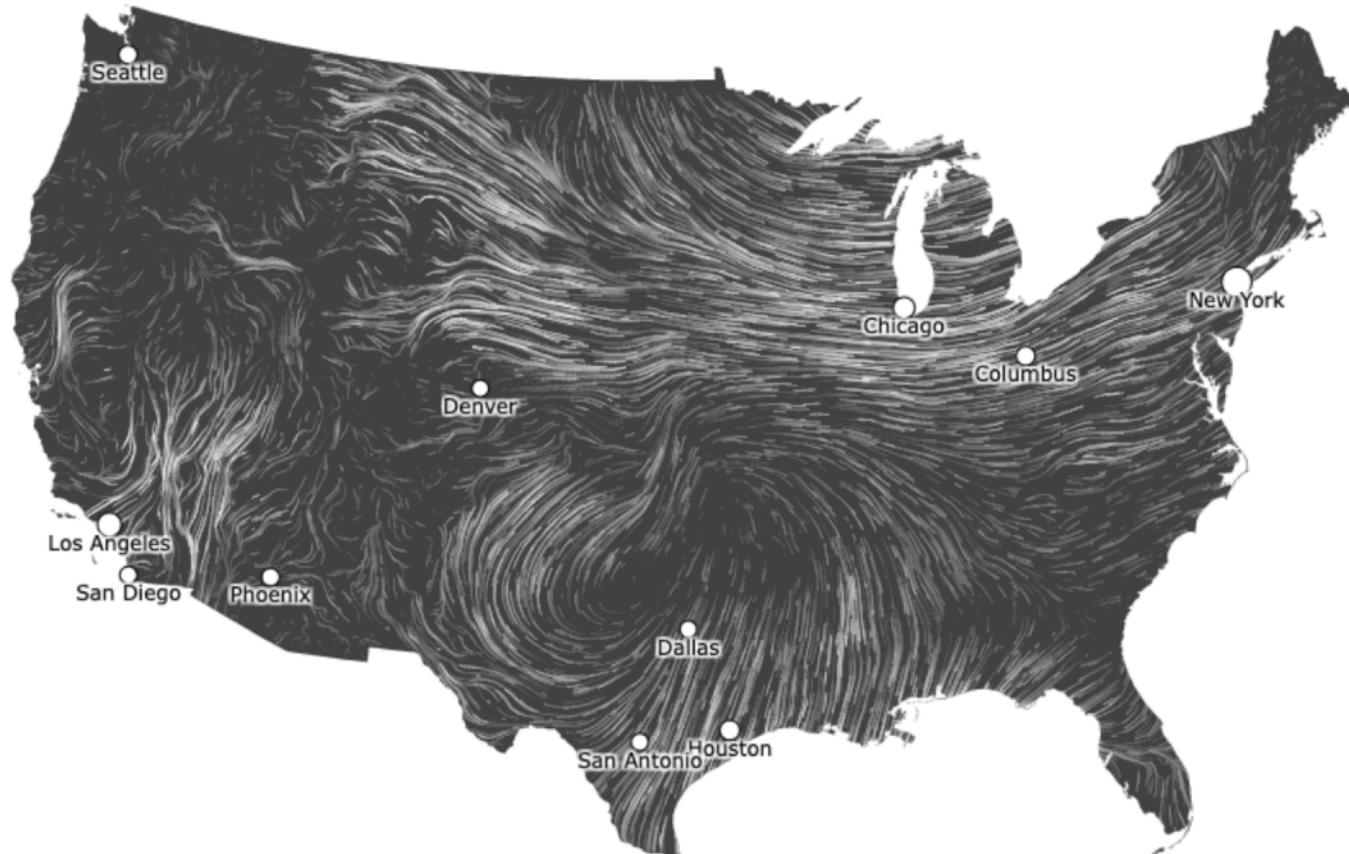
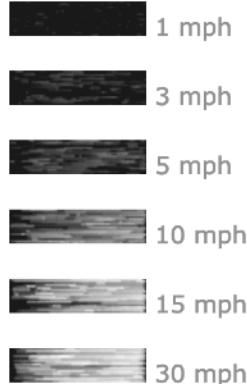
January 13, 2025

12:21 pm EST

(time of forecast download)

top speed: **25.2 mph**

average: **8.1 mph**



# Multidimensional Data

# Visual Encoding Channels

Position (X)

Position (Y)

Area

Value

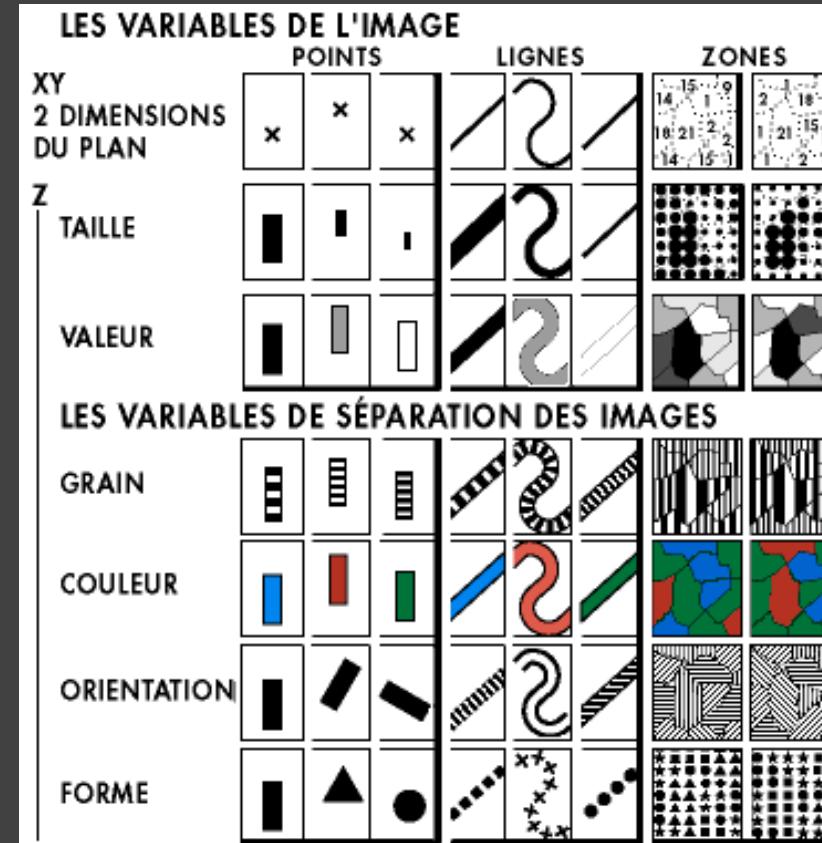
Texture

Color

Orientation

Shape

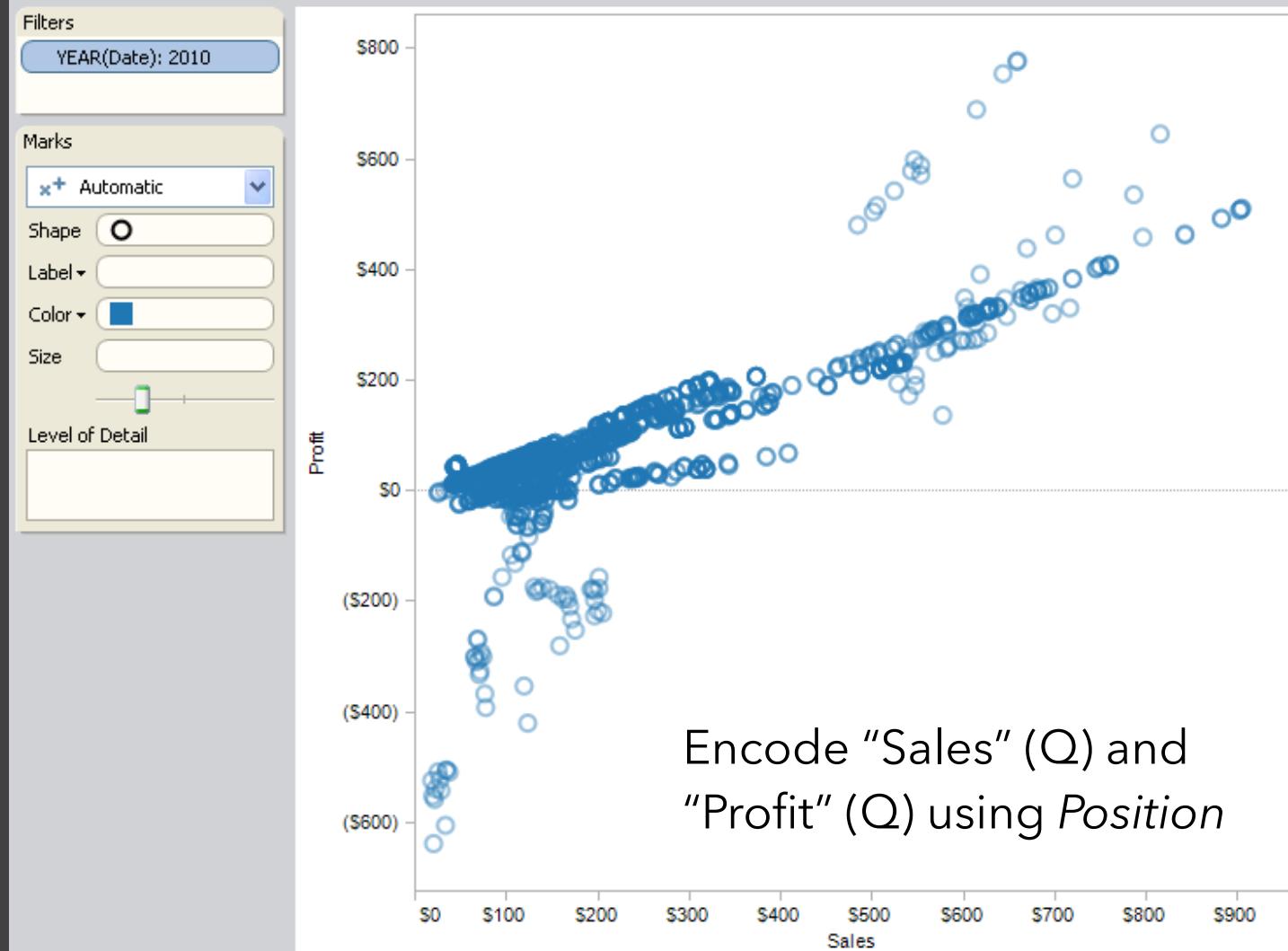
~8 dimensions?

