

CSE 512 - Data Visualization

Color



Jeffrey Heer University of Washington

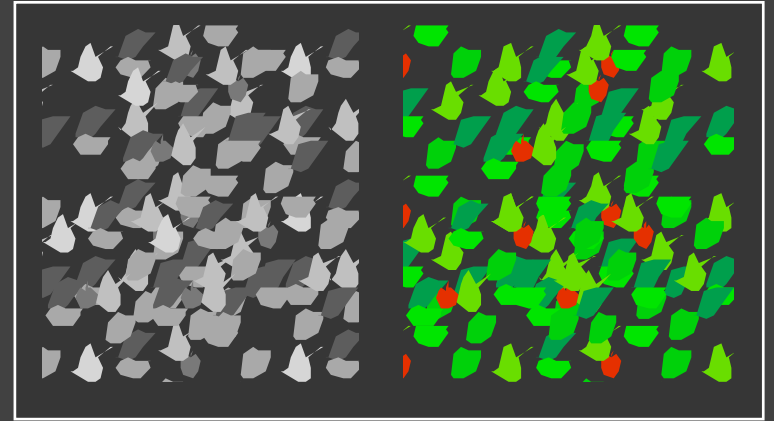
Purpose of Color

To label

To measure

To represent and imitate

To enliven and decorate



"Above all, do no harm."

- Edward Tufte

Topics

Perception of Color

Light, Visual system, Mental models

Color in Information Visualization

Categorical & Quantitative encoding

Guidelines for color palette design

Perception of Color

What color is this?

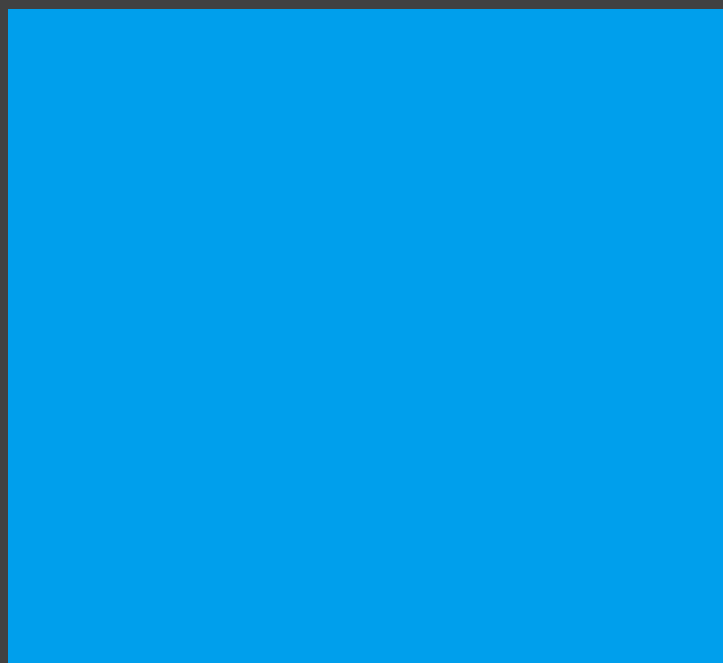


What color is this?

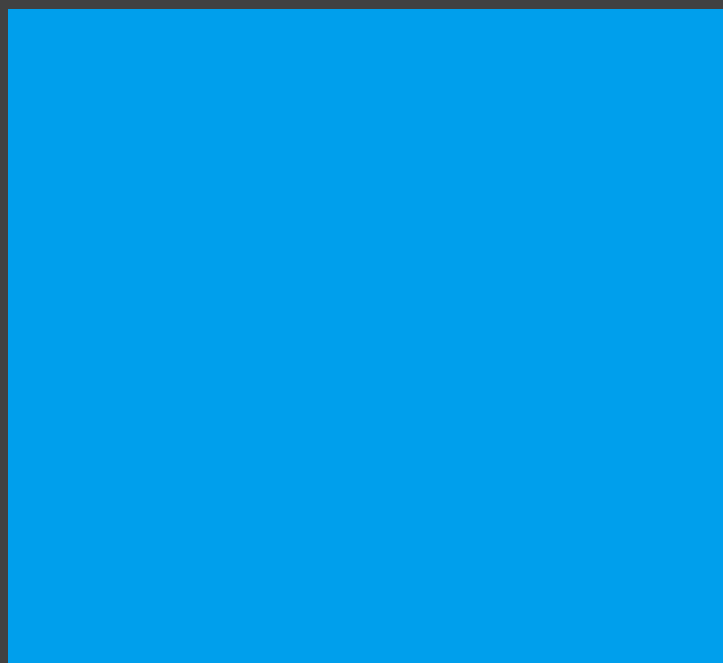


"Yellow"

What color is this?

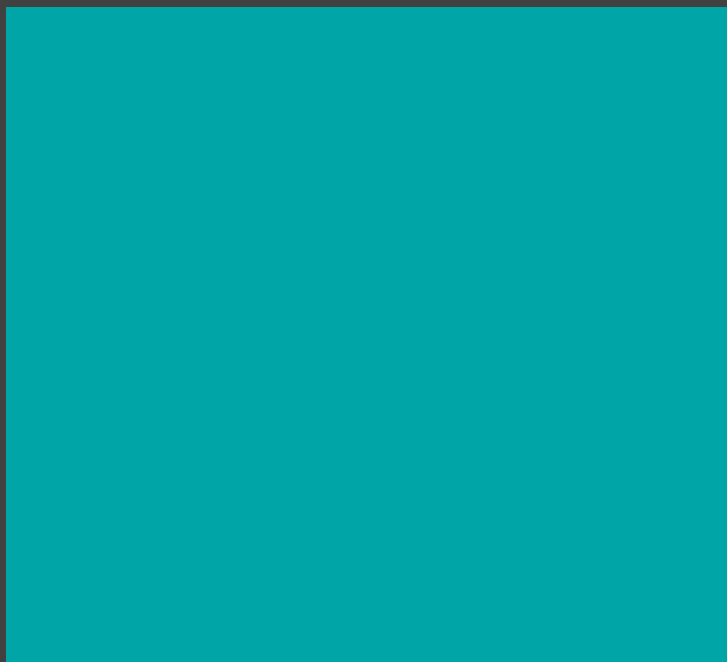


What color is this?



"Blue"

What color is this?

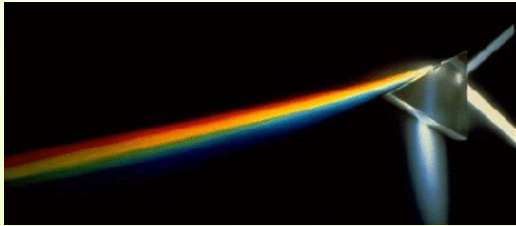


What color is this?

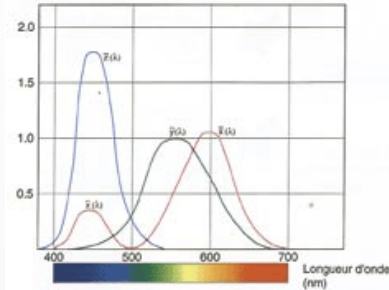


"Teal" ?

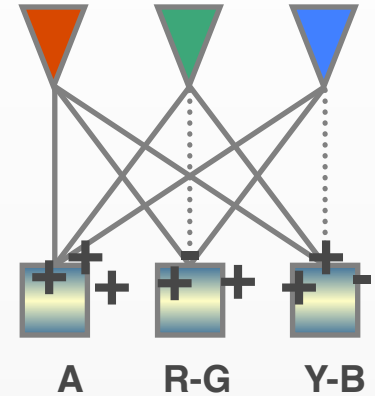
Perception of Color



Light



Cone Response



Opponent Signals

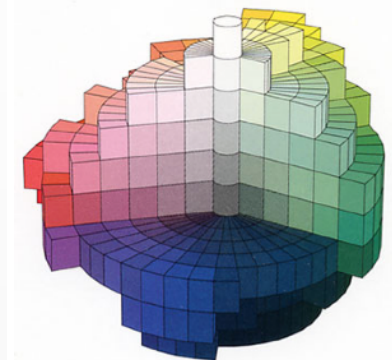
“Yellow”

Color Cognition



Mark D. Fairchild
**COLOR APPEARANCE
MODELS**

Color Appearance



Color Perception

Physicist's View

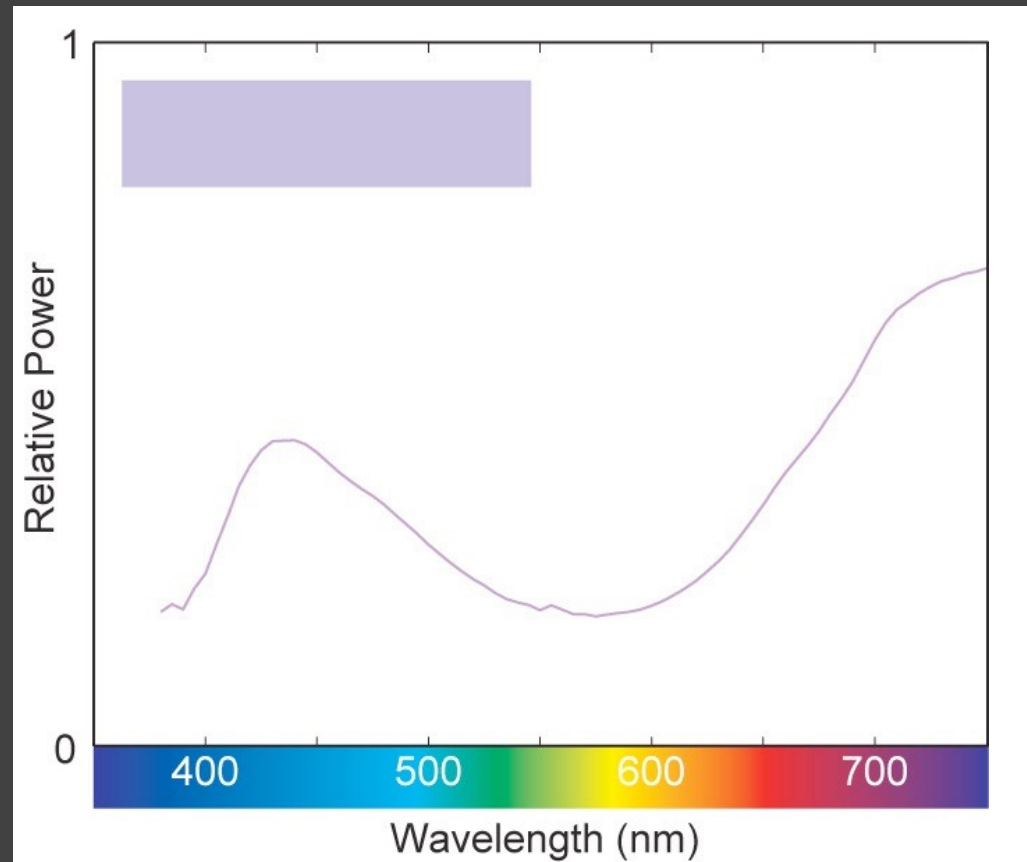
Light as electromagnetic waves

Wavelength

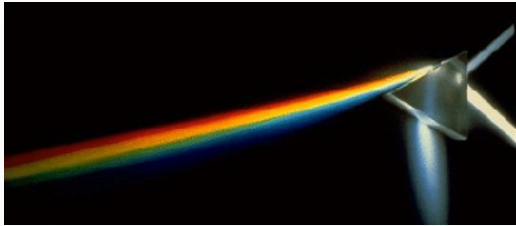
Visible spectrum is
370-730 nm

Power or

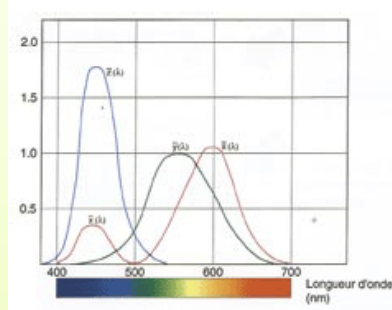
"Relative luminance"



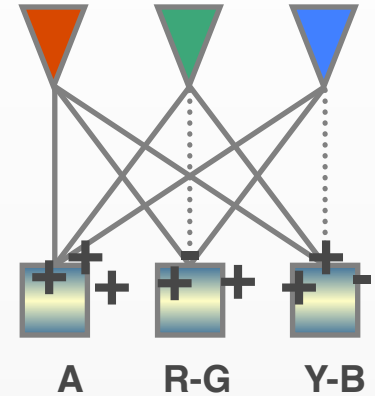
Perception of Color



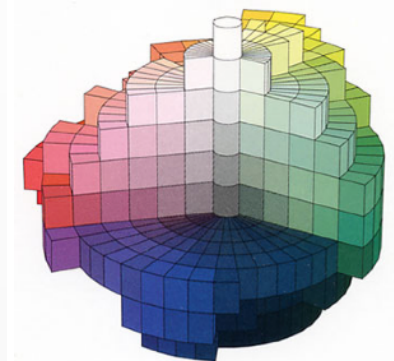
Light



Cone Response



Opponent Signals



Color Perception

“Yellow”

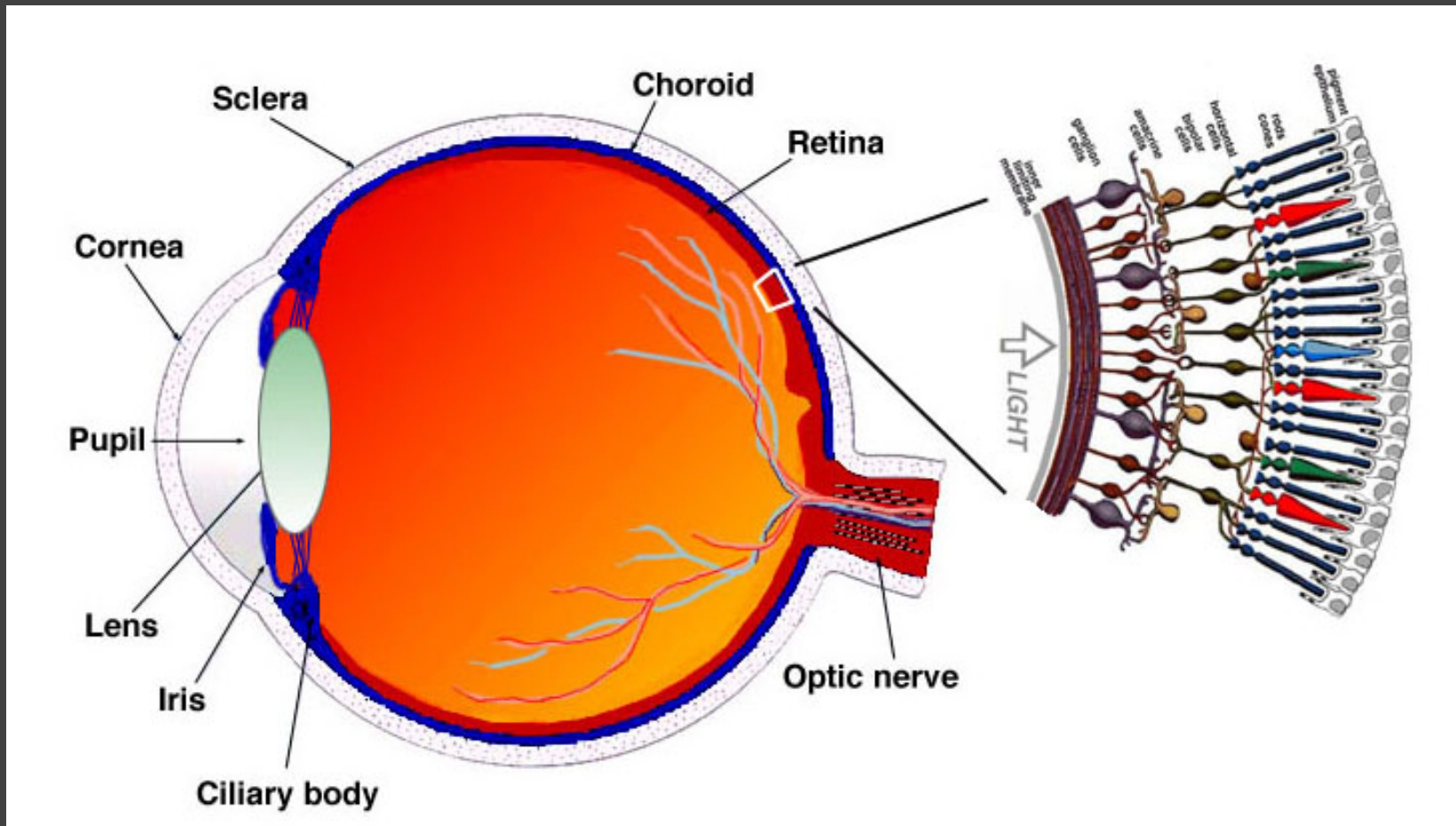
Color Cognition



Mark D. Fairchild
COLOR APPEARANCE
MODELS

Color Appearance

Retina

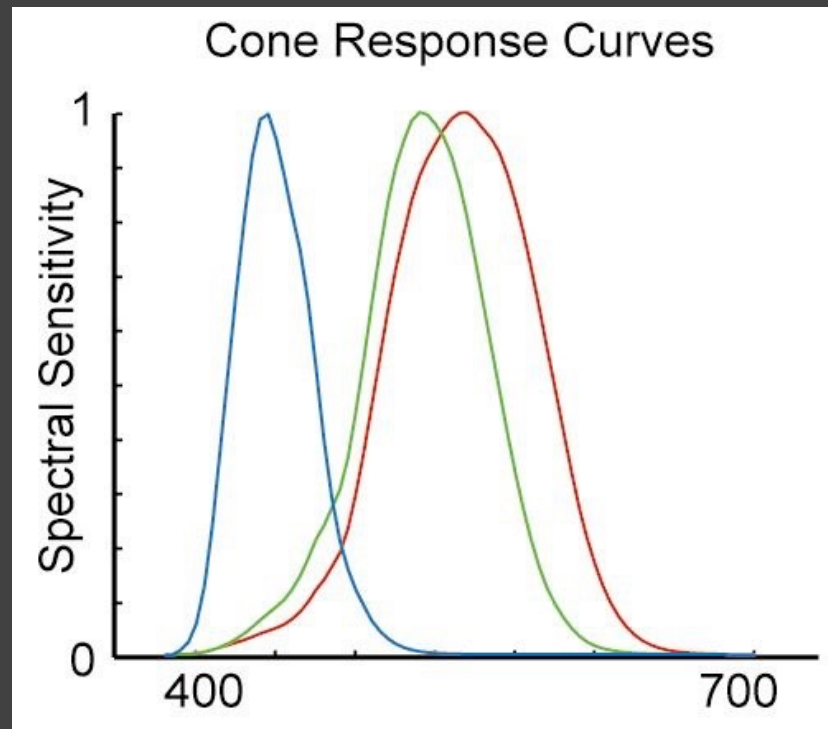


Simple Anatomy of the Retina, Helga Kolb

As light enters our retina...