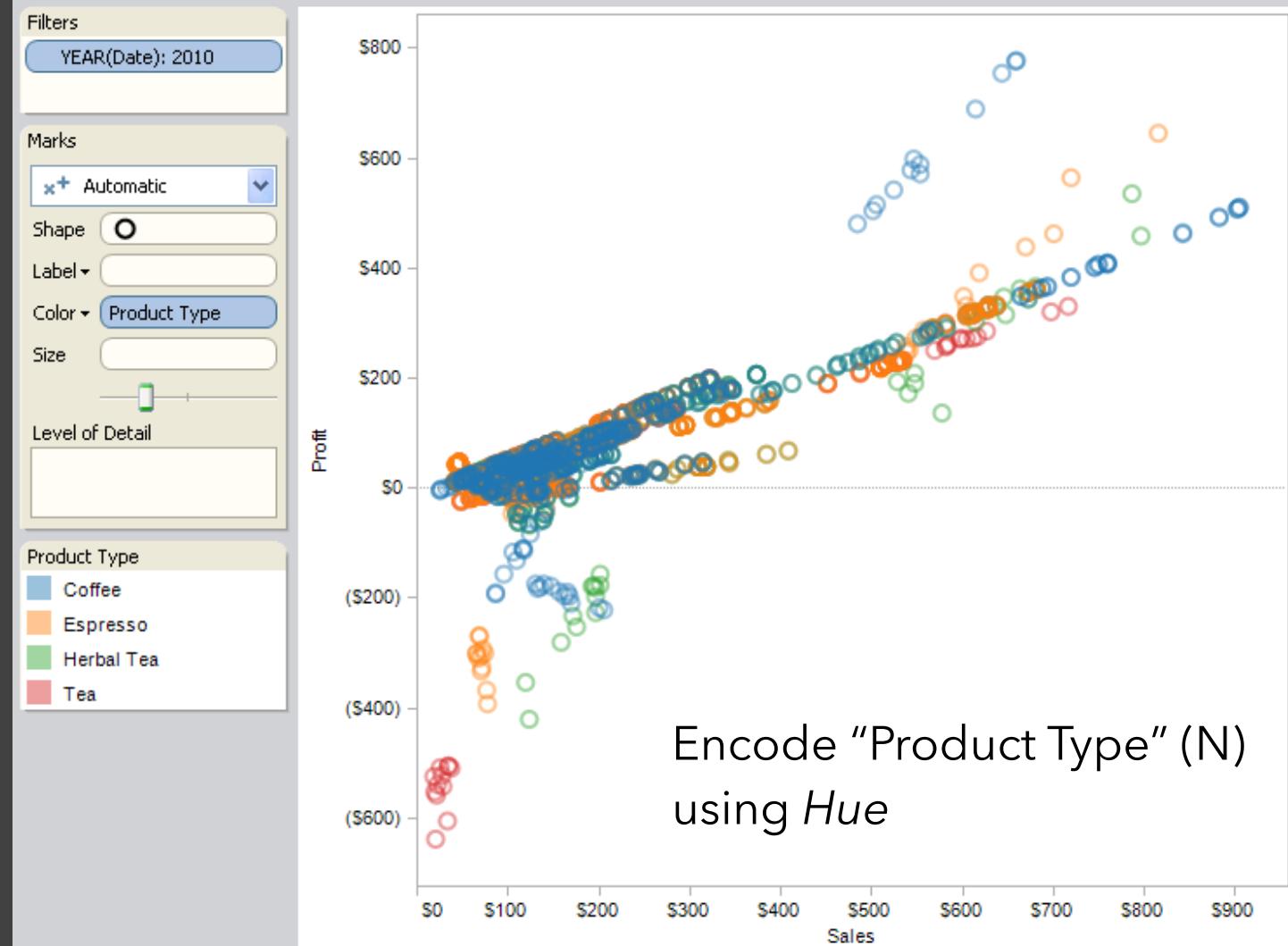


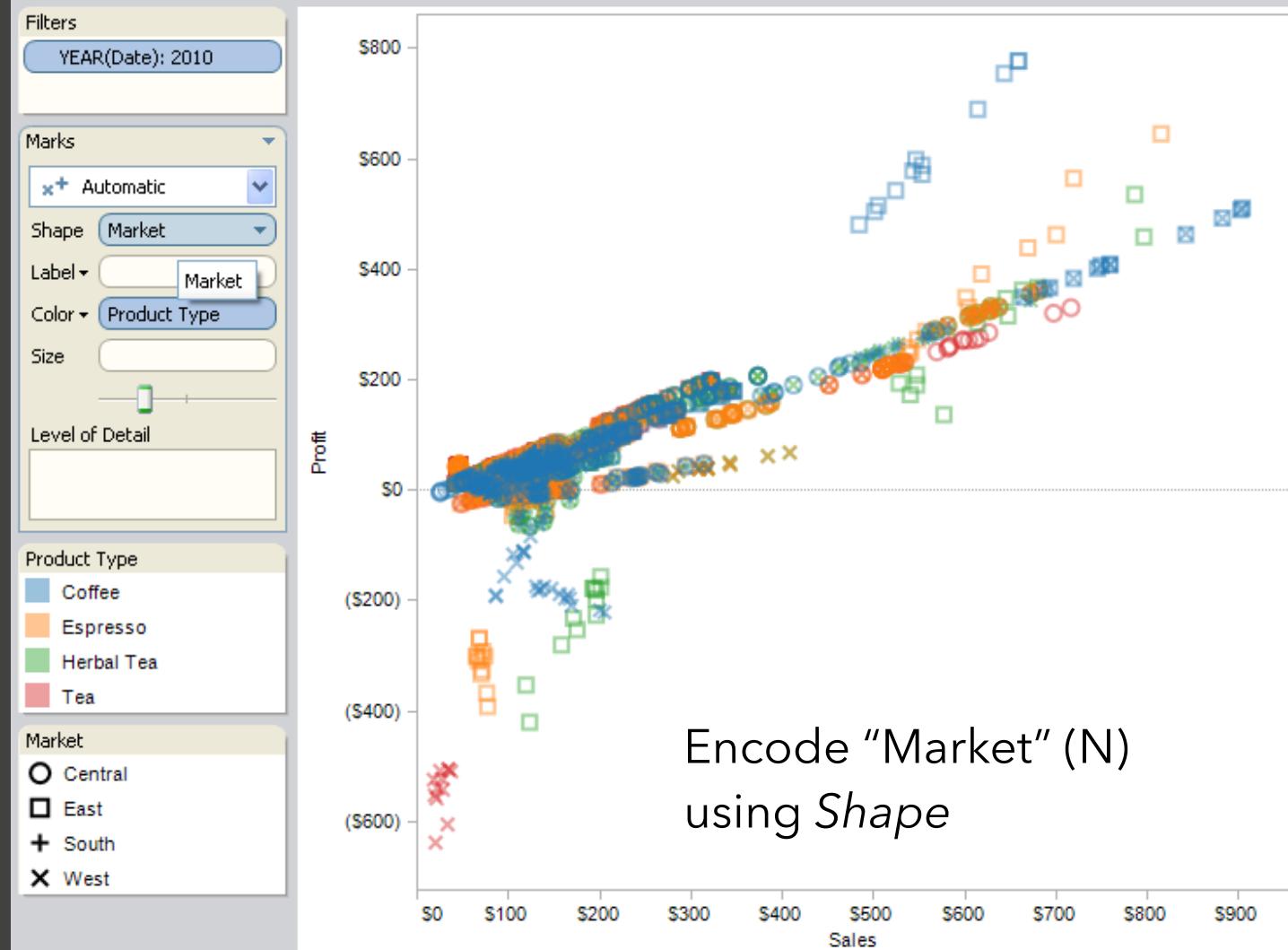
# Example: Coffee Sales

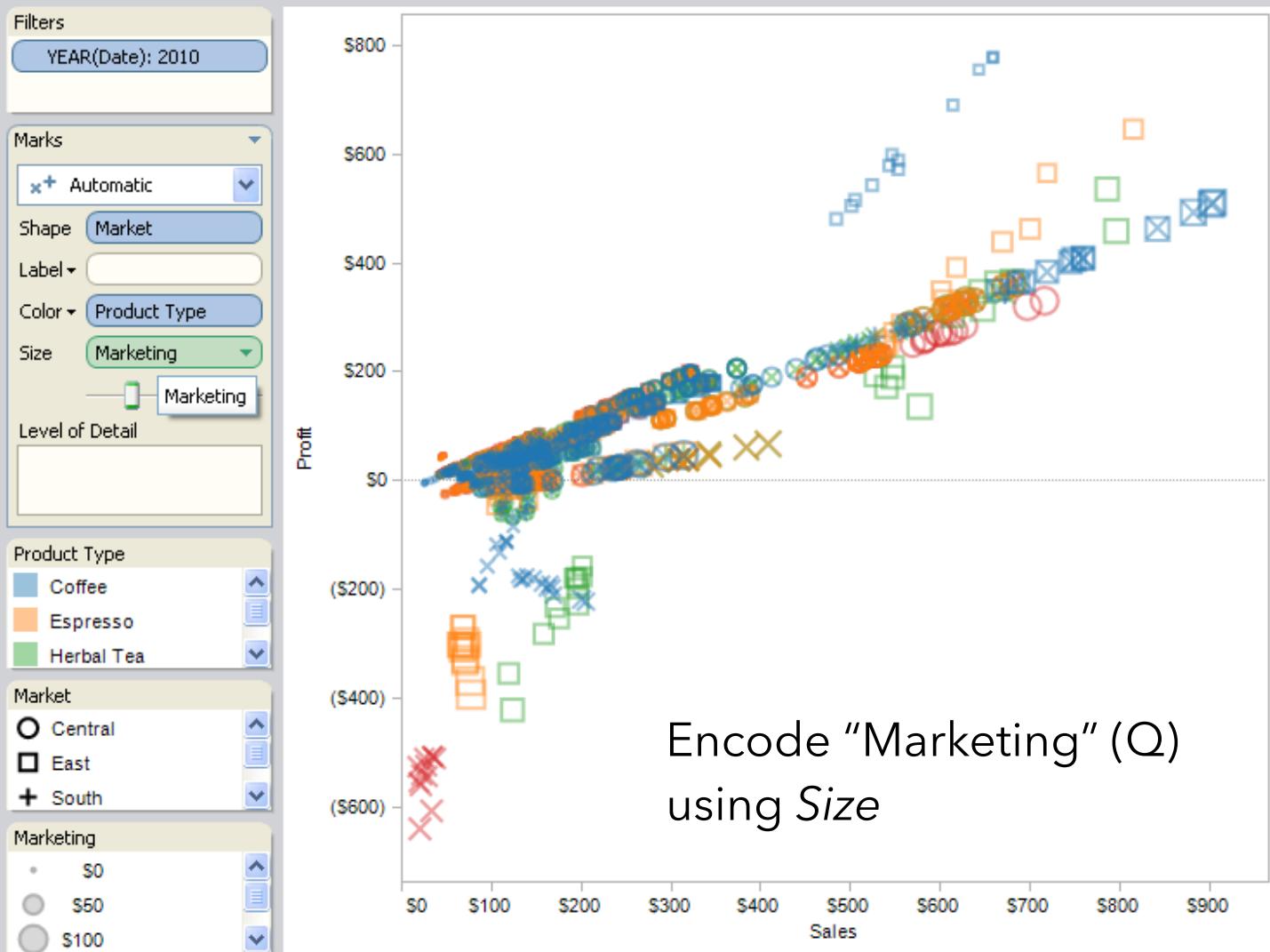
Sales figures for a fictional coffee chain

Sales	Q-Ratio
Profit	Q-Ratio
Marketing	Q-Ratio
Product Type	N {Coffee, Espresso, Herbal Tea, Tea}