LMS (Long, Middle, Short) Cones

Sensitive to different wavelengths

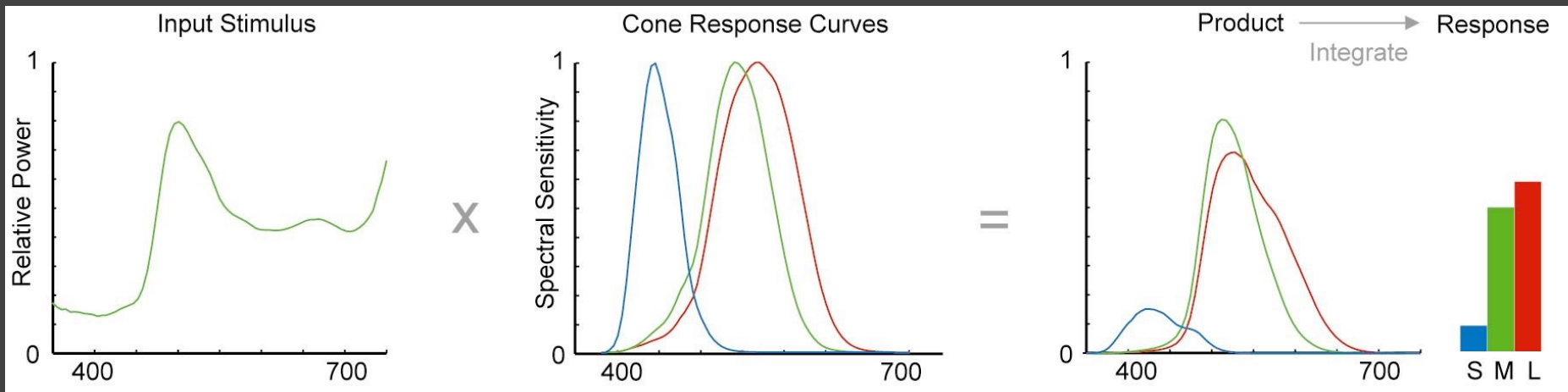


As light enters our retina...

LMS (Long, Middle, Short) Cones

Sensitive to different wavelengths

Integration with input stimulus



Effects of Retina Encoding

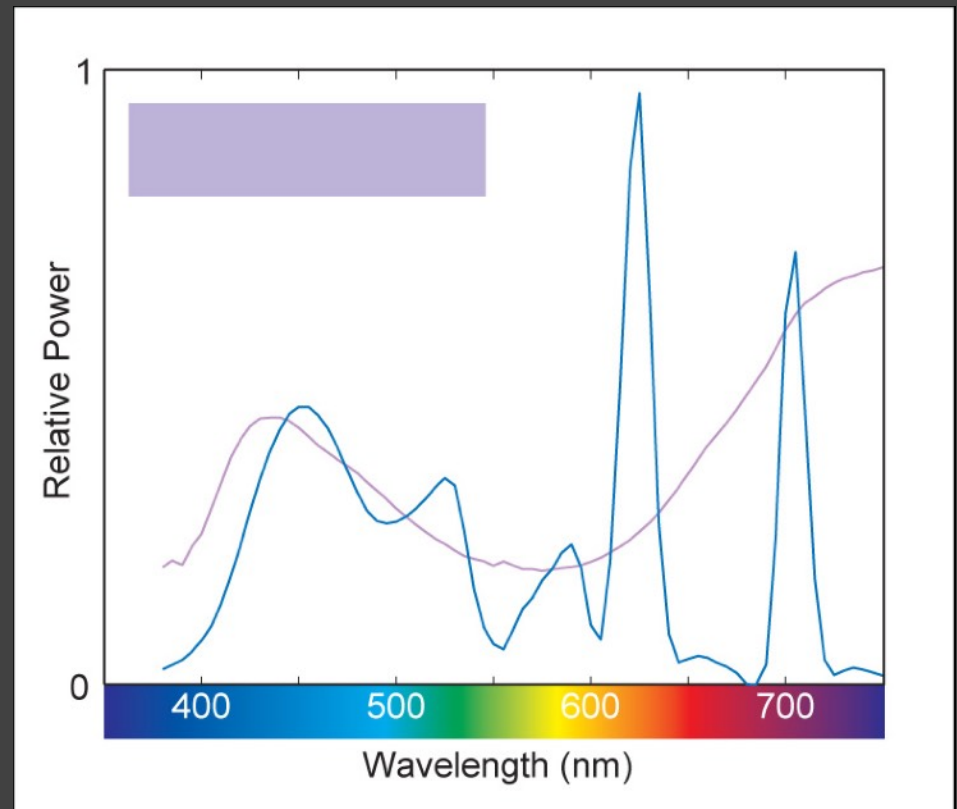
Spectra that stimulate the same LMS response are indistinguishable (a.k.a. "metamers").

"Tri-stimulus"

Computer displays

Digital scanners

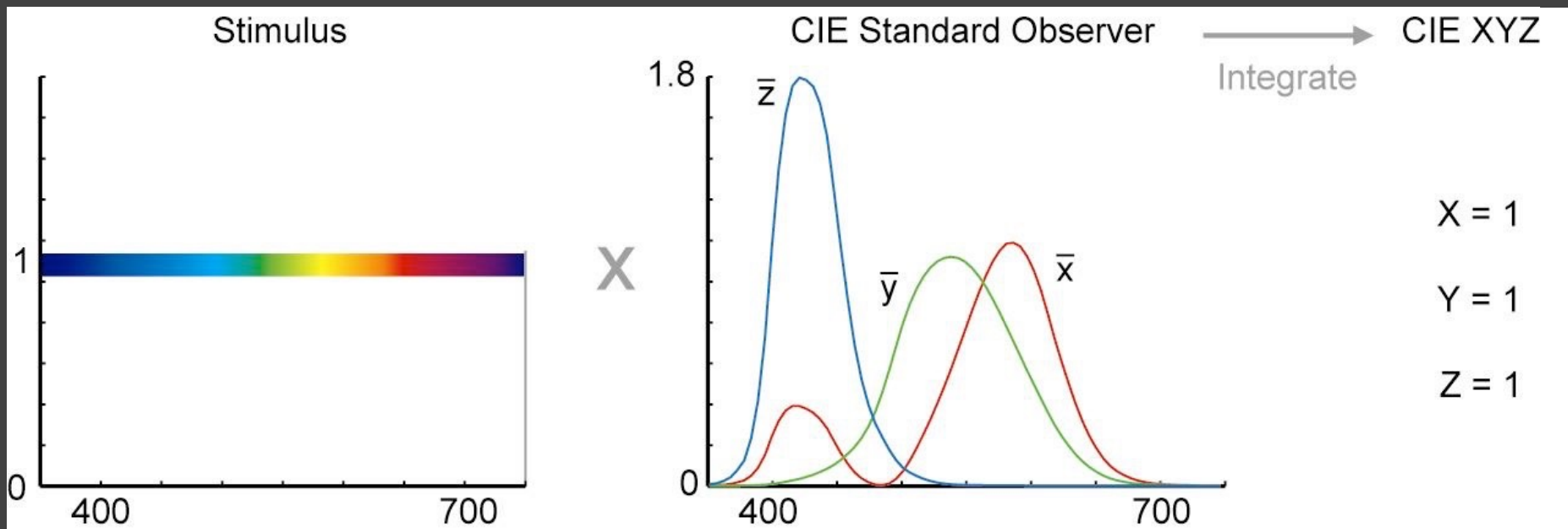
Digital cameras



CIE XYZ Color Space

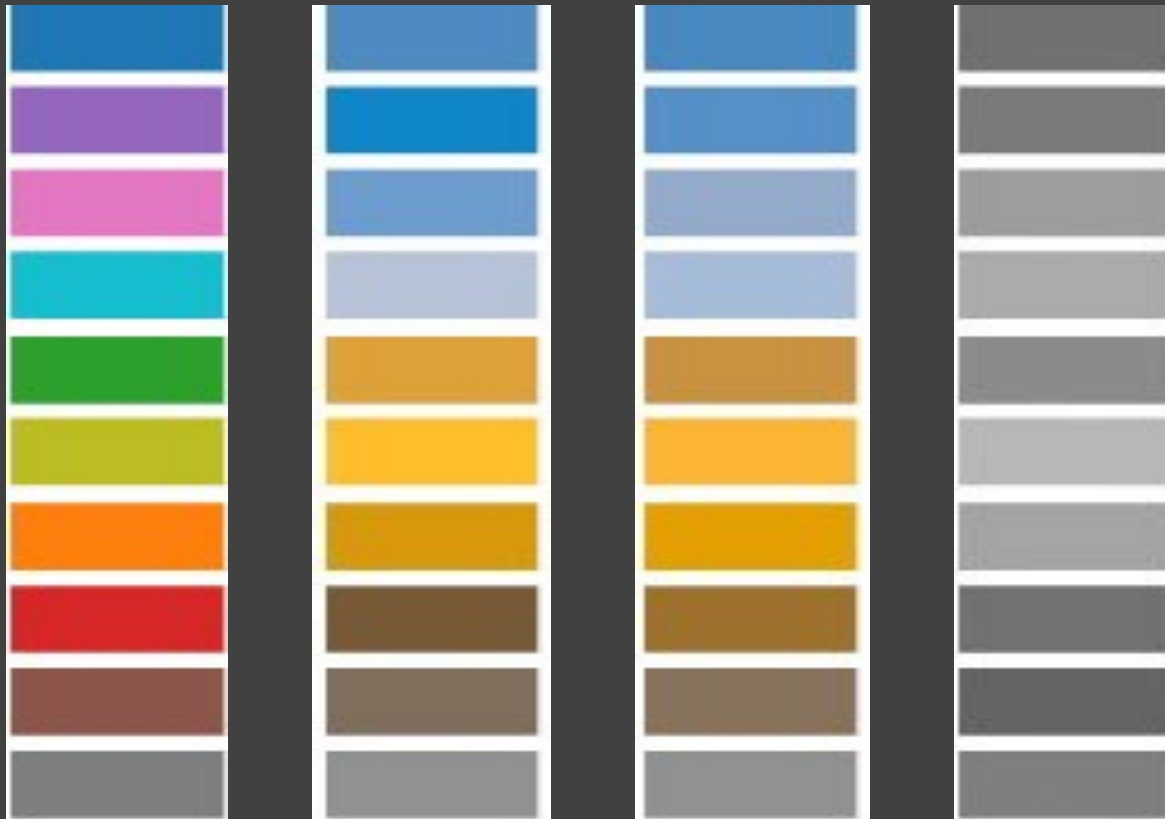
Standardized in 1931 to mathematically represent tri-stimulus response from cones on the retina.

“Standard observer” response curves



Color Vision Deficiency (CVD)

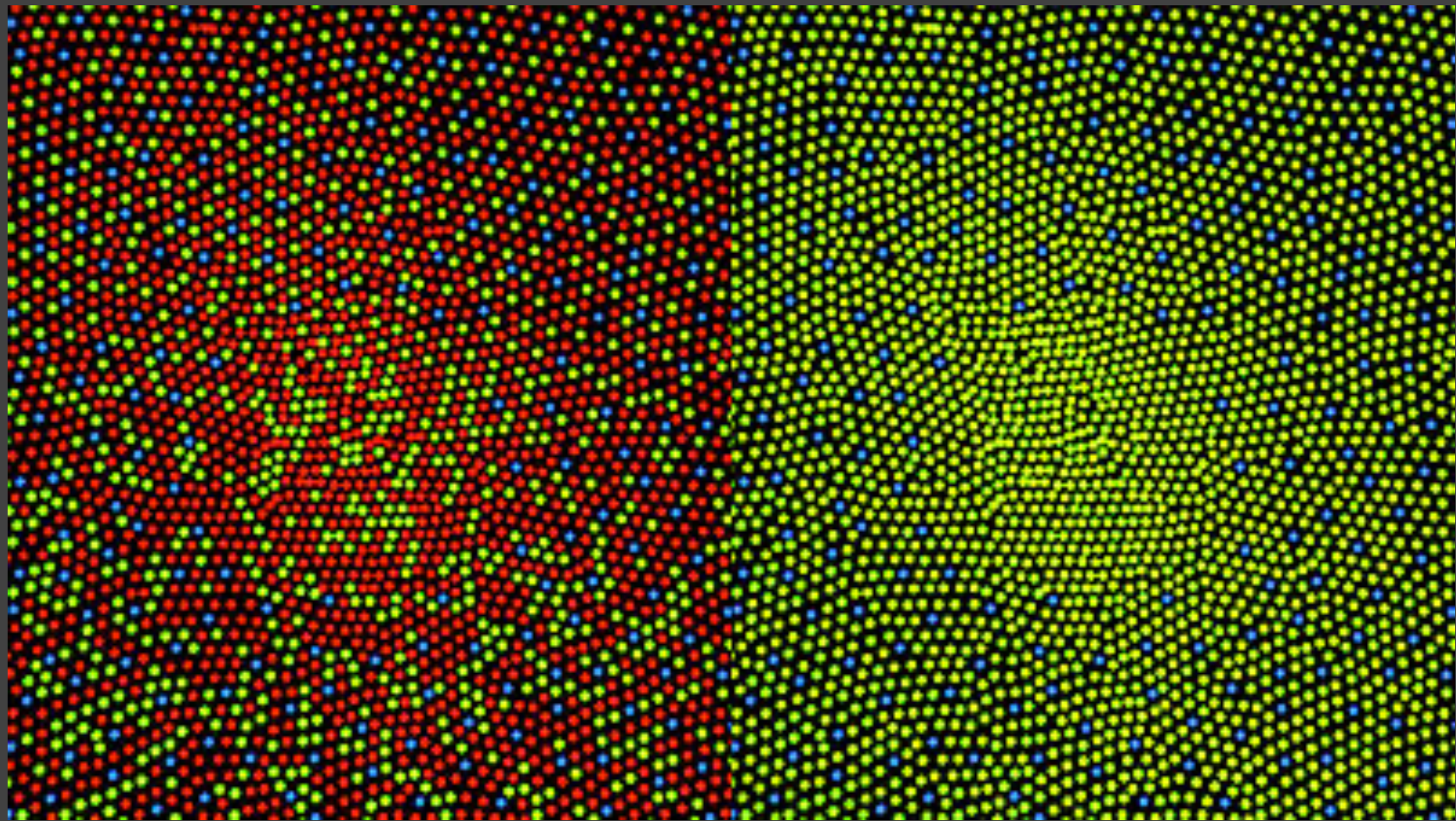
Missing one or more cones or rods in retina.



Protanope

Deuteranope

Luminance



Normal Retina

Protanopia

Color Vision Simulators

Simulate color vision deficiencies

Browser plug-ins

Photoshop plug-ins, etc.



Deuteranope



Protanope

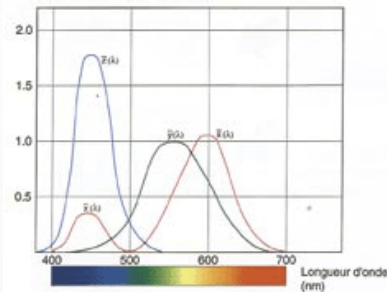


Tritanope

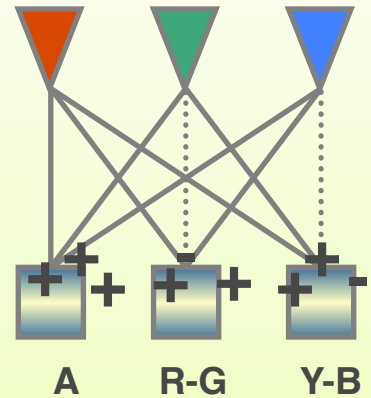
Perception of Color



Light



Cone Response



Opponent Signals

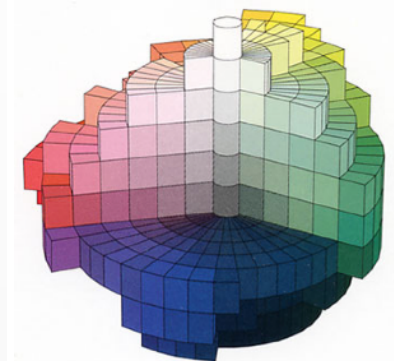
“Yellow”

Color Cognition



Mark D. Fairchild
COLOR APPEARANCE
MODELS

Color Appearance



Color Perception

Primary Colors

To paint "all colors":

Leonardo da Vinci, circa 1500 described in his notebooks a list of simple colors...

Yellow

Blue

Green

Red

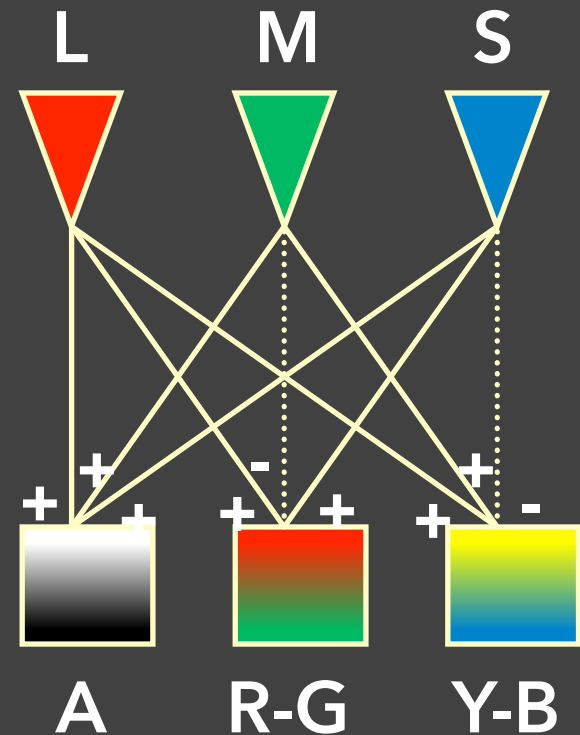
Opponent Processing Theory

LMS are combined to create:

Lightness

Red-green contrast

Yellow-blue contrast



[Fairchild]

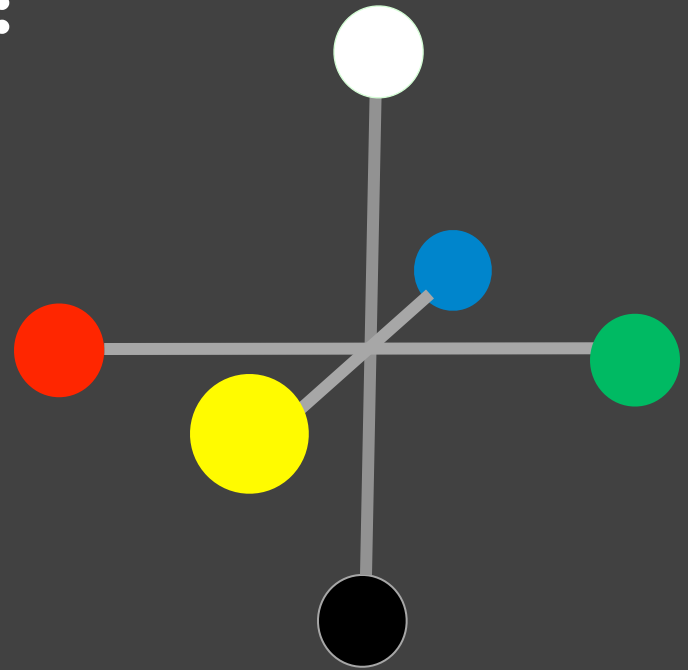
Opponent Processing Theory

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Opponent Processing Theory

LMS are combined to create:

Lightness

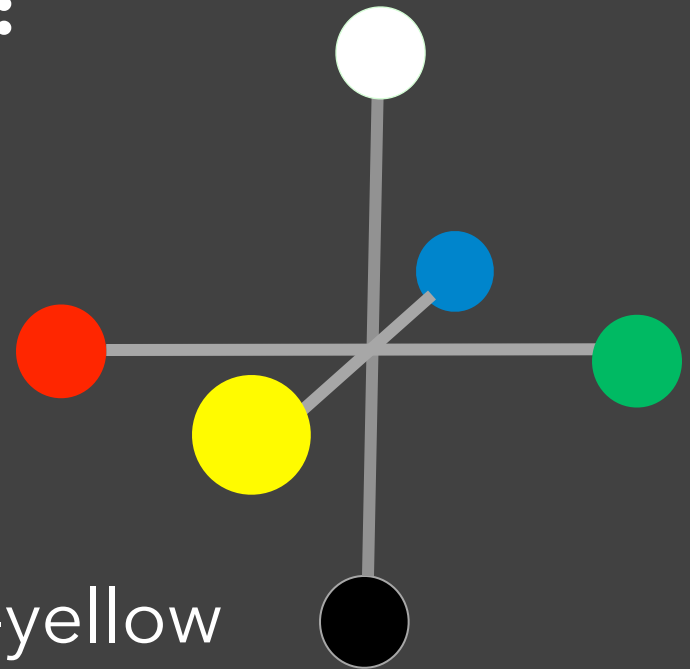
Red-green contrast

Yellow-blue contrast

Experiments:

No reddish-green, no blueish-yellow

Color after images



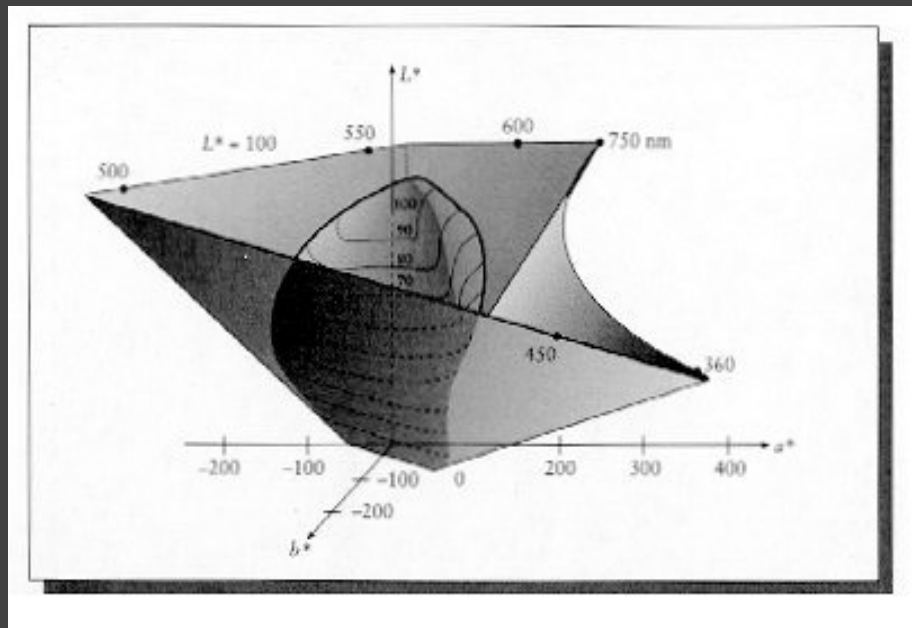
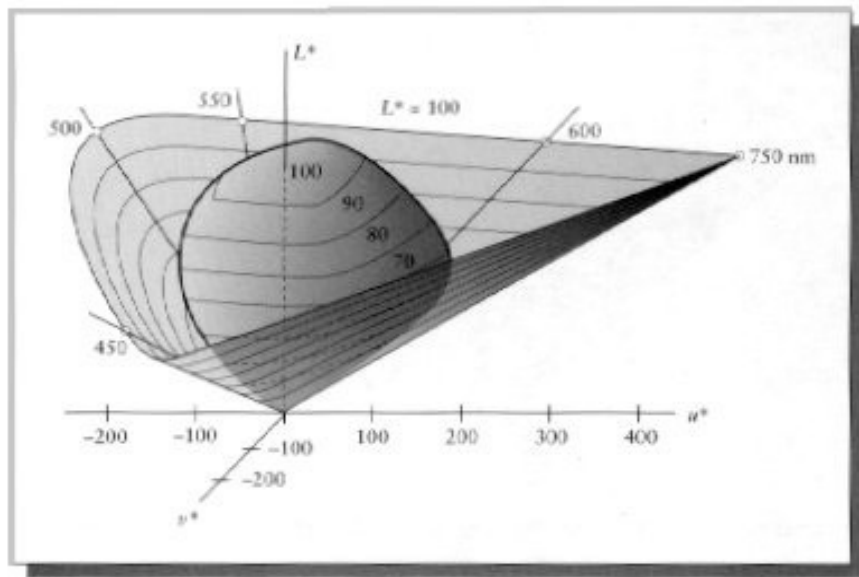




CIE LAB and LUV Color Spaces

Standardized in 1976 to mathematically represent opponent processing theory.

Non-linear transformation of CIE XYZ



CIE LAB Color Space

Axes correspond to opponent signals

L* = Luminance

a* = Red-green contrast

b* = Yellow-blue contrast

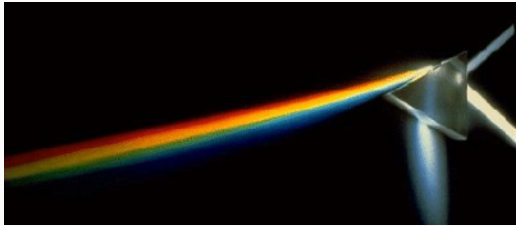
Much more perceptually uniform than sRGB!

Scaling of axes to represent "color distance"

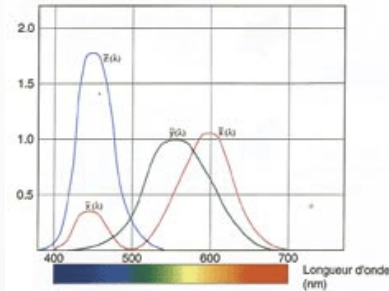
JND = Just noticeable difference (~2.3 units)

D3 + Vega include LAB color space support!

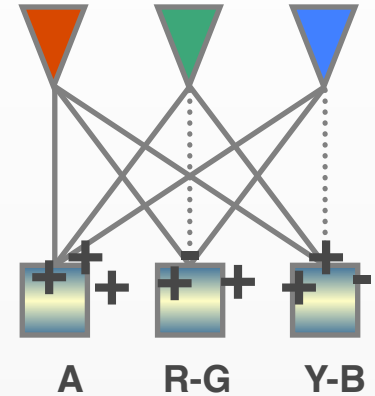
Perception of Color



Light



Cone Response



Opponent Signals

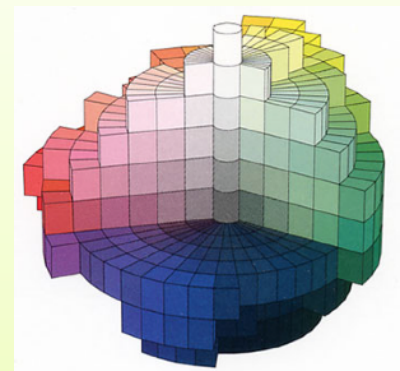
“Yellow”

Color Cognition



Mark D. Fairchild
COLOR APPEARANCE
MODELS

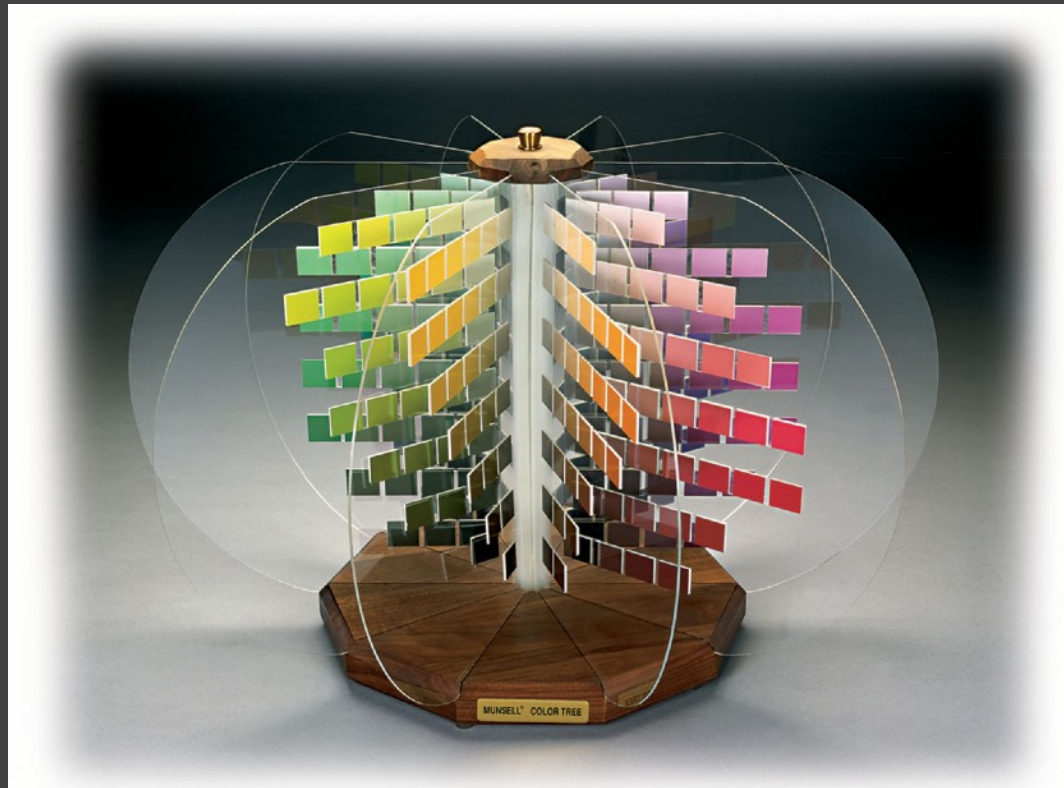
Color Appearance



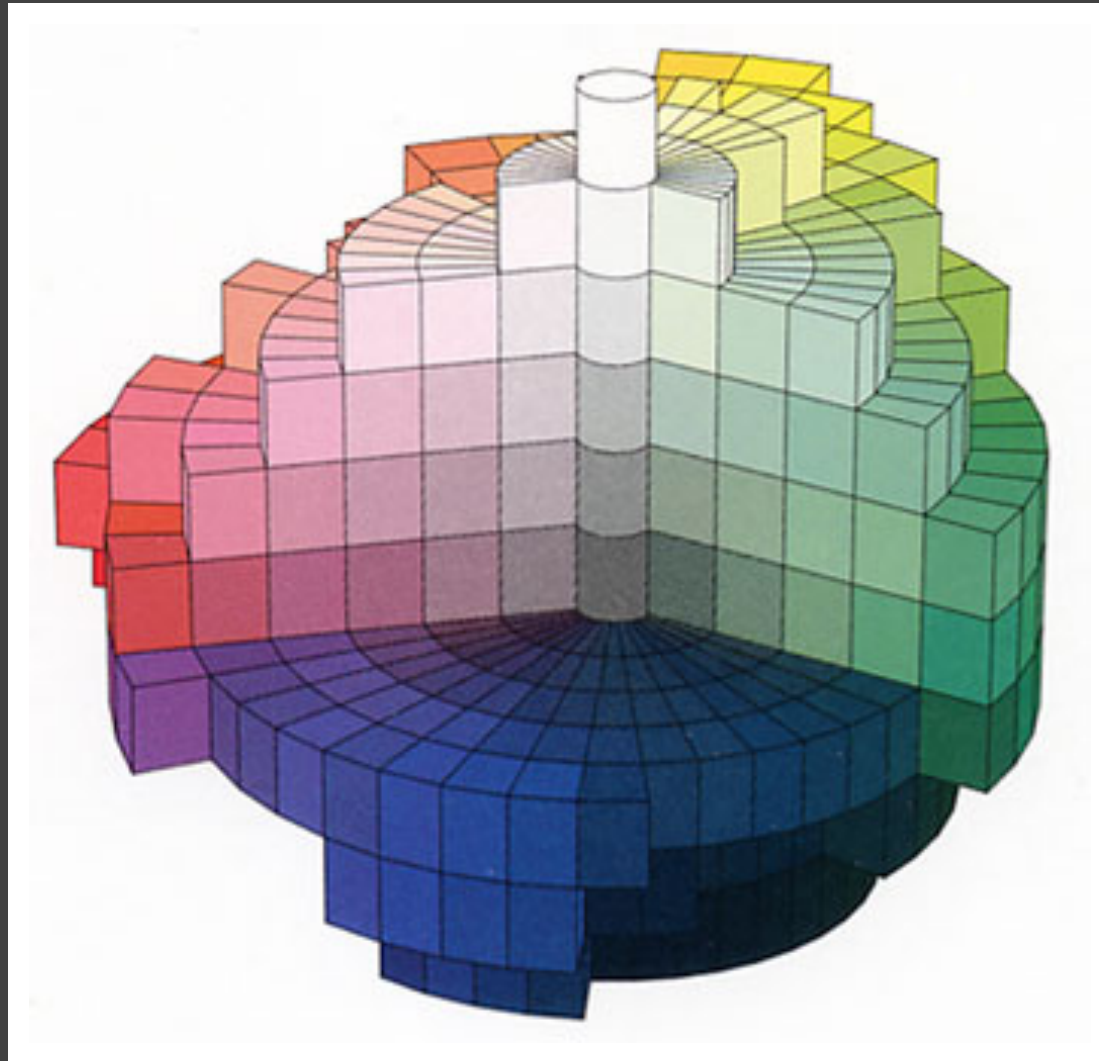
Color Perception

Albert Munsell

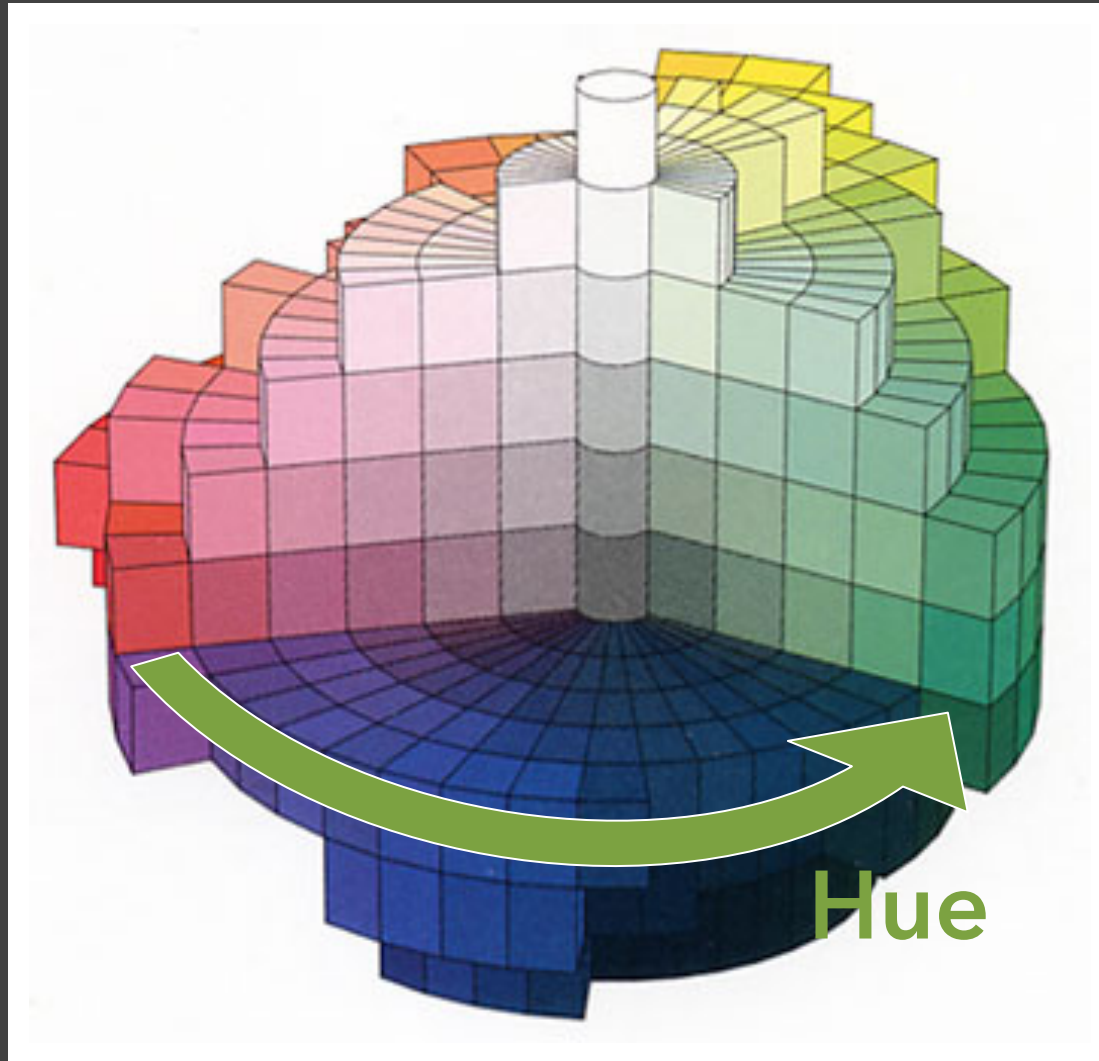
Developed the first perceptual color system based on his experience as an artist (1905).