Market	N {Central, East, South, West}









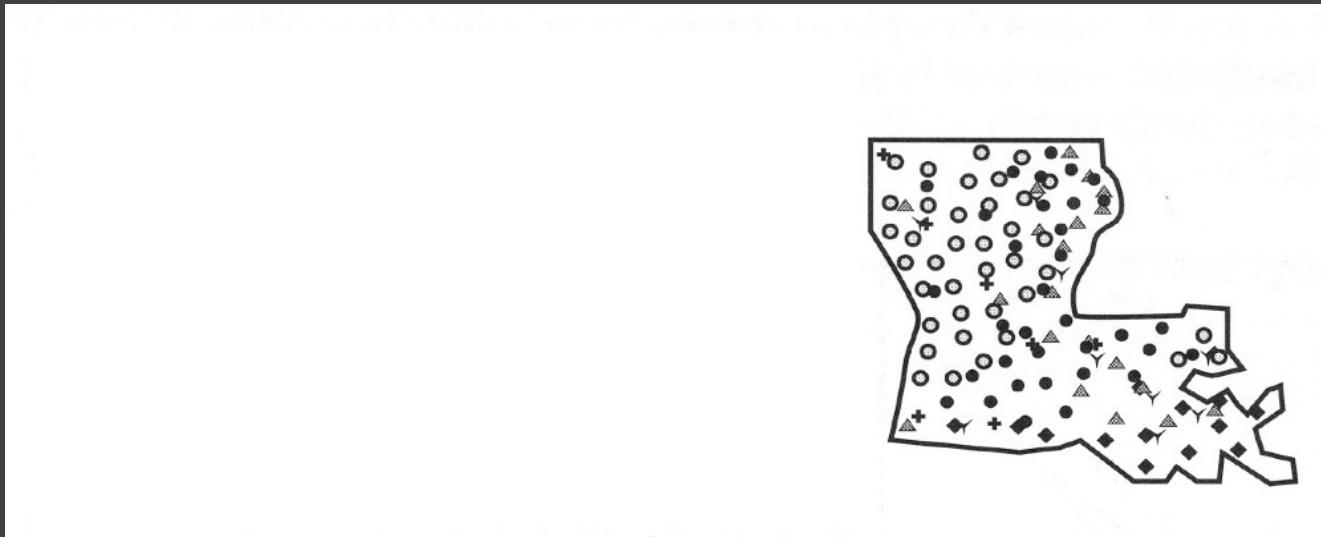
# Trellis Plots



A *trellis plot* subdivides space to enable comparison across multiple plots.

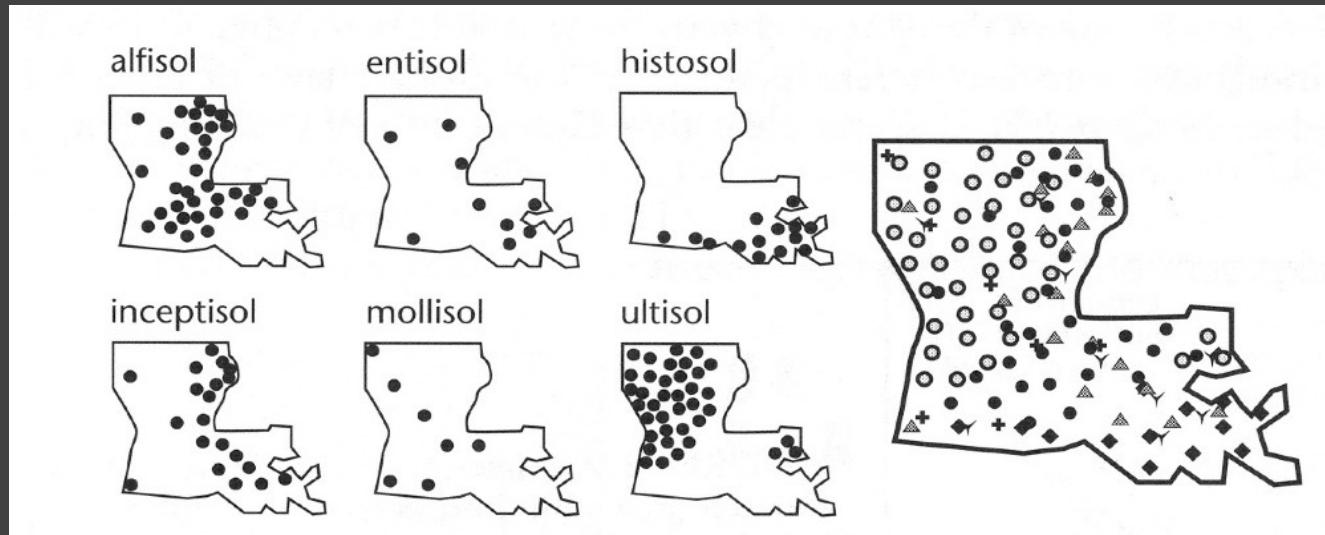
Typically nominal or ordinal variables are used as dimensions for subdivision.