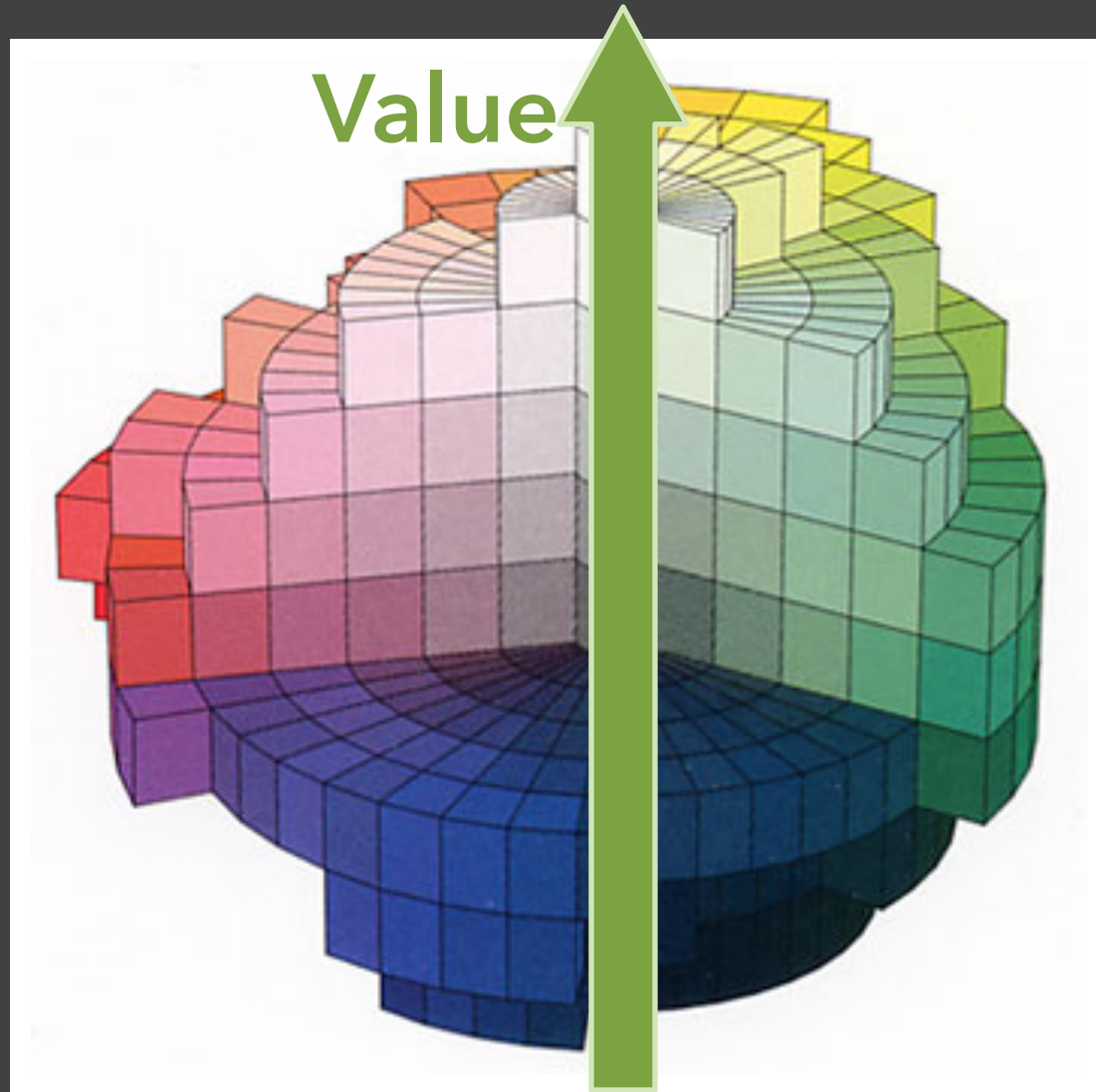
Hue, Value, and Chroma



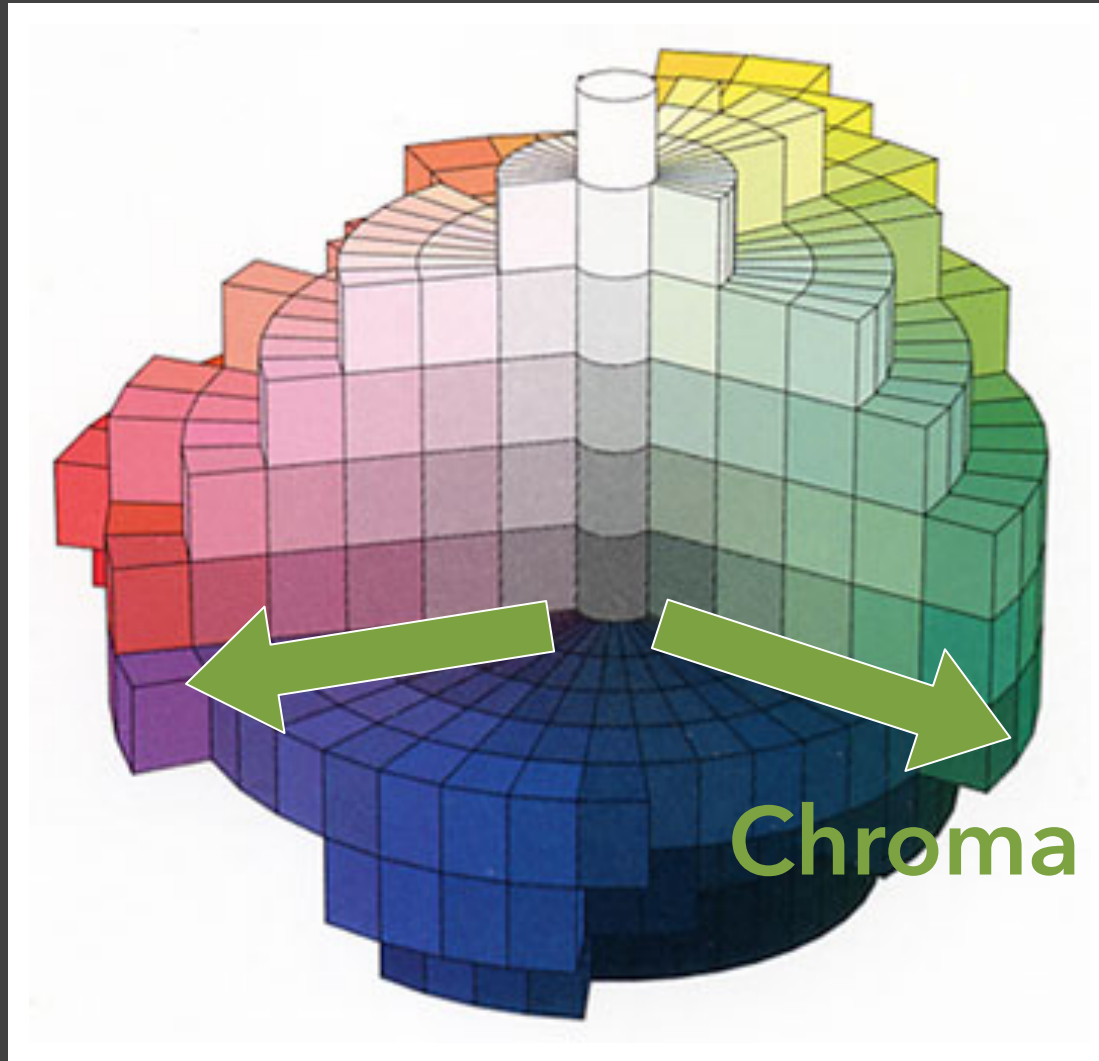
Hue, Value and Chroma



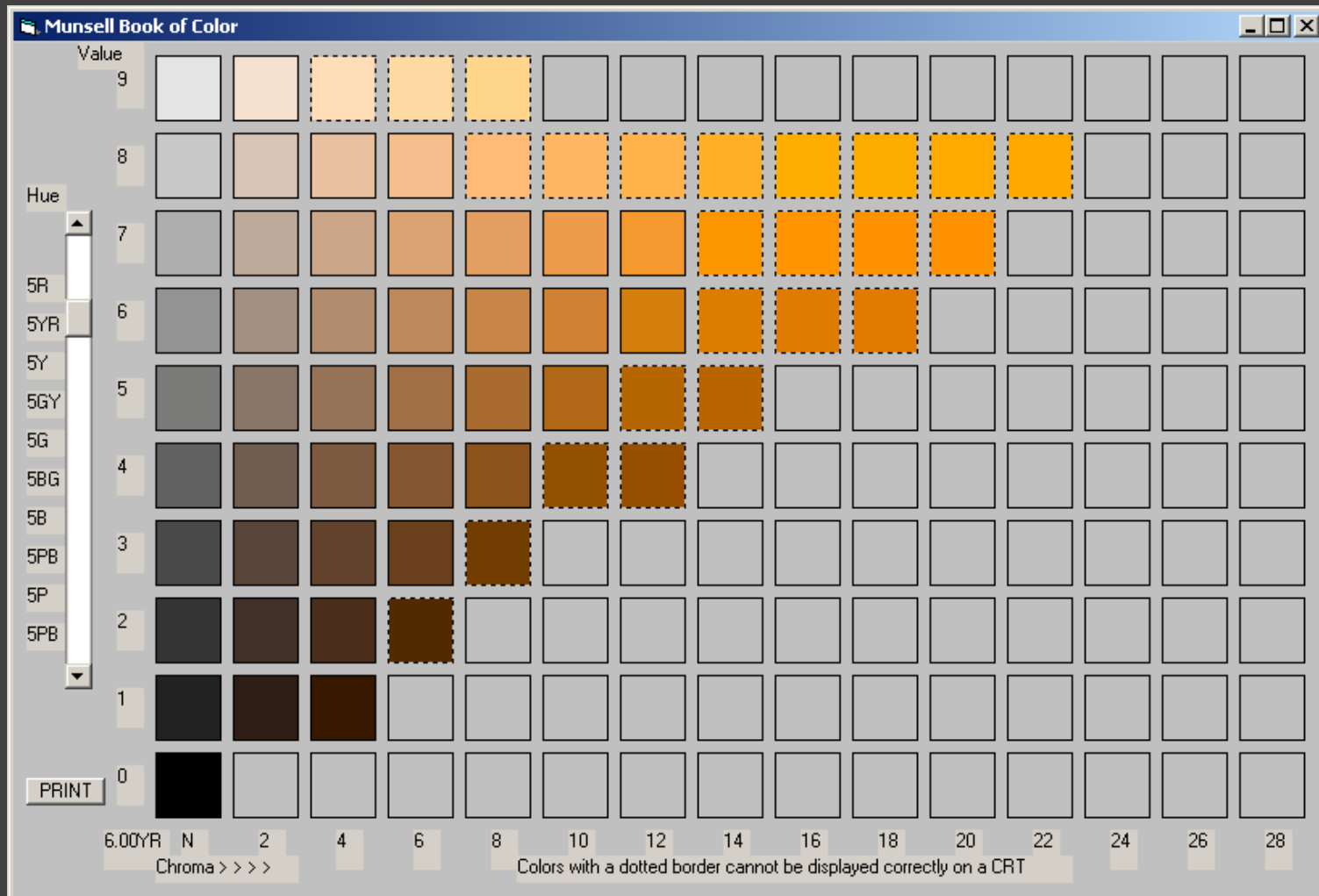
Hue, Value and Chroma



Hue, Value and Chroma

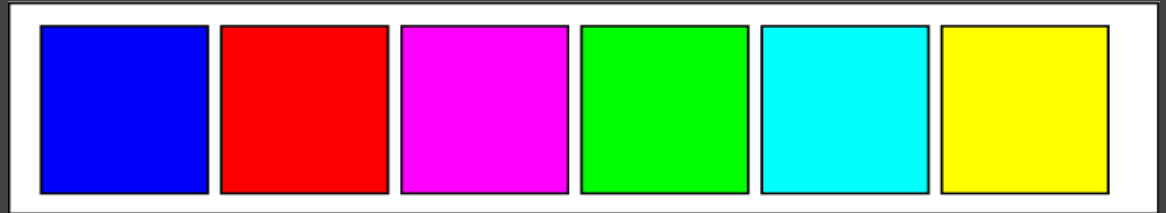


Munsell Color System



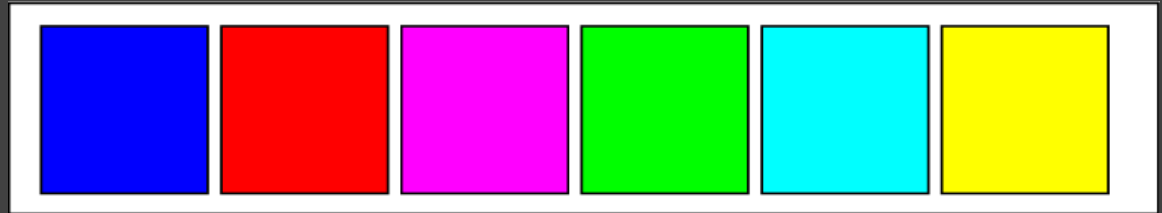
Perceptual Brightness

Color palette



Perceptual Brightness

Color palette

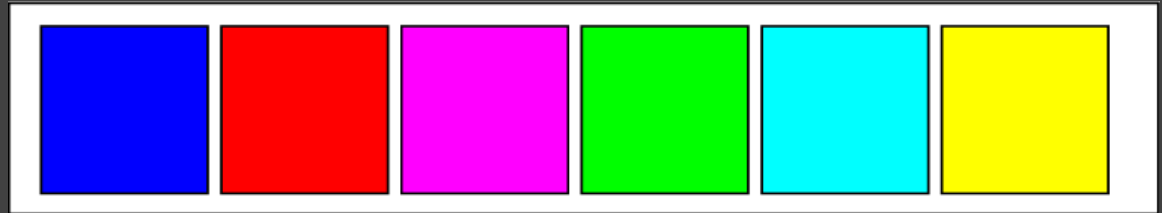


HSL Lightness
(*Photoshop*)



Perceptual Brightness

Color palette

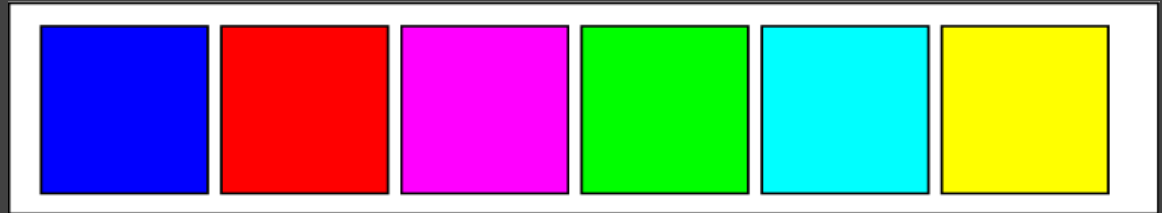


Luminance Y
(CIE XYZ)