# Small Multiples



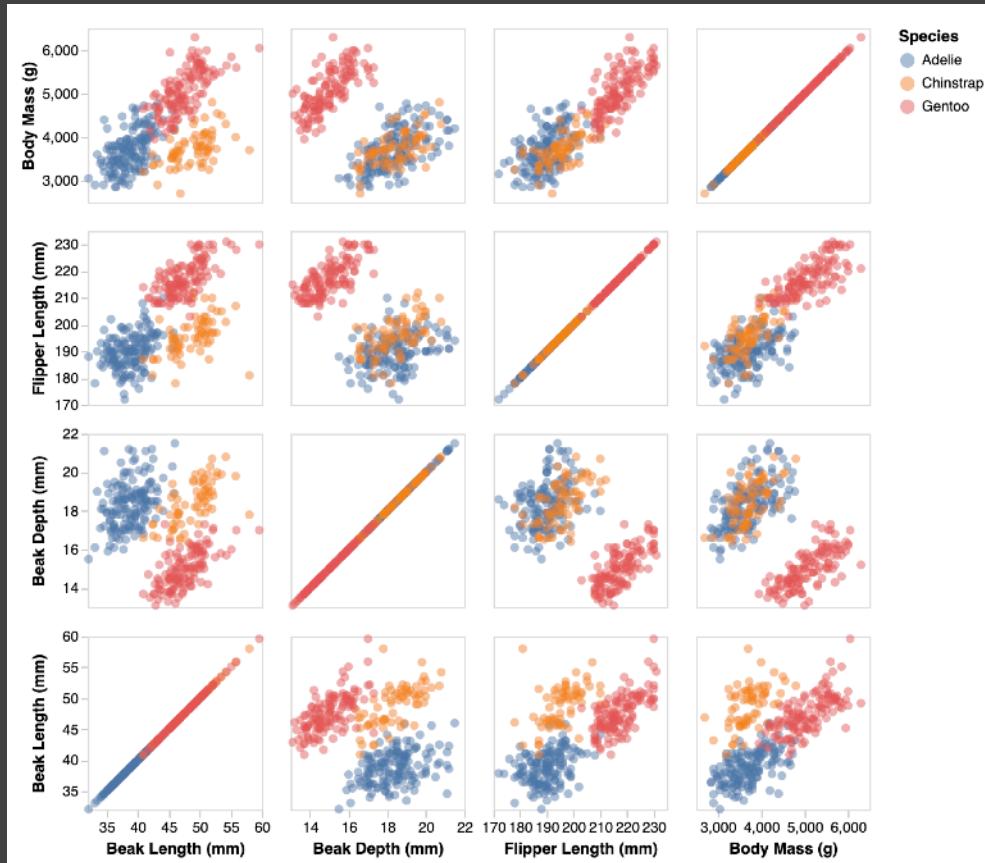
[MacEachren '95, Figure 2.11, p. 38]

# Small Multiples



[MacEachren '95, Figure 2.11, p. 38]

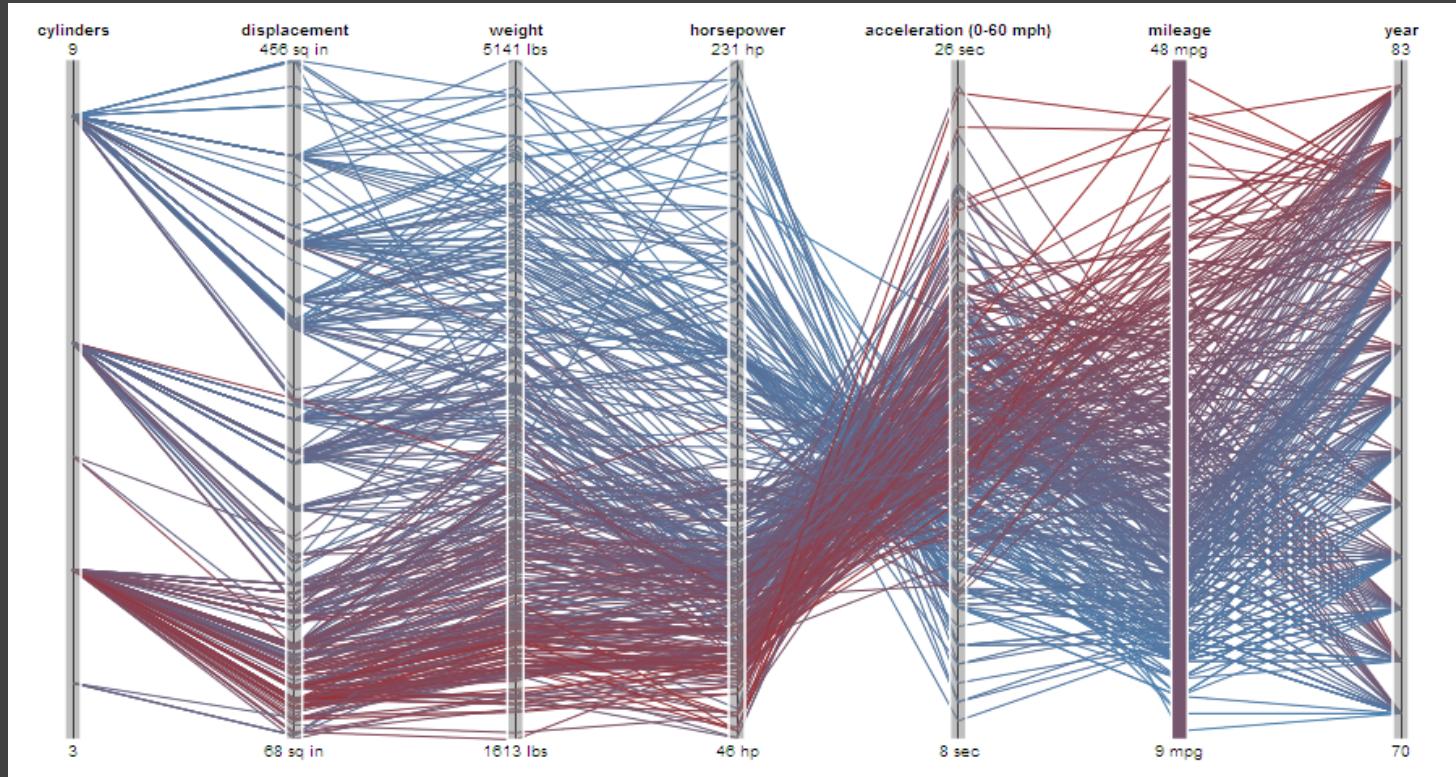
# Scatterplot Matrix (SPLOM)



Scatter plots for pairwise comparison of each data dimension.

# Parallel Coordinates

# Parallel Coordinates [Inselberg]



# Parallel Coordinates [Inselberg]

Visualize up to ~two dozen dimensions at once

1. Draw parallel axes for each variable
2. For each tuple, connect points on each axis

Between adjacent axes: line crossings imply neg. correlation, shared slopes imply pos. correlation.

Full plot can be cluttered. **Interactive selection** can be used to assess multivariate relationships.

Highly sensitive to axis **scale** and **ordering**.

Expertise required to use effectively!

# A1: Expository Visualization

Using the given climate data set...

Pick a **guiding question**, use it to title your vis.

Design a **static visualization** for that question.

You are free to **use any visualization tool**.

**Deliverables** via Gradescope

Image of your visualization (PNG or JPG format)

Short description + design rationale ( $\leq 4$  paragraphs)

Due by **EOD, Tue April 8**.

# Scales & Axes

# Scale Transforms

$$f: D \rightarrow R$$

A **scale** is a function that maps a domain  $D$  of data values to a range  $R$  of visual values.

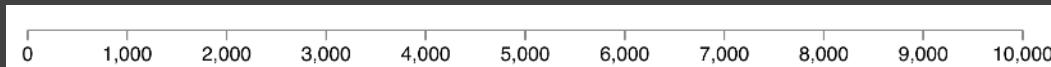
Example ranges: x-position, color, size, angle

Scales are the workhorses of visual encoding!

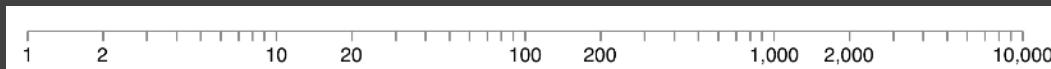
We can modify domains, ranges, transforms (*log*, etc.), padding, and more...

# Positional Scales $R = pixels$

## Continuous / Quantitative



linear



log

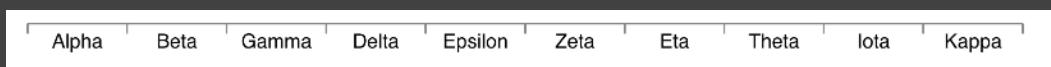


sqrt

## Discrete / Ordinal



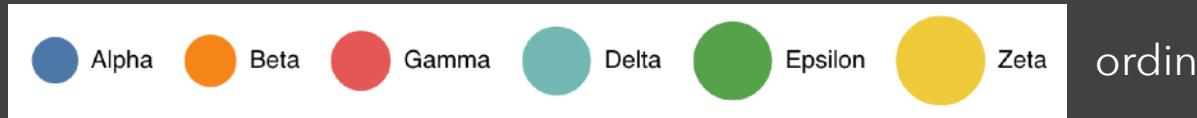
point



band

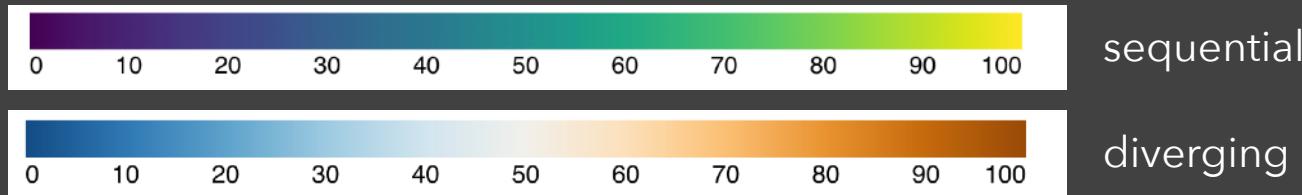
# Color Scales $R = \text{colors}$

## Discrete / Categorical



ordinal

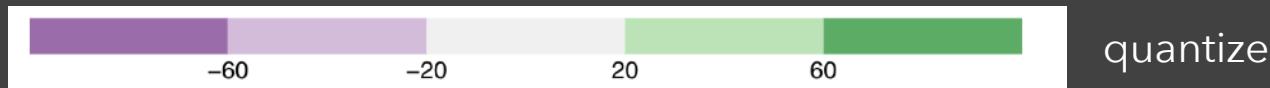
## Continuous / Quantitative



sequential

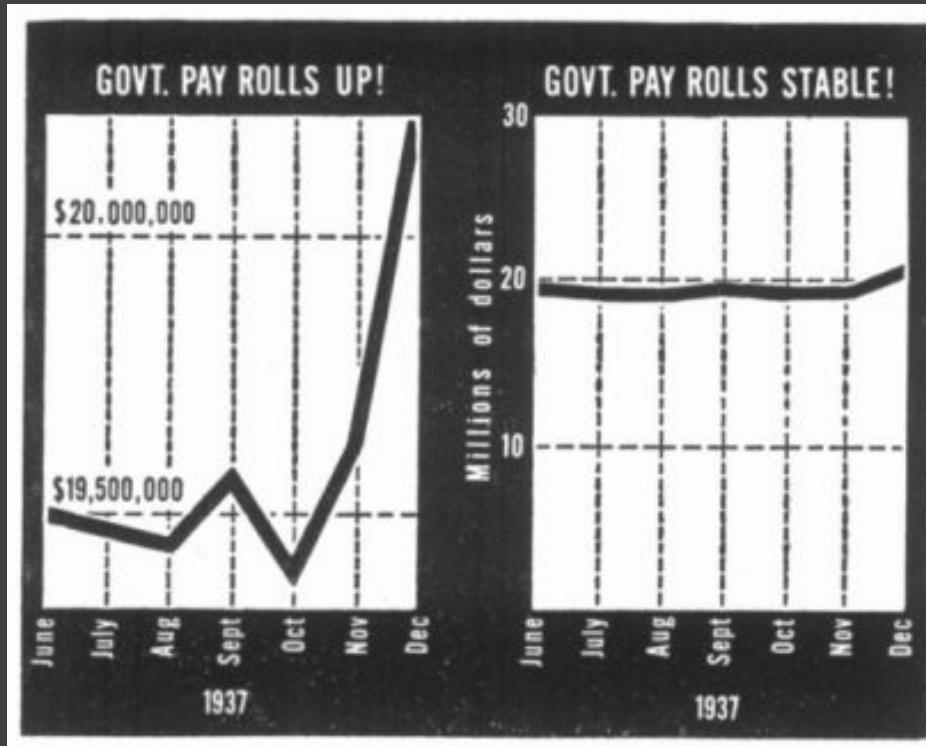
diverging

## Discretized / Binned Quantitative



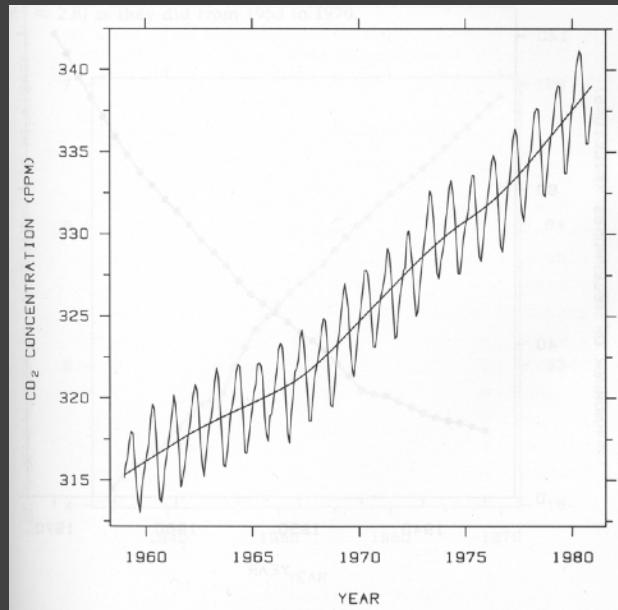
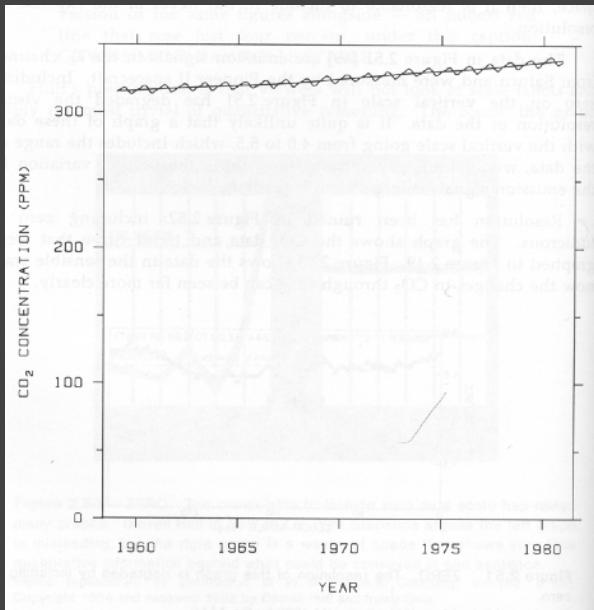
quantize

# Include Zero in Axis Scale?



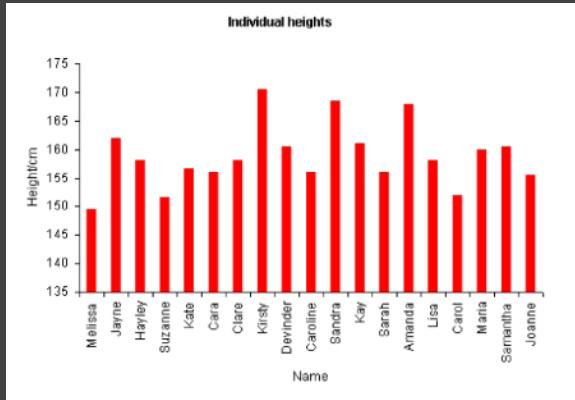
Government payrolls in 1937 [How To Lie With Statistics. Huff]

# Include Zero in Axis Scale?

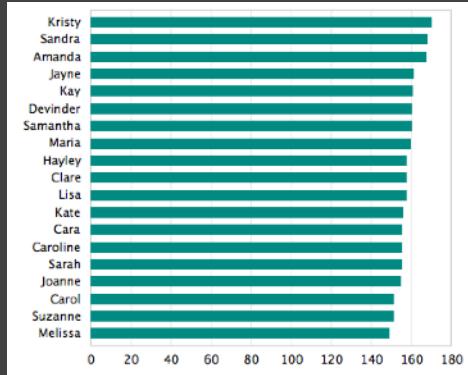


Yearly CO<sub>2</sub> concentrations [Cleveland 85]

# Include Zero in Axis Scale?

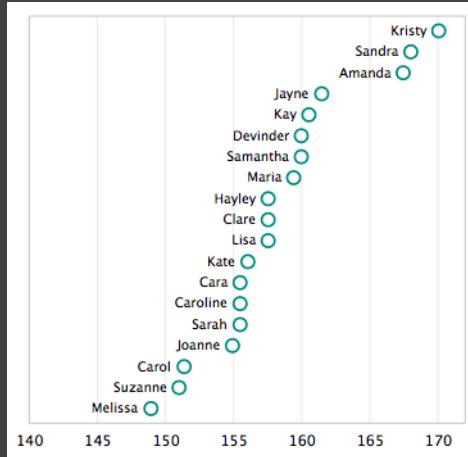


Compare  
Proportions  
(Q-Ratio)

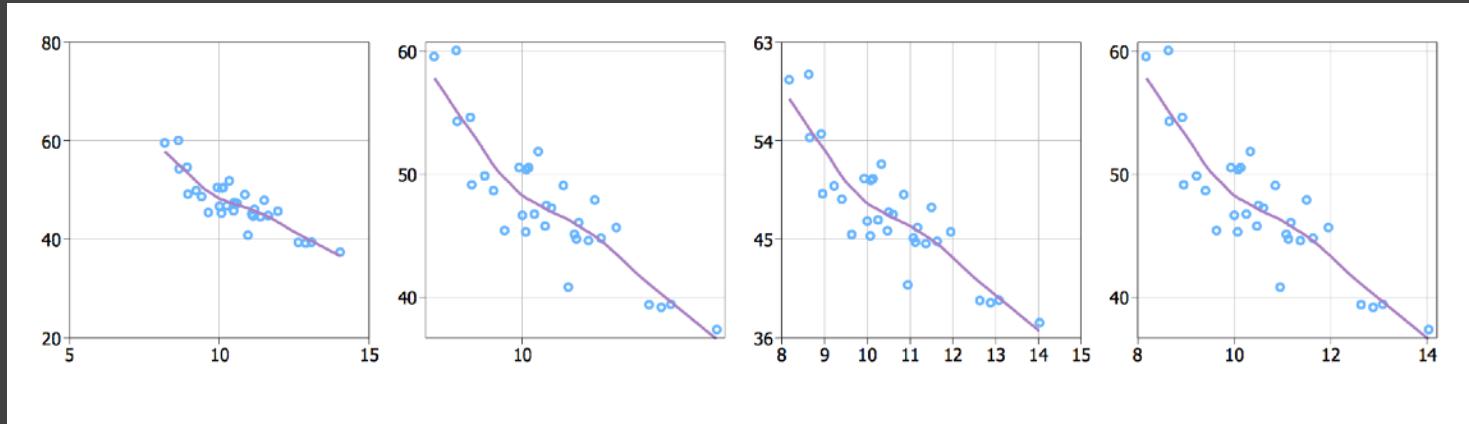


Violates Expressiveness Principle!