Perceptual Brightness

Color palette

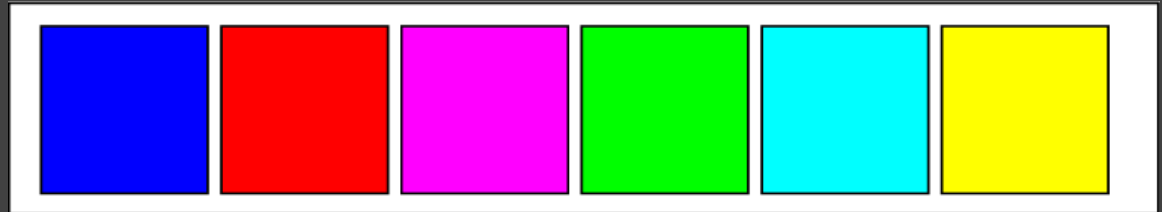


Munsell Value



Perceptual Brightness

Color palette

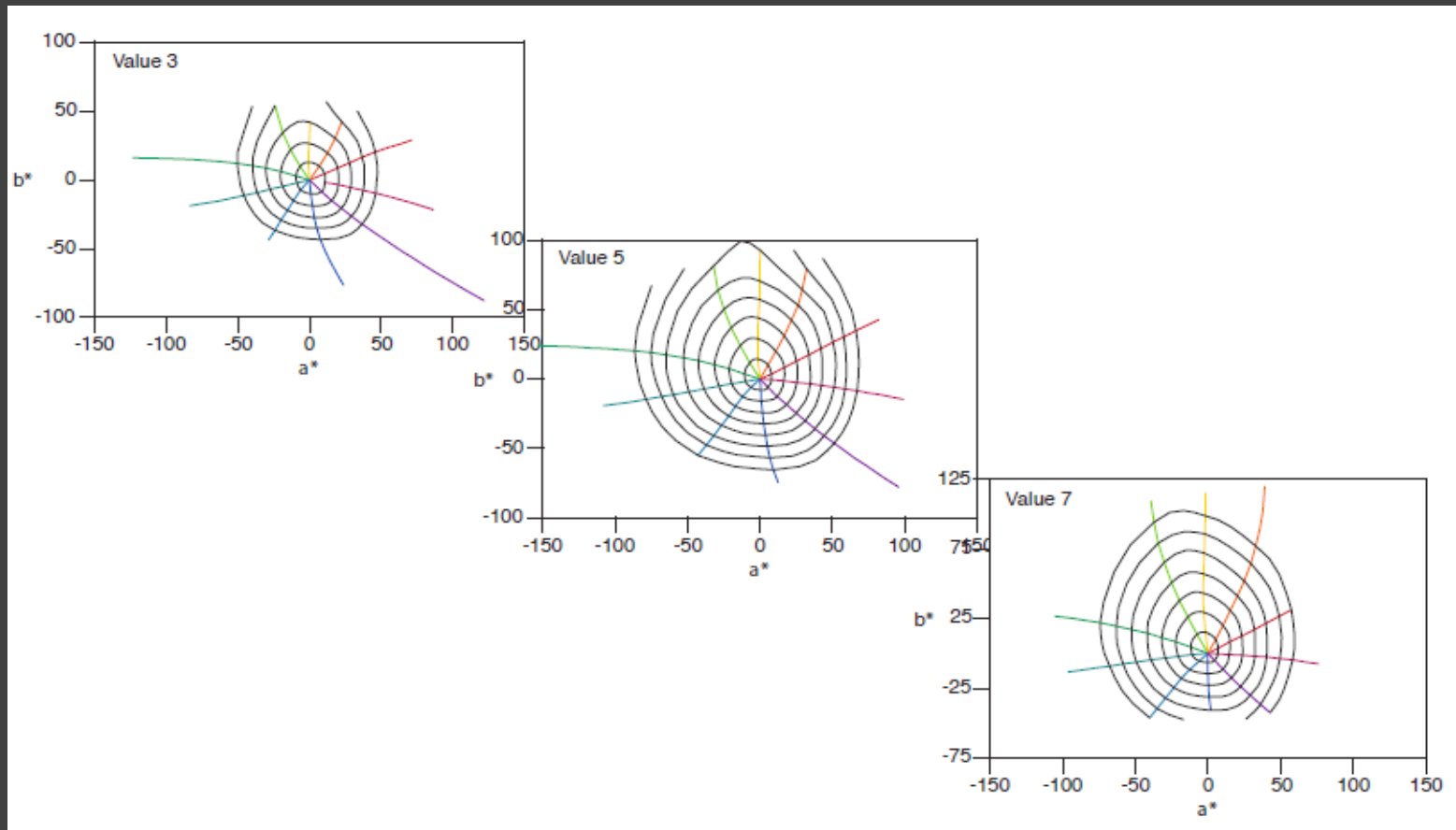


Munsell Value
L* (CIE LAB)



Perceptually-Uniform Color Space

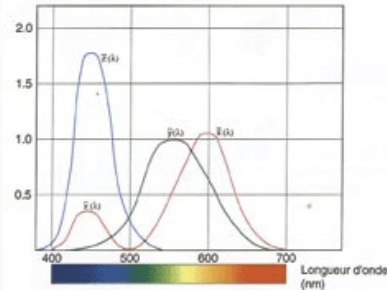
Munsell colors in CIE LAB coordinates



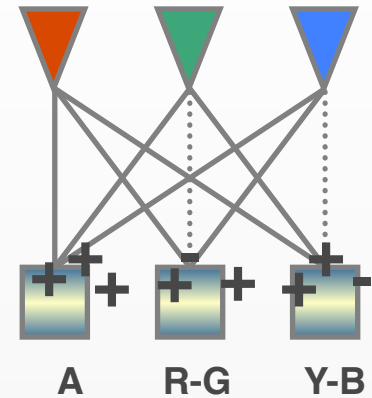
Perception of Color



Light



Cone Response



Opponent Signals

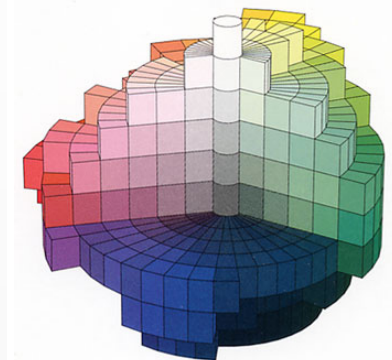
“Yellow”

Color Cognition



Mark D. Fairchild
COLOR APPEARANCE
MODELS

Color Appearance



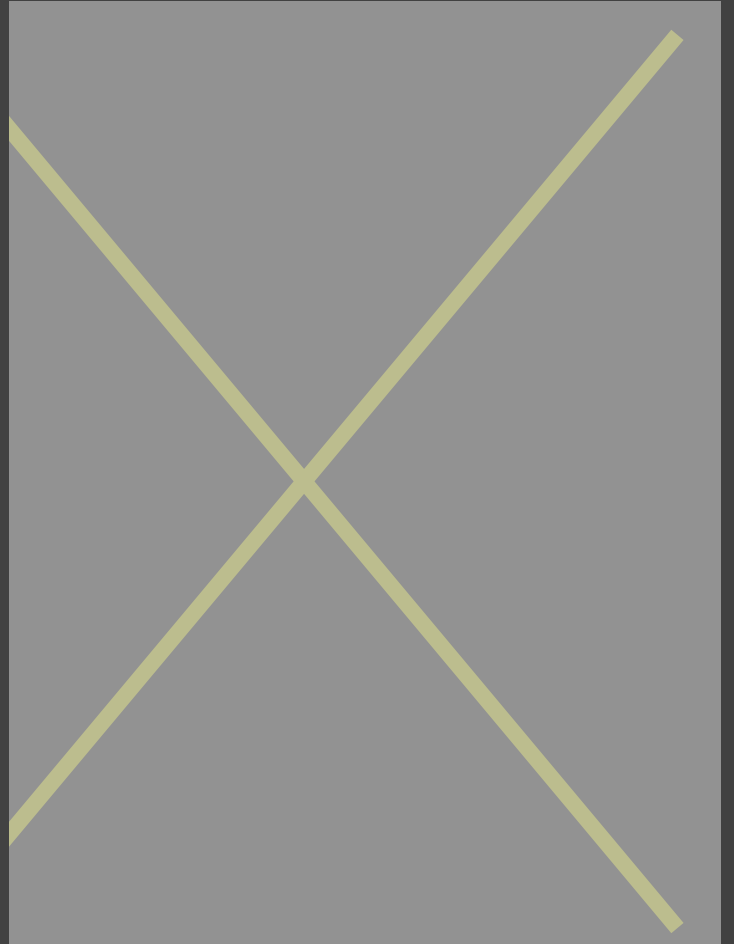
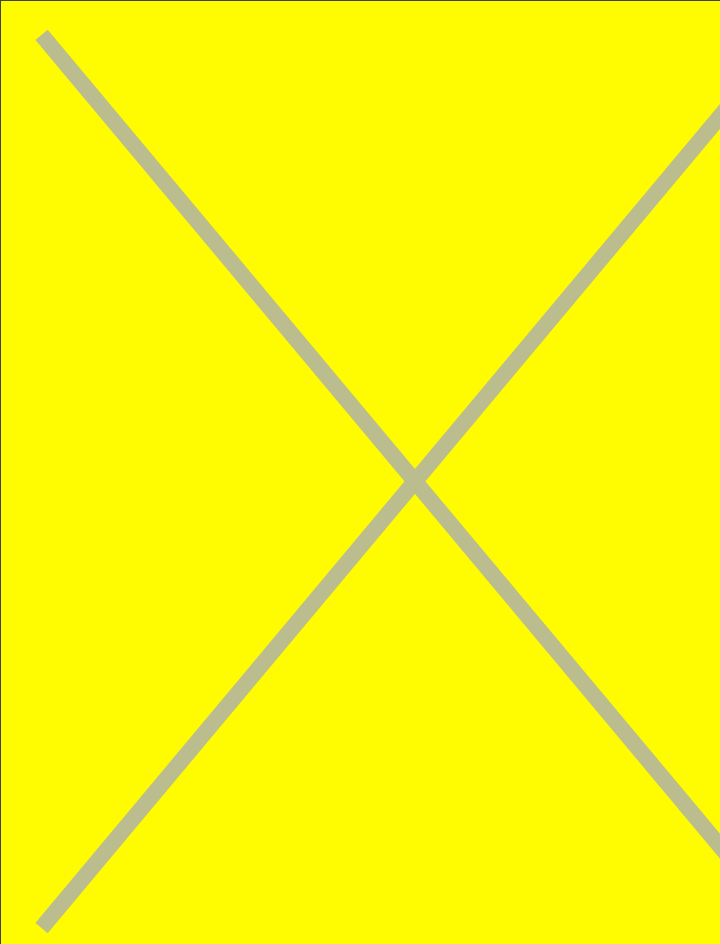
Color Perception

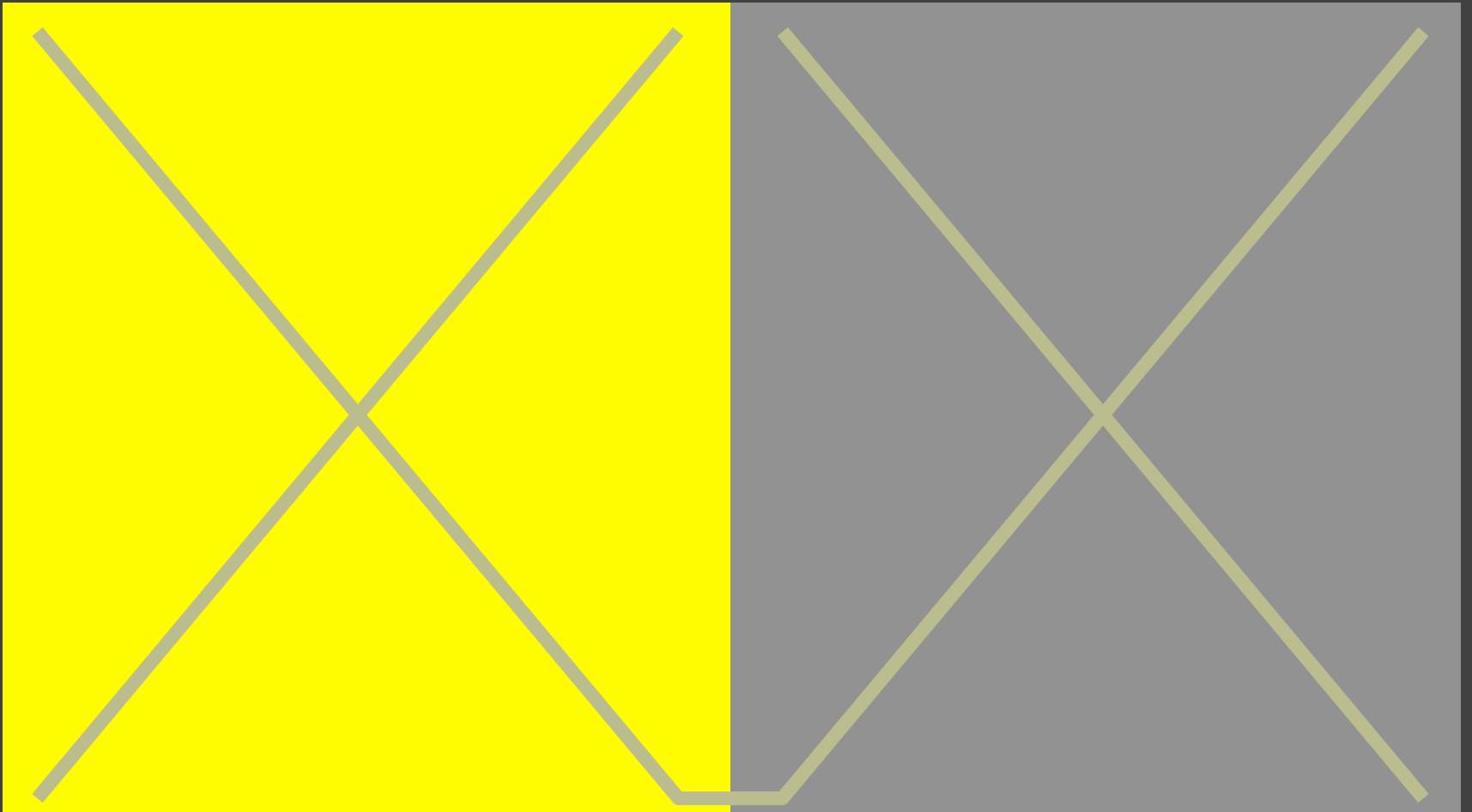
Color Appearance

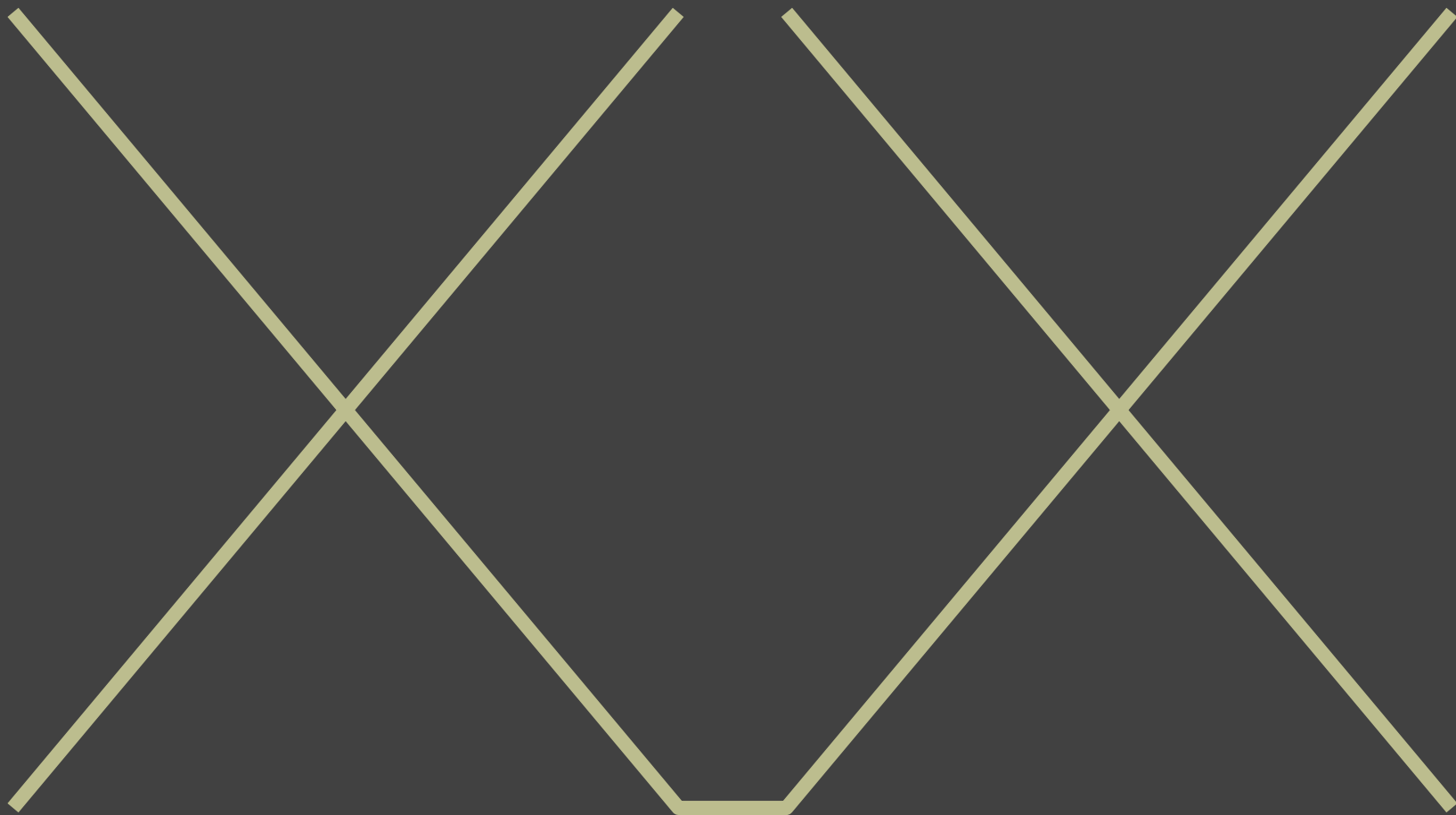
If we have a perceptually-uniform color space,
can we predict how we perceive colors?

“In order to use color effectively it is necessary to recognize that it deceives continually.”