Compare  
Relative  
Position  
(Q-Interval)

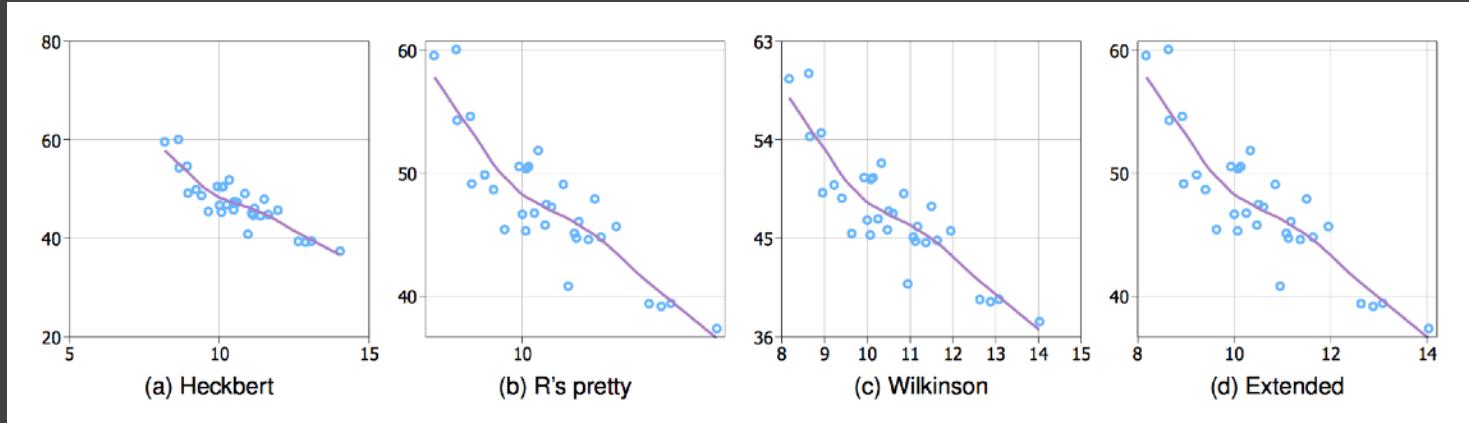


# Axis Tick Mark Selection



What are some properties of "good" tick marks?

# Axis Tick Mark Selection



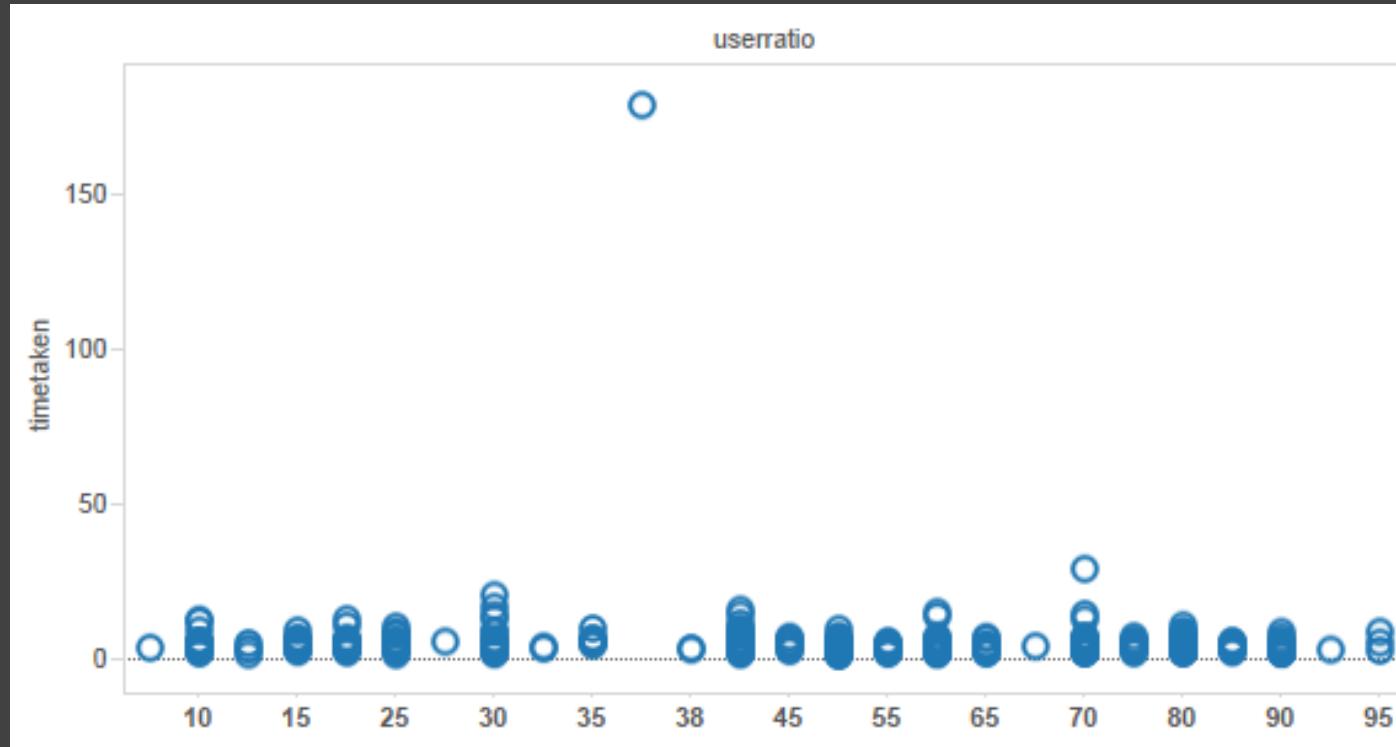
**Simplicity** - numbers are multiples of 10, 5, 2

**Coverage** - ticks near the ends of the data

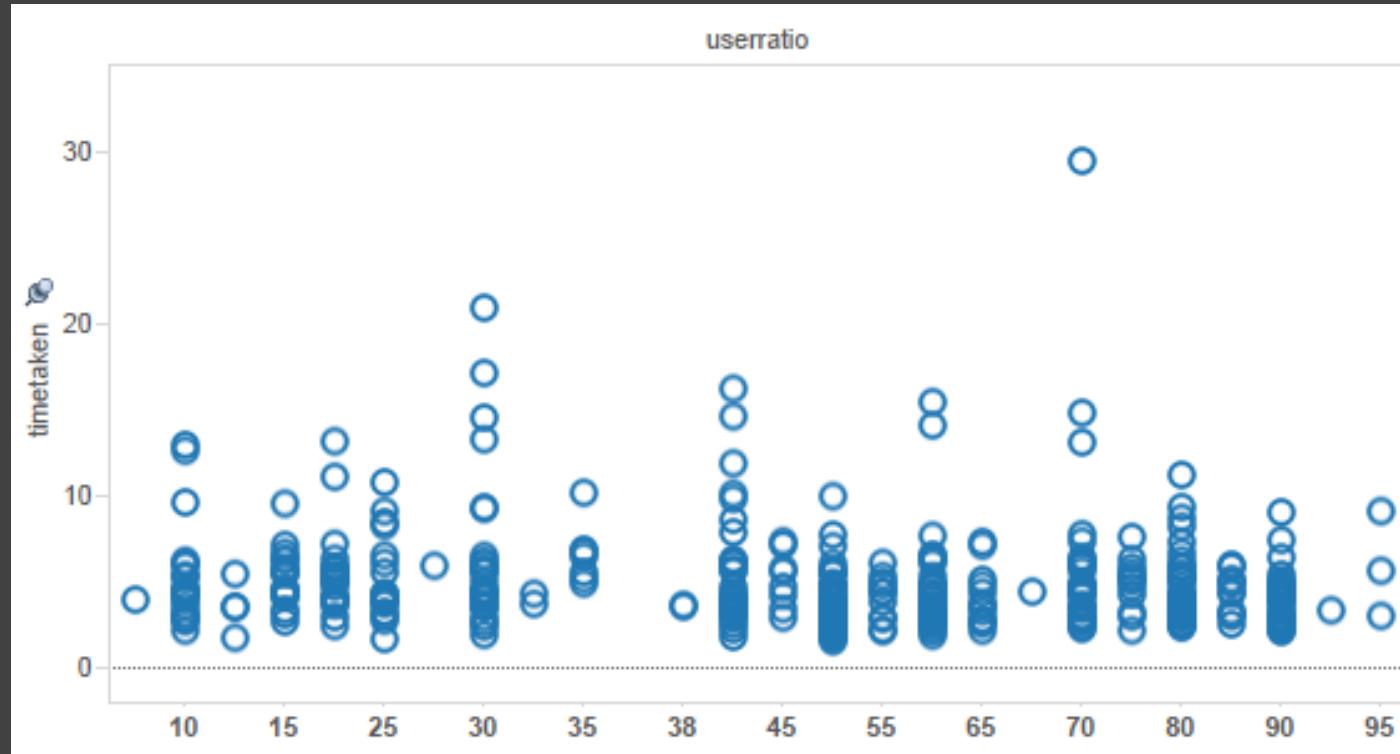
**Density** - not too many, nor too few

**Legibility** - whitespace, horizontal text, size

# How to Scale the Axis?

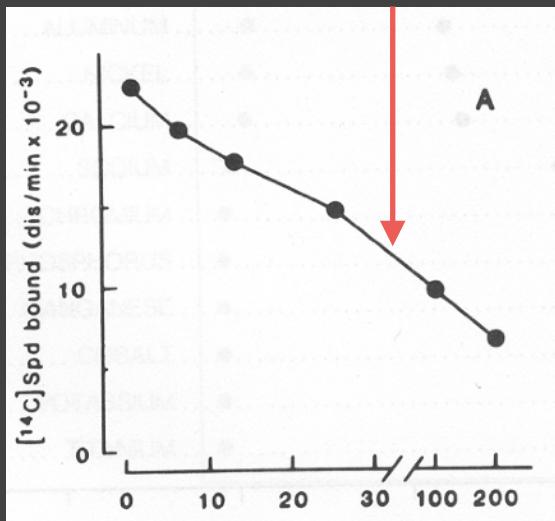


# One Option: Clip Outliers

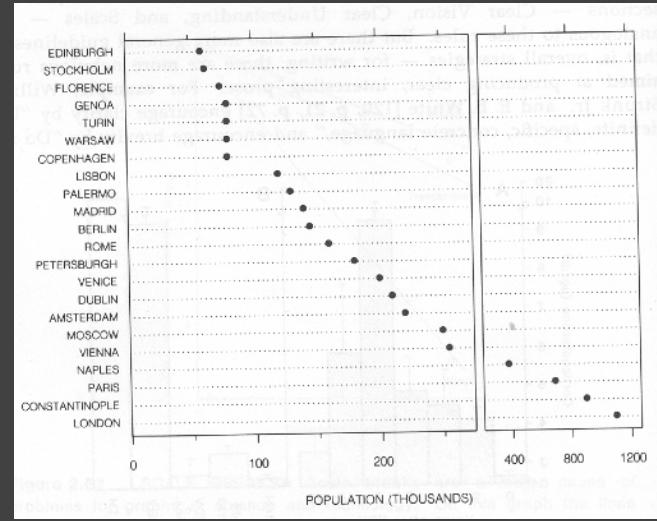


# Clearly Mark Scale Breaks

Violates Expressiveness Principle!

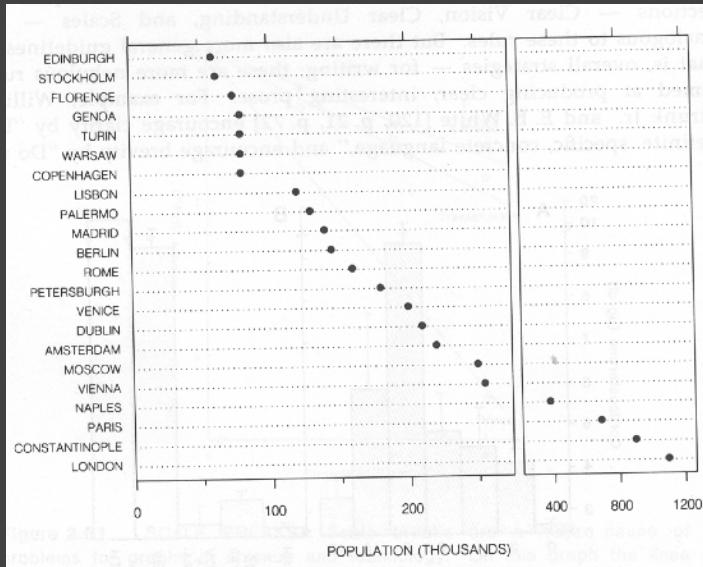


Poor scale break [Cleveland 85]

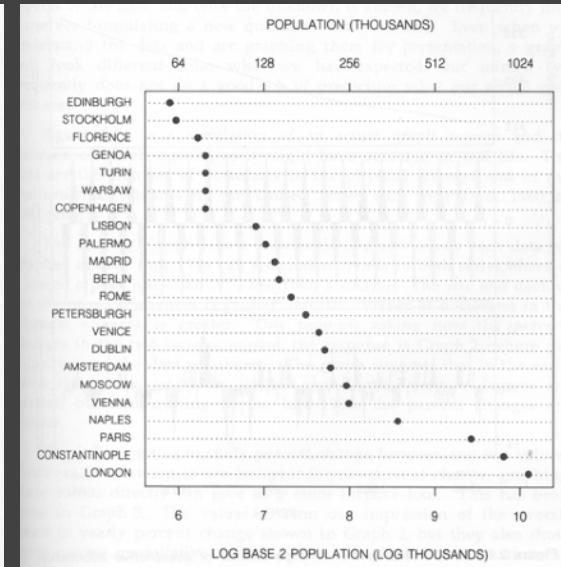


Well-marked scale break [Cleveland 85]

# Scale Break vs. Log Scale



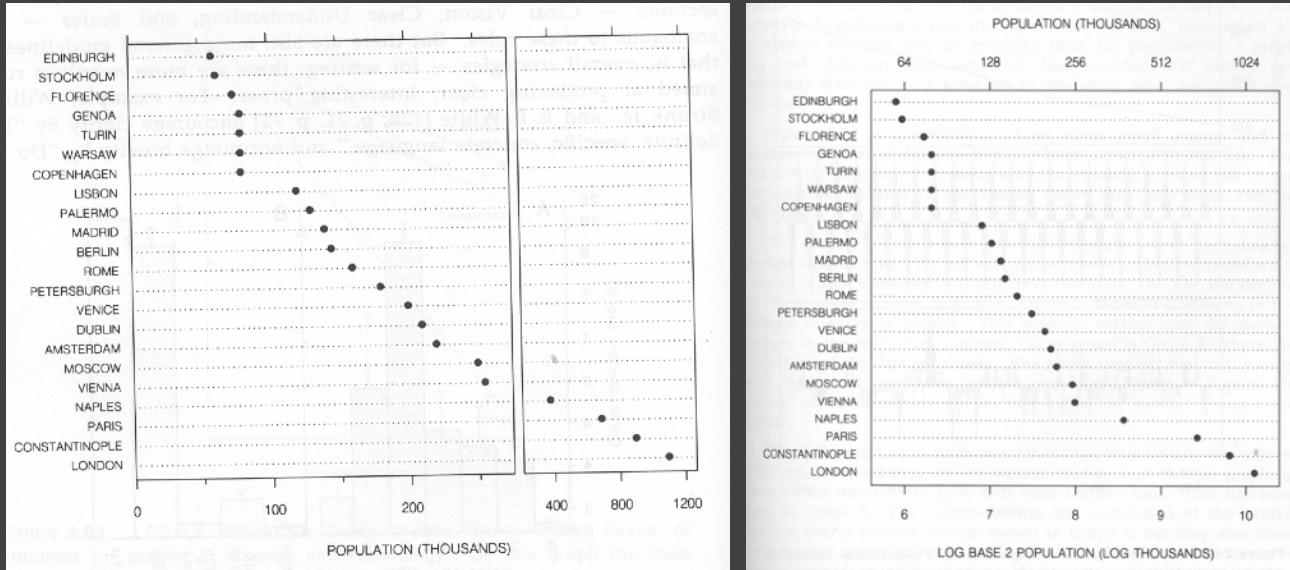
Scale Break



Log Scale

[Cleveland 85]

# Scale Break vs. Log Scale



**Both increase visual resolution**

Scale break: difficult to compare (*cognitive* – not *perceptual* – work)  
Log scale: direct comparison of all data

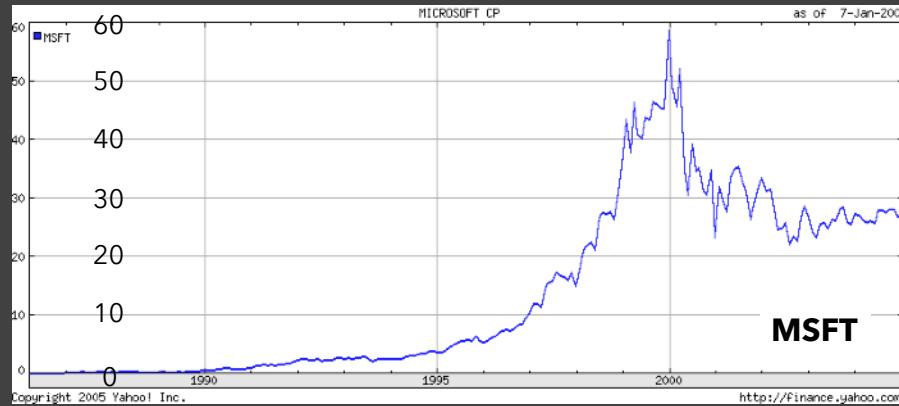
Logarithms turn *multiplication* into *addition*.