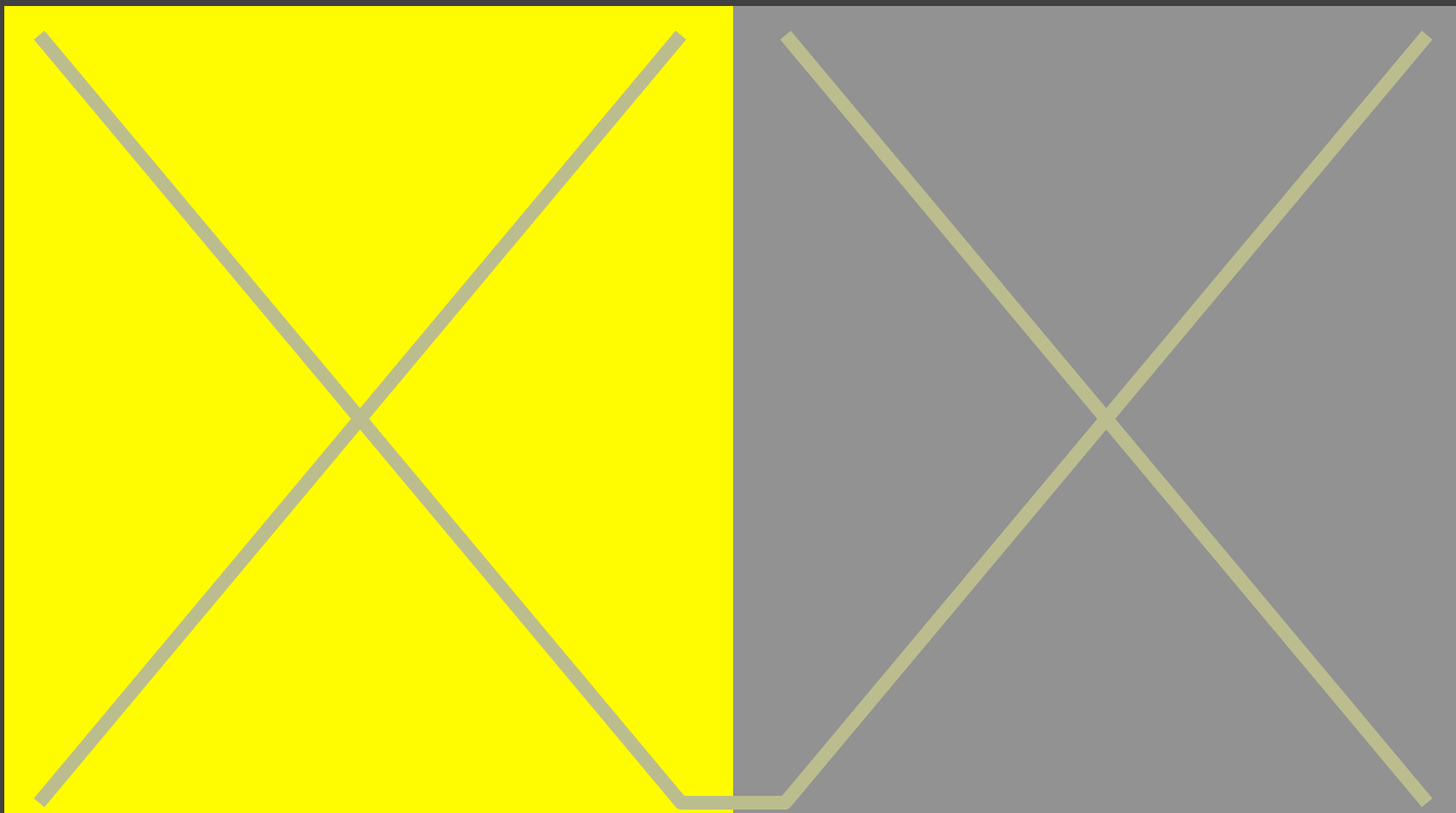
- Josef Albers, *Interaction of Color*







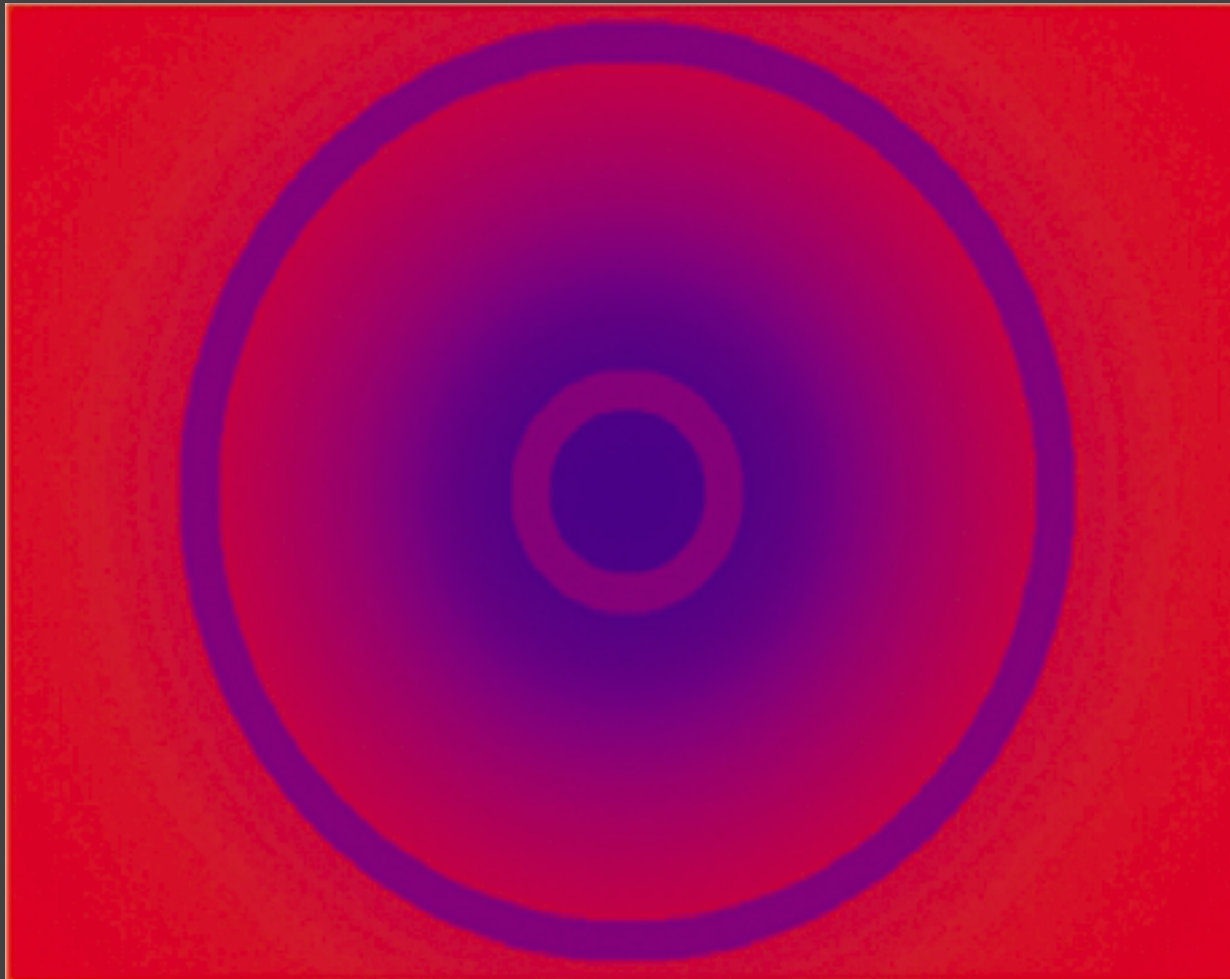
Simultaneous Contrast



Josef Albers

Simultaneous Contrast

Inner & outer rings are the same physical purple.



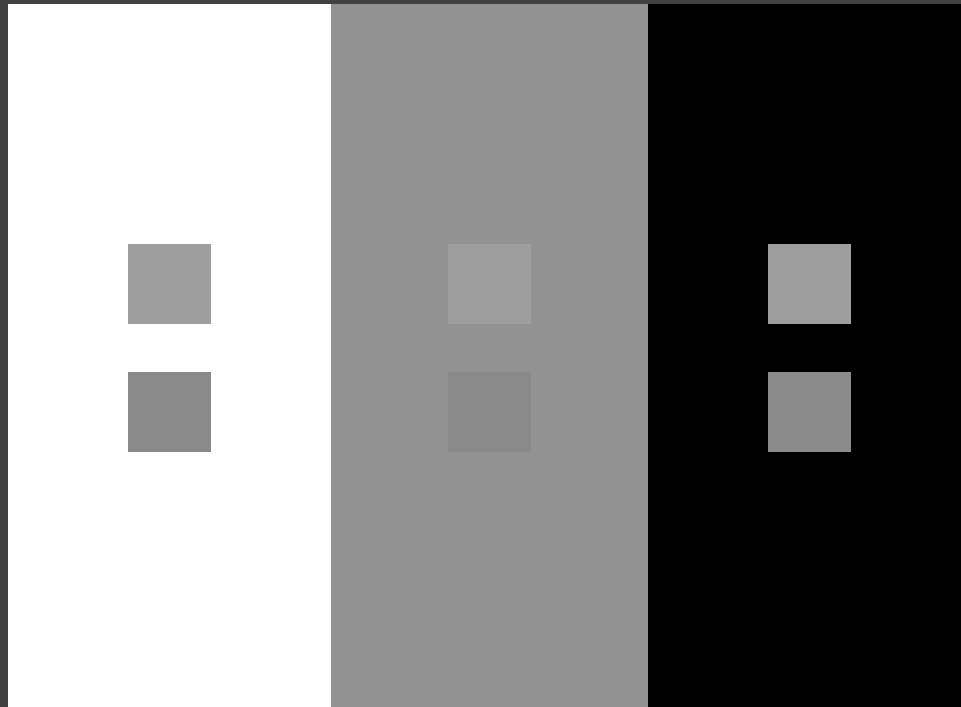
Bezold Effect

Color appearance depends on adjacent colors



Crispening

Perceived difference depends on background

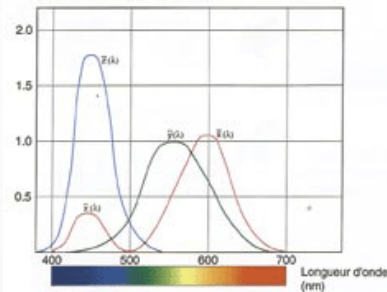


Color Appearance Models, Fairchild

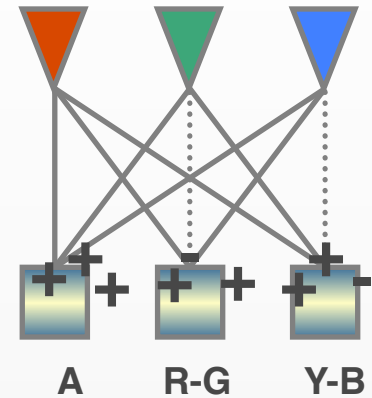
Perception of Color



Light



Cone Response



Opponent Signals

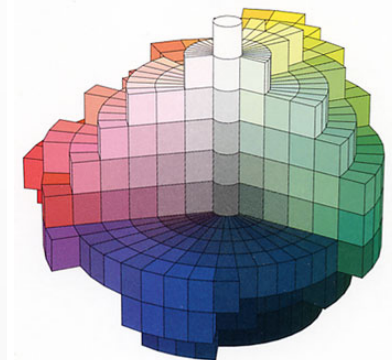
“Yellow”

Color Cognition



Mark D. Fairchild
**COLOR APPEARANCE
MODELS**

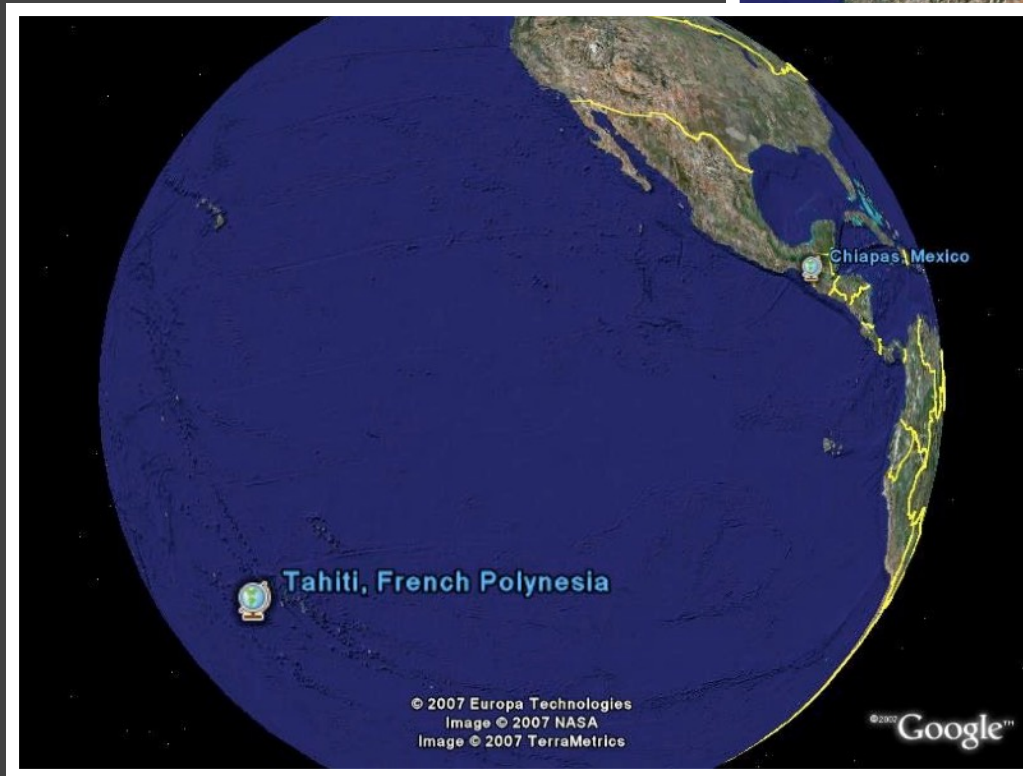
Color Appearance



Color Perception

Basic Color Terms

Chance discovery by Brent Berlin and Paul Kay.



Basic Color Terms

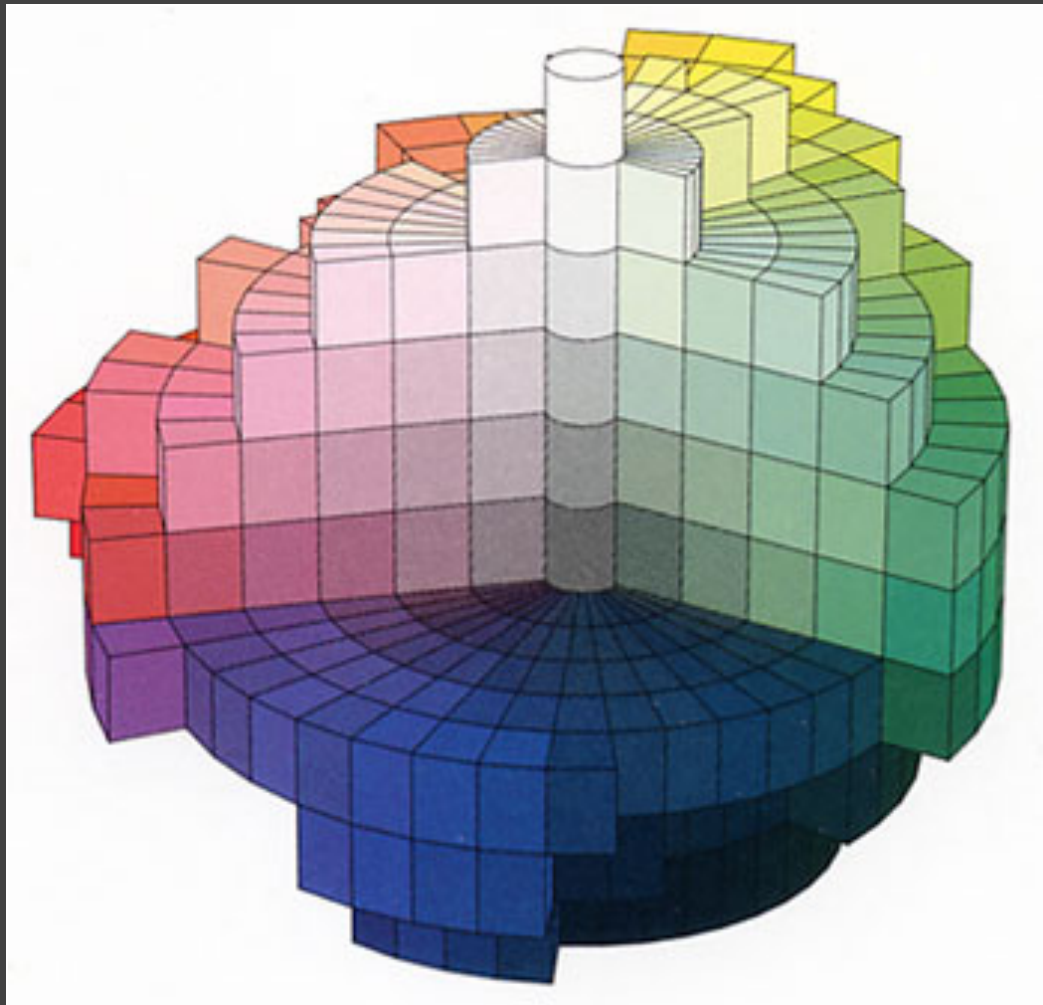
Chance discovery by Brent Berlin and Paul Kay.

Initial study in 1969

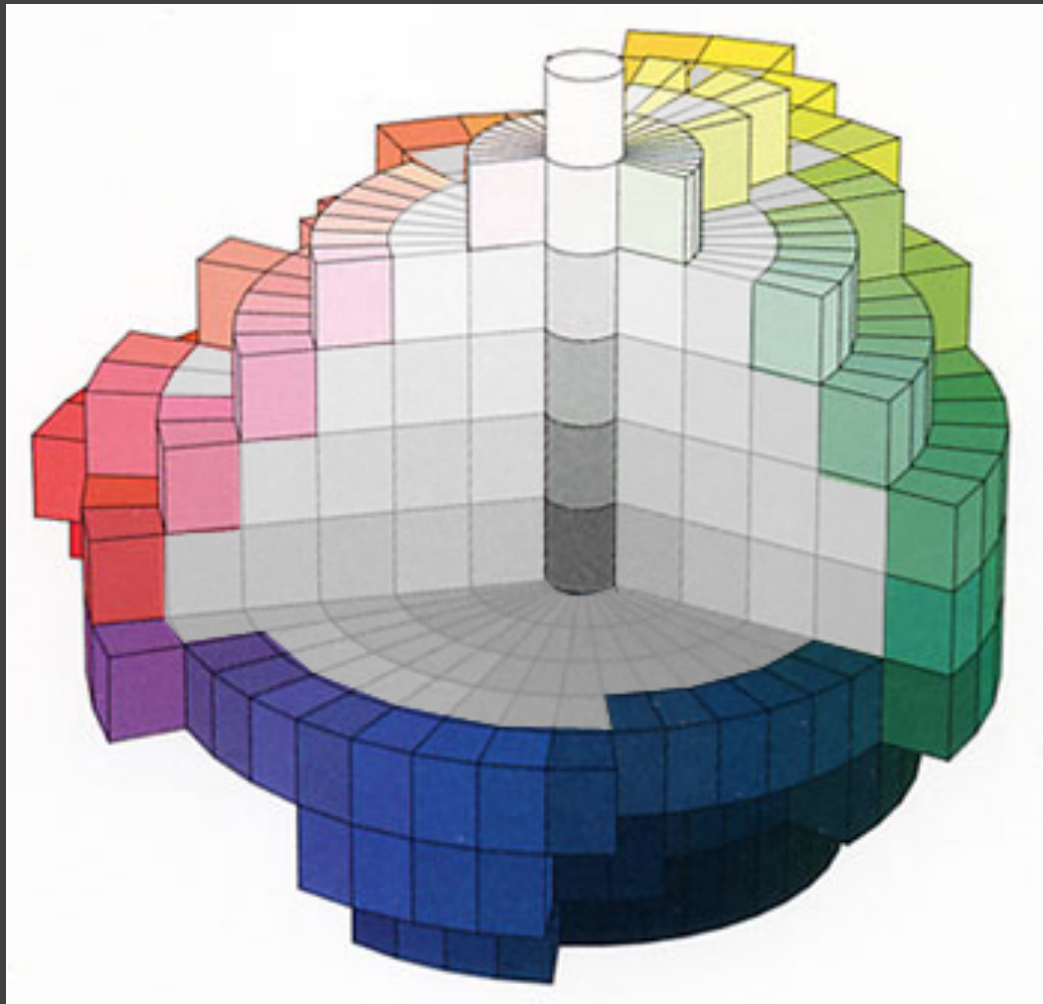
Surveyed speakers from 20 languages

Literature from 69 languages

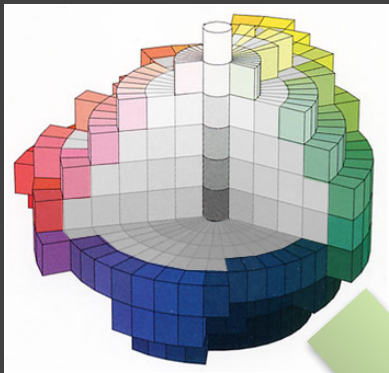
World Color Survey



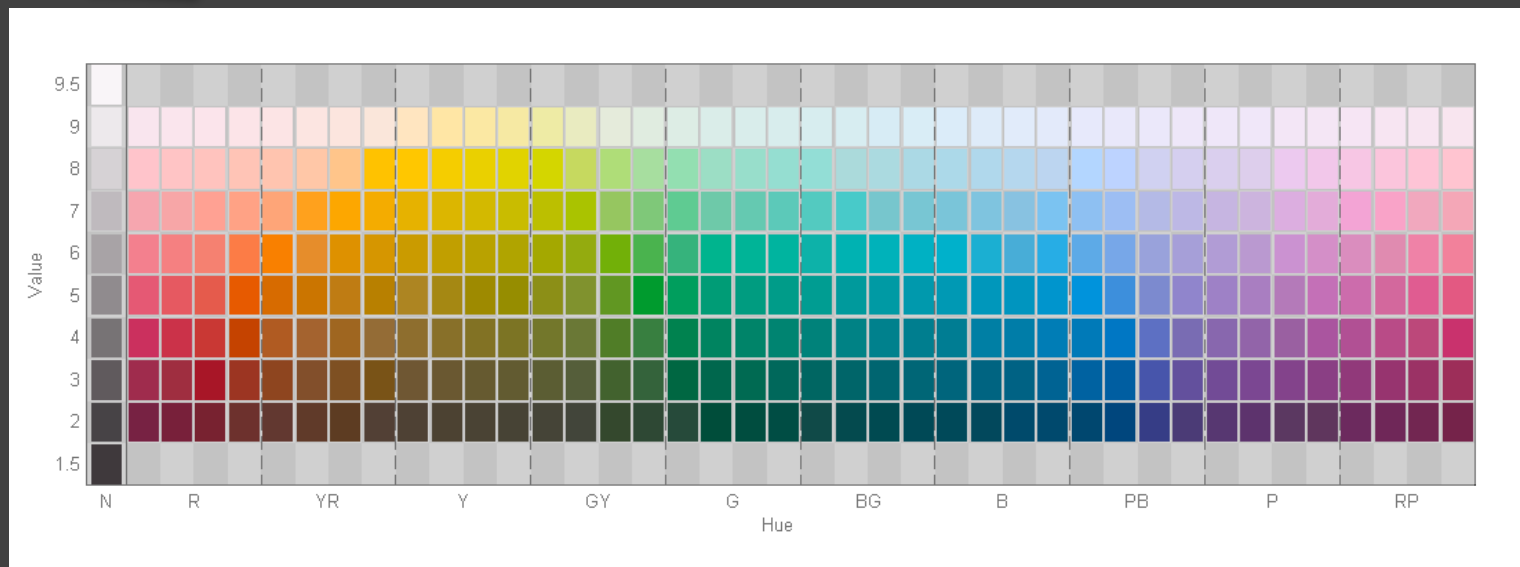
World Color Survey



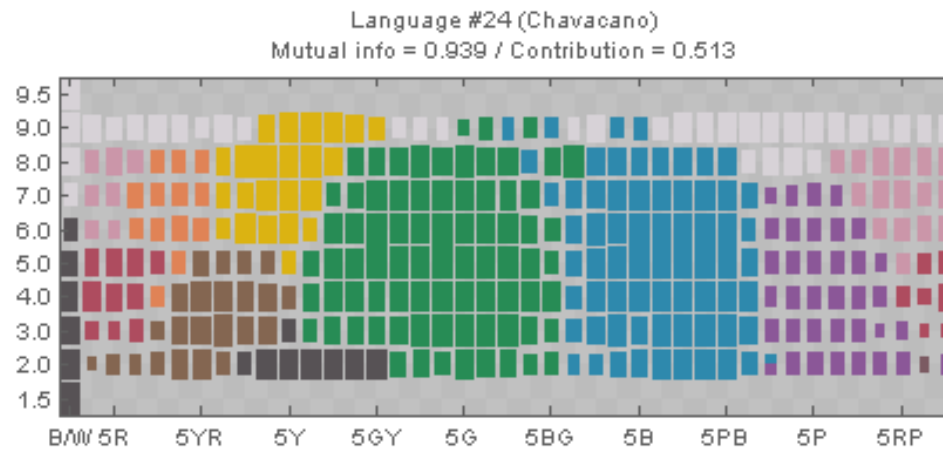
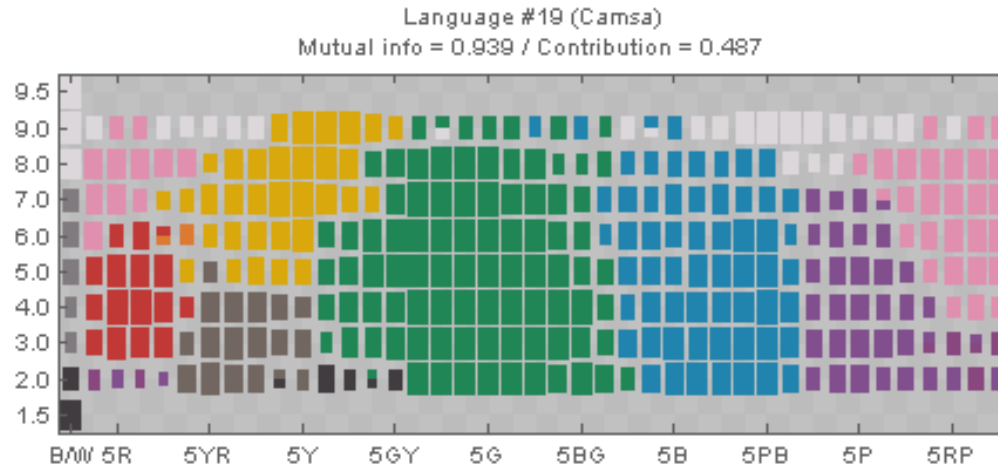
World Color Survey



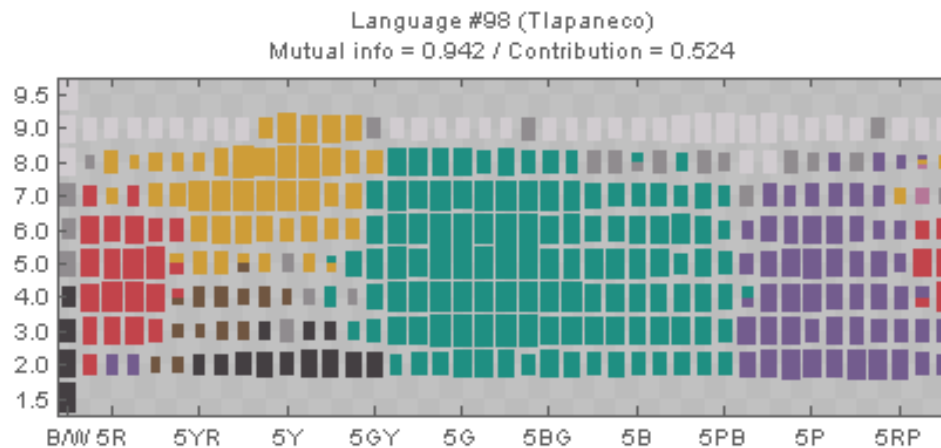
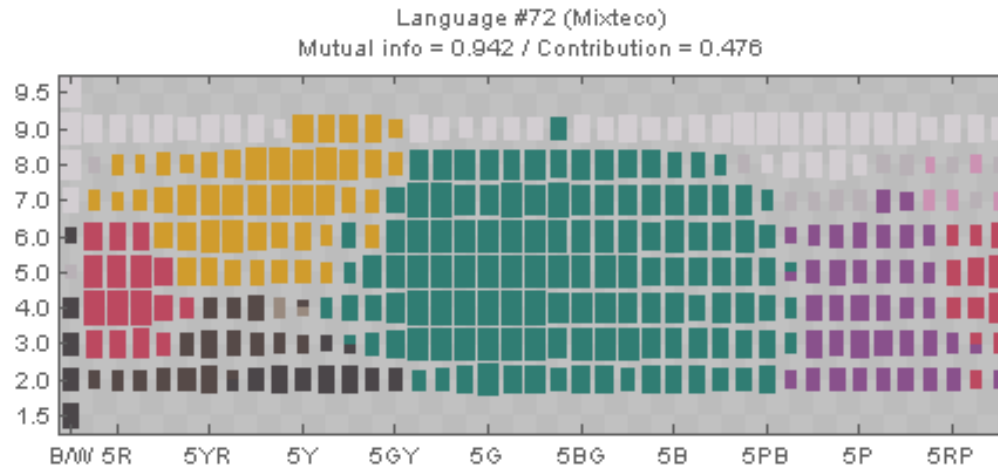
Naming information from 2,616 speakers from 110 languages on 330 Munsell color chips



Results from WCS



Results from WCS



Universal (?) Basic Color Terms

Basic color terms recur across languages.



White



Red



Pink



Grey



Yellow



Brown



Black



Green



Orange



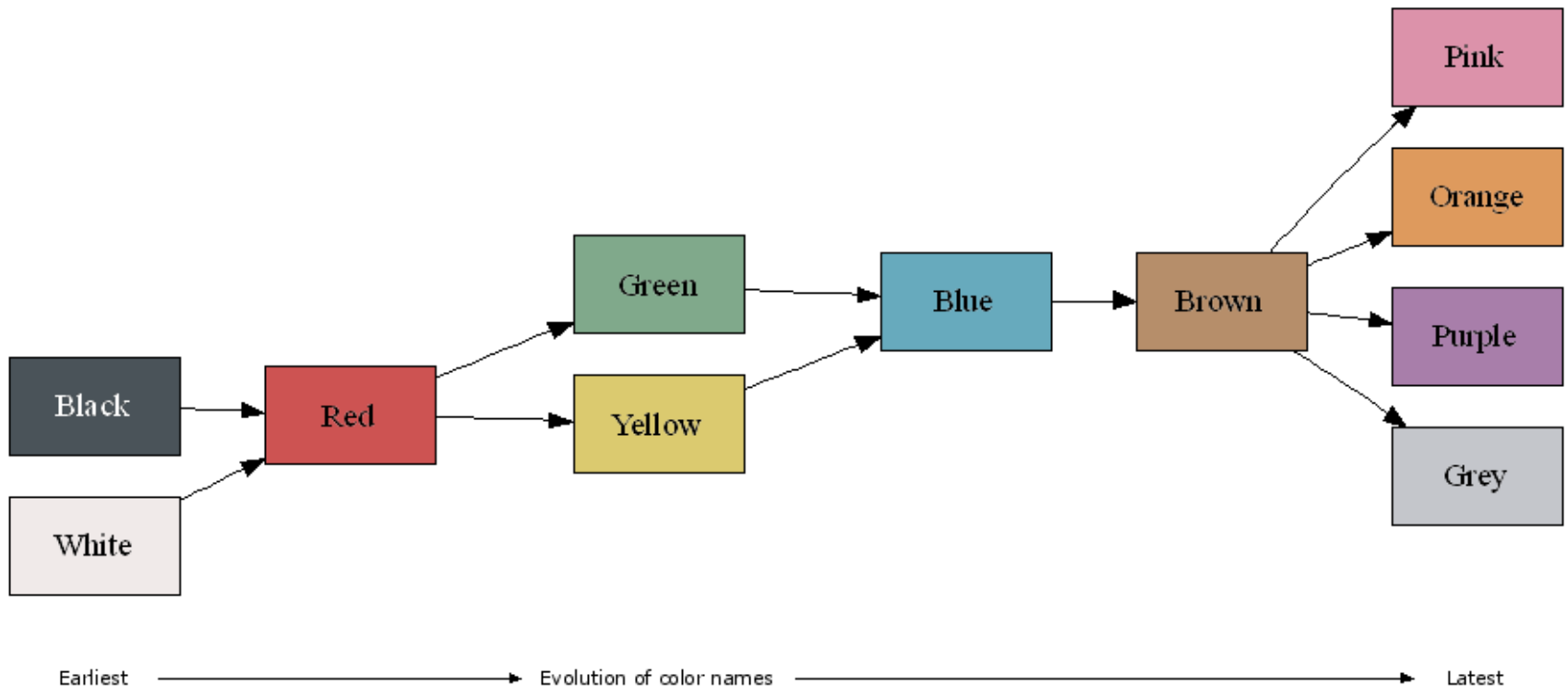
Blue



Purple

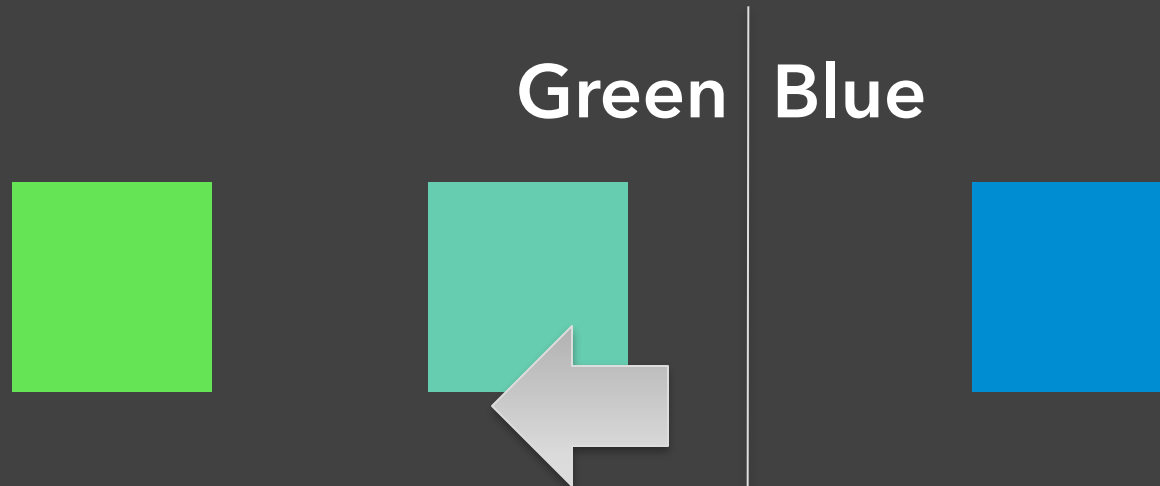
Evolution of Basic Color Terms

Proposed term evolution across languages.



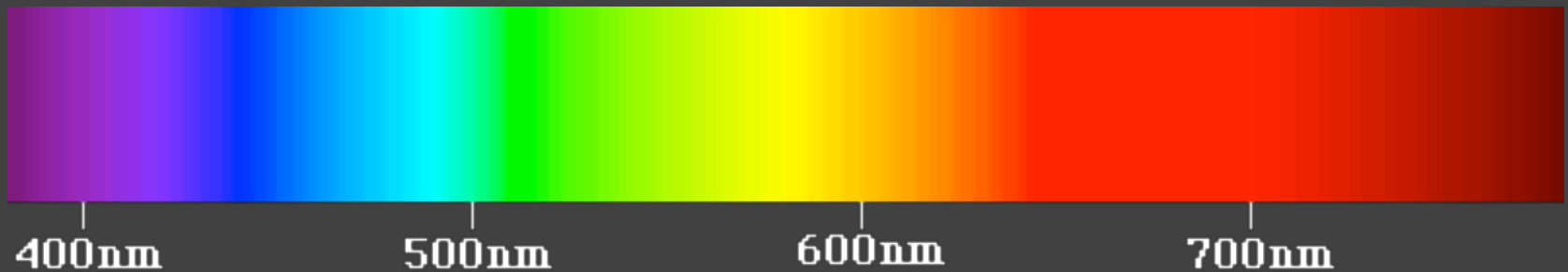
Naming Effects Color Perception

Color name boundaries



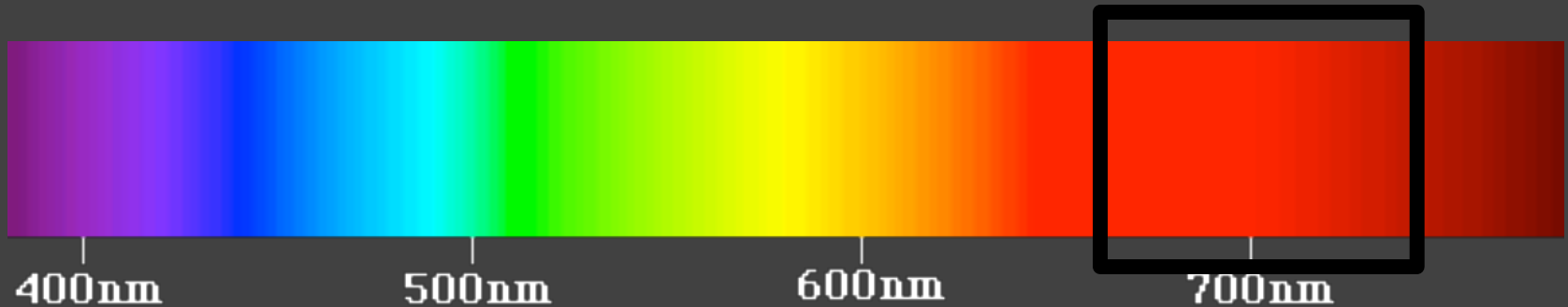
Rainbow Color Map

We associate and group colors together, often using the name we assign to the colors.



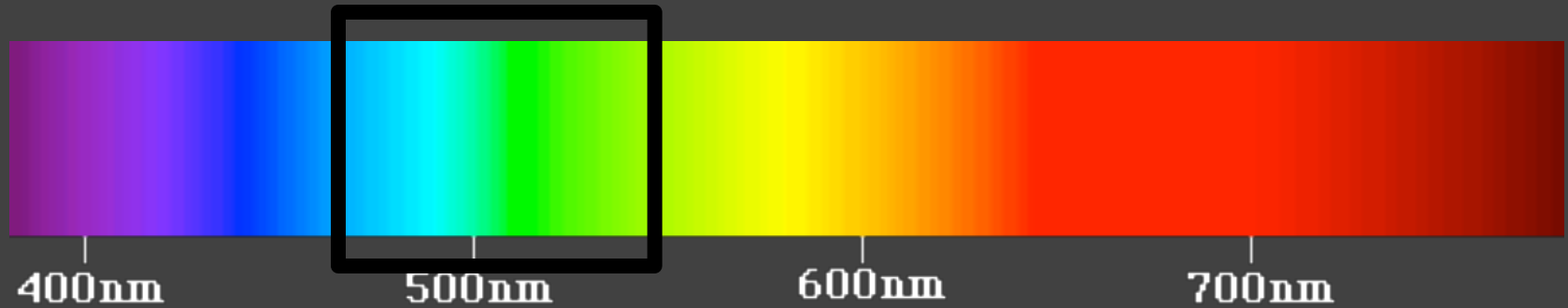
Rainbow Color Map

We associate and group colors together, often using the name we assign to the colors.



Rainbow Color Map

We associate and group colors together, often using the name we assign to the colors.



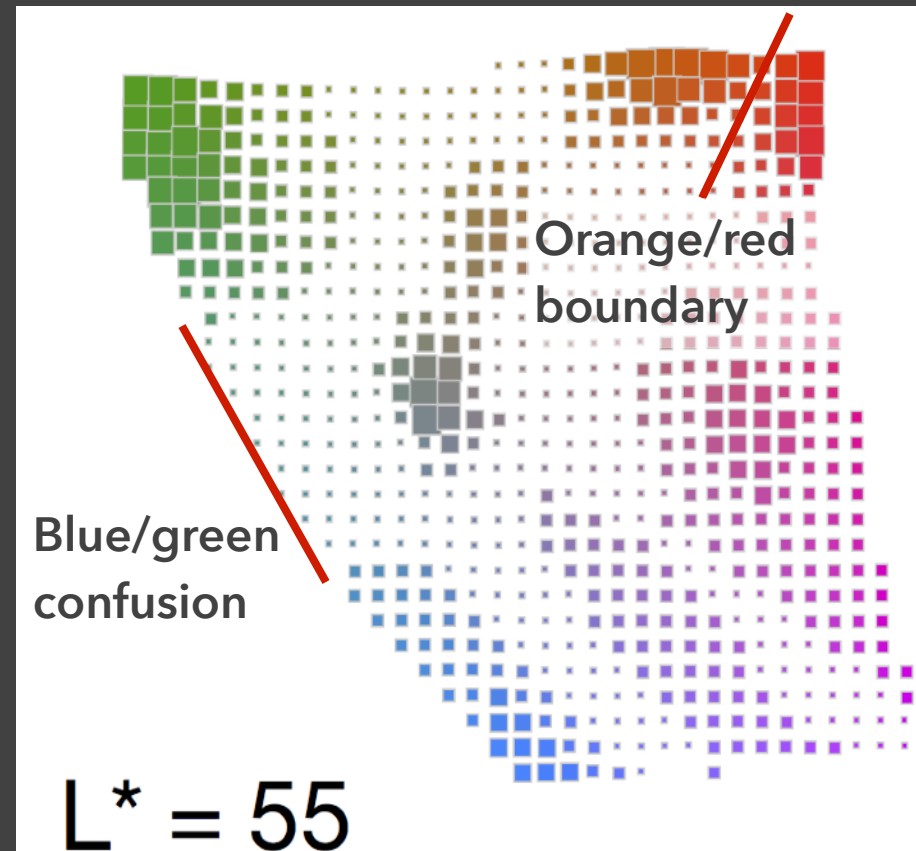
Color Naming Models [Heer & Stone '12]

Model 3 million responses from XKCD survey

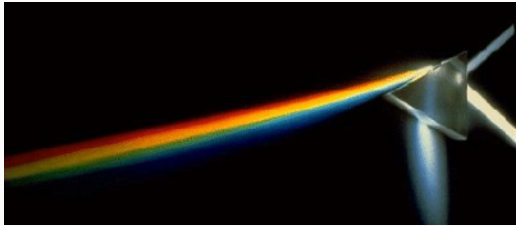
Bins in LAB space
sized by *saliency*:

How much do people
agree on color name?

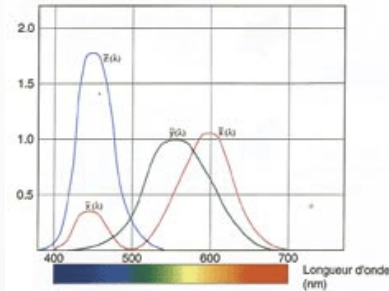
Modeled by entropy
of $p(\text{name} \mid \text{color})$



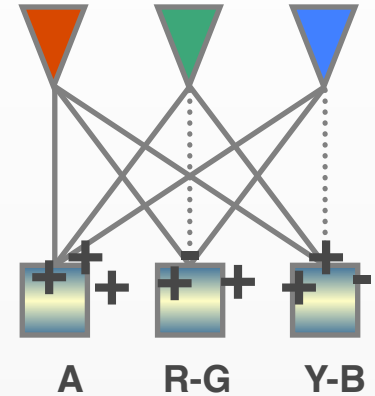
Perception of Color



Light



Cone Response



Opponent Signals

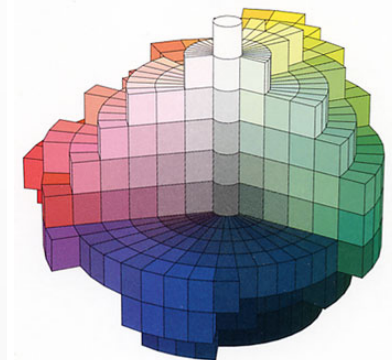
“Yellow”

Color Cognition



Mark D. Fairchild
COLOR APPEARANCE
MODELS

Color Appearance



Color Perception

Designing Colormaps

Colormap Design Considerations

Perceptually distinguishable colors

Value distance matches perceptual distance

Colors and concepts properly align

Aesthetically pleasing, intriguing

Respect color vision deficiencies

Should survive printing to black & white

Don't overwhelm people's capability!

Discrete (Binary, Categorical)

Symbol Legend



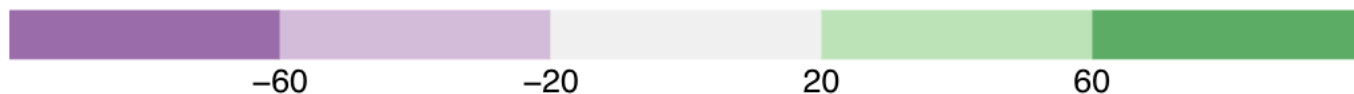
Continuous (Sequential, Diverging, Cyclic)

Gradient Legend



Discretized Continuous

Discrete Gradient



Categorical Color

Allocation of the Radio Spectrum

UNITED STATES FREQUENCY ALLOCATIONS THE RADIO SPECTRUM

RADIO SERVICES COLOR LEGEND

- | | | |
|-------------------------------|---------------------------|--|
| AERONAUTICAL MOBILE | HYPER-SATELLITE | RADIO ASTRONOMY |
| AERONAUTICAL MOBILE SATELLITE | LAND MOBILE | RADIO DETERMINATION SATELLITE |
| AERONAUTICAL RADIO NAVIGATION | LAND MOBILE SATELLITE | RADIO LOCATION |
| AMATEUR | MARITIME MOBILE | RADIO LOCATION SATELLITE |
| AMATEUR SATELLITE | MARITIME MOBILE SATELLITE | RADIO NAVIGATION |
| BROADCASTING | MARITIME RADIO NAVIGATION | RADIO NAVIGATION SATELLITE |
| BROADCASTING SATELLITE | METEOROLOGICAL AID | SPACE OPERATION |
| EARTH ORBITATION SATELLITE | METEOROLOGICAL SATELLITE | SPACE RESEARCH |
| FIXED | MOBILE | STANDARD FREQUENCY AND TIME SIGNAL |
| FIXED SATELLITE | MOBILE SATELLITE | STANDARD FREQUENCY AND TIME SIGNAL SATELLITE |

- ### ACTIVITY CODE
- | | |
|--------------------------|----------------------------------|
| GOVERNMENT EXCLUSIVE | GOVERNMENT/NON-GOVERNMENT SHARED |
| NON-GOVERNMENT EXCLUSIVE | |

ALLOCATION USE DESIGNATION


SERVICE	EXAMPLE	DESCRIPTION
Primary	F1E2	Capital Letters
Secondary	F1E2	Capital Letters



Alloc

UNITED STATES FREQUENCY ALLOCATION THE RADIO SPECTRUM

RADIO SERVICES COLOR LEGEND

 AERONAUTICAL MOBILE	 INTER-SATELLITE	 RADIO ASTRONOMY
 AERONAUTICAL MOBILE SATELLITE	 LAND MOBILE	 RADIODETERMINATION SATELLITE
 AERONAUTICAL RADIONAVIGATION	 LAND MOBILE SATELLITE	 RADIOLOCATION
 AMATEUR	 MARITIME MOBILE	 RADIOLOCATION SATELLITE
 AMATEUR SATELLITE	 MARITIME MOBILE SATELLITE	 RADIONAVIGATION
 BROADCASTING	 MARITIME RADIONAVIGATION	 RADIONAVIGATION SATELLITE
 BROADCASTING SATELLITE	 METEOROLOGICAL AIDS	 SPACE OPERATION
 EARTH EXPLORATION SATELLITE	 METEOROLOGICAL SATELLITE	 SPACE RESEARCH
 FIXED	 MOBILE	 STANDARD FREQUENCY AND TIME SIGNAL
 FIXED SATELLITE	 MOBILE SATELLITE	 STANDARD FREQUENCY AND TIME SIGNAL SATELLITE

ACTIVITY CODE

RADIO SERVICES COLOR LEGEND

<input type="checkbox"/> AERONAUTICAL MOBILE	<input type="checkbox"/> INTER-SATELLITE	<input type="checkbox"/> RADIO ASTRONOMY
<input type="checkbox"/> AERONAUTICAL MOBILE SATELLITE	<input type="checkbox"/> LAND MOBILE	<input type="checkbox"/> RADIODETERMINATION SATELLITE
<input type="checkbox"/> AERONAUTICAL RADIONAVIGATION	<input type="checkbox"/> LAND MOBILE SATELLITE	<input type="checkbox"/> RADIOLOCATION
<input type="checkbox"/> AMATEUR	<input type="checkbox"/> MARITIME MOBILE	<input type="checkbox"/> RADIOLOCATION SATELLITE
<input type="checkbox"/> AMATEUR SATELLITE	<input type="checkbox"/> MARITIME MOBILE SATELLITE	<input type="checkbox"/> RADIONAVIGATION
<input type="checkbox"/> BROADCASTING	<input type="checkbox"/> MARITIME RADIONAVIGATION	<input type="checkbox"/> RADIONAVIGATION SATELLITE
<input type="checkbox"/> BROADCASTING SATELLITE	<input type="checkbox"/> METEOROLOGICAL AIDS	<input type="checkbox"/> SPACE OPERATION
<input type="checkbox"/> EARTH EXPLORATION SATELLITE	<input type="checkbox"/> METEOROLOGICAL SATELLITE	<input type="checkbox"/> SPACE RESEARCH
<input type="checkbox"/> FIXED	<input type="checkbox"/> MOBILE	<input type="checkbox"/> STANDARD FREQUENCY AND TIME SIGNAL
<input type="checkbox"/> FIXED SATELLITE	<input type="checkbox"/> MOBILE SATELLITE	<input type="checkbox"/> STANDARD FREQUENCY AND TIME SIGNAL SATELLITE

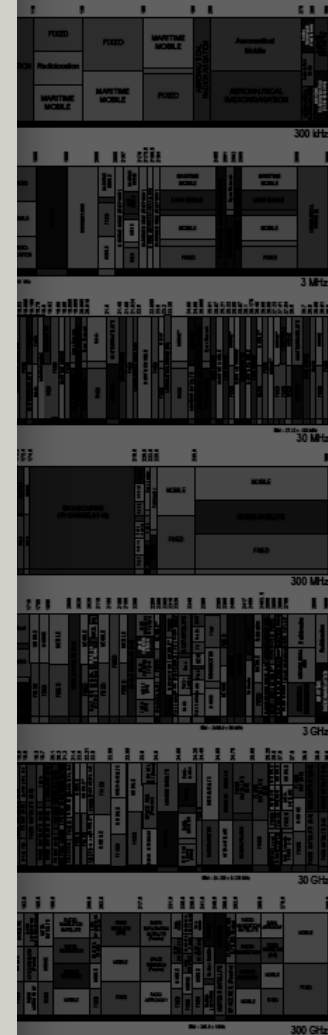
ACTIVITY CODE

<input type="checkbox"/> GOVERNMENT EXCLUSIVE	<input type="checkbox"/> GOVERNMENT-GOVERNMENT SHARED
<input type="checkbox"/> NON-GOVERNMENT EXCLUSIVE	

ALLOCATION USAGE DESIGNATION

SERVICE	EXAMPLE	DESCRIPTION
Primary	F1E2D	Coastal Station
Secondary	F1E2D	Coastal Station

rum



Allocation of the Radio Spectrum

UNITED STATES FREQUENCY ALLOCATIONS THE RADIO SPECTRUM

RADIO SERVICES COLOR LEGEND

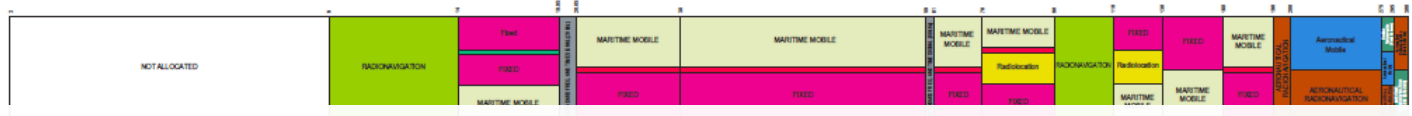
AERONAUTICAL MOBILE	INTERSATELLITE	RADIO ASTRONOMY
AERONAUTICAL MOBILE SATELLITE	LAND MOBILE	RADIO DETERMINATION SATELLITE
AERONAUTICAL RADIOLOCATION	LAND MOBILE SATELLITE	RADIO LOCATION
AMATEUR	MARITIME MOBILE	RADIO LOCATION SATELLITE
AMATEUR SATELLITE	MARITIME MOBILE SATELLITE	RADIO NAVIGATION
BROADCASTING	MARITIME RADIOLOCATION	RADIO NAVIGATION SATELLITE
BROADCASTING SATELLITE	METEOROLOGICAL AIDS	SPACE OPERATION
EARTH EXPLORATION SATELLITE	METEOROLOGICAL SATELLITE	SPACE RESEARCH
FIXED	MOBILE	STANDARD FREQUENCY AND TIME SIGNAL
FIXED SATELLITE	MOBILE SATELLITE	STANDARD FREQUENCY AND TIME SIGNAL SATELLITE

ACTIVITY CODE

GOVERNMENT EXCLUSIVE	GOVERNMENT/NON-GOVERNMENT SHARED