$$\log(x \cdot y) = \log(x) + \log(y)$$

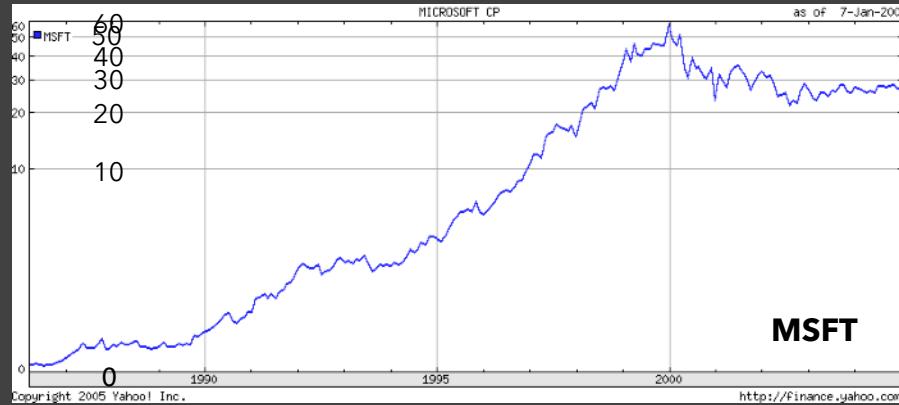
Equal steps on a log scale correspond to equal changes to a multiplicative scale factor.

# Linear Scale vs. Log Scale

Linear Scale



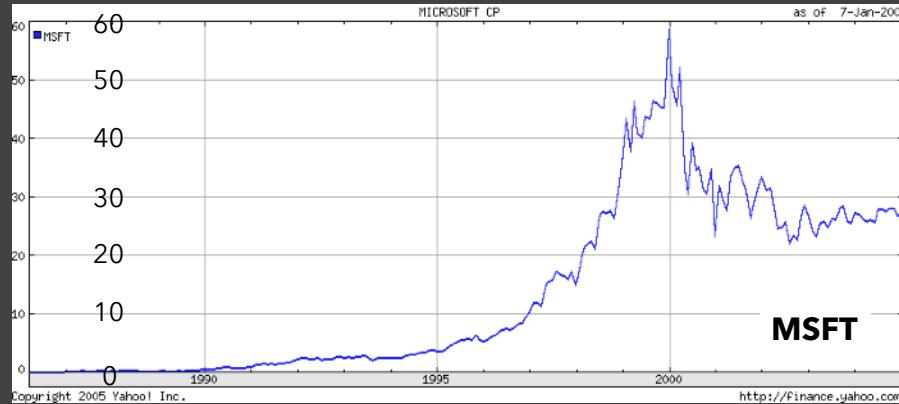
Log Scale



# Linear Scale vs. Log Scale

## Linear Scale

Absolute change

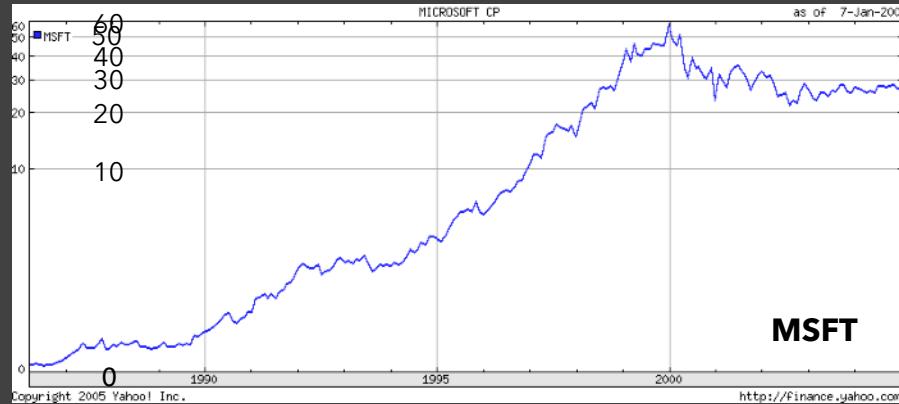


## Log Scale

Small fluctuations

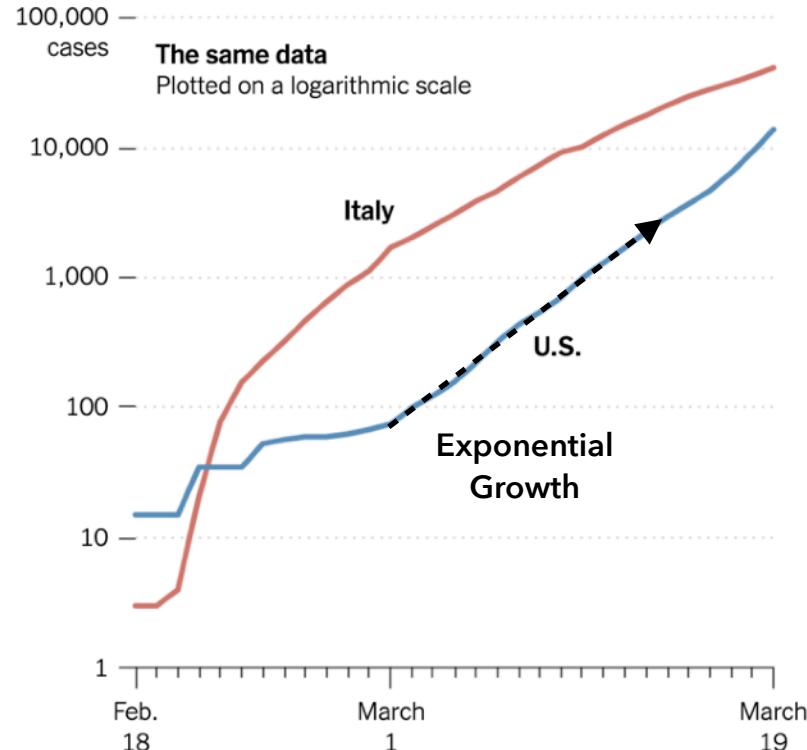
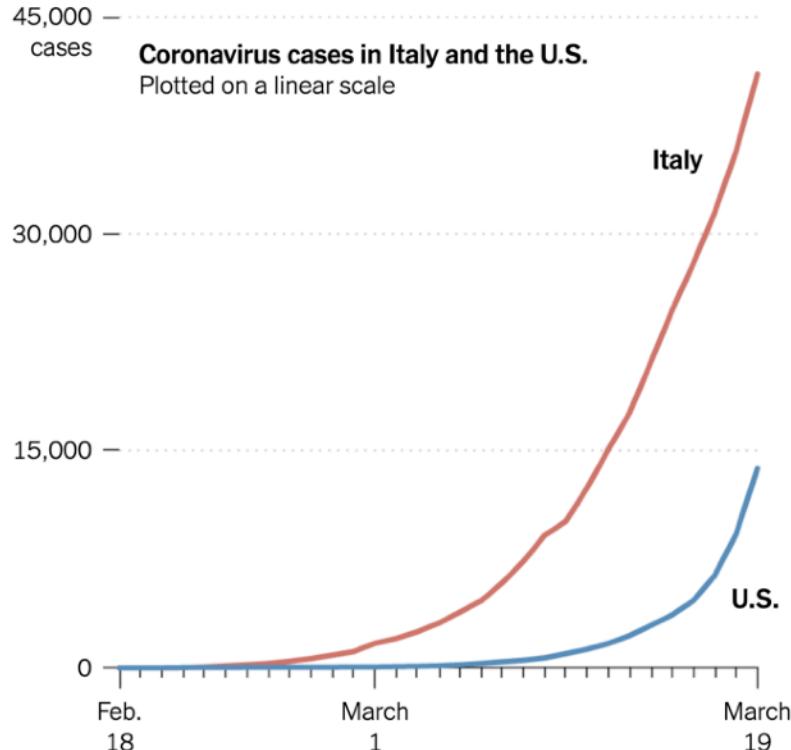
Percent change

$$d(10,30) > d(30,60)$$



## Bending the Curve

Logarithmic scales can emphasize the rate of change in a way that linear scales do not. Italy seems to be slowing the coronavirus infection rate, while the number of cases in the United States continues to double every few days.



# When To Apply a Log Scale?

**Address data skew** (e.g., long tails, outliers)

Enables comparison within and across multiple orders of magnitude.

**Focus on multiplicative factors** (not additive)

Recall that the logarithm transforms  $\times$  to  $+$ !

Percentage change, not linear difference.

Constraint: **positive, non-zero values**

Constraint: **audience familiarity?**

# Visual Encoding Design

Use **expressive** and **effective** encodings

**Reduce** the problem space

Avoid **over-encoding**

Use **space** and **small multiples** intelligently

Use **interaction** to generate *relevant* views

Rarely does a single visualization answer all questions. Instead, the ability to generate appropriate visualizations quickly is critical!

# About the design process...

Visualization draws upon both science and art!

Principles like expressiveness & effectiveness are not hard-and-fast rules, but can assist us to guide the process and articulate alternatives.

They can lead us to think more deeply about our design rationale and prompt us to reflect.

**It helps to know “the rules” in order to wisely bend (or break) them at the right times!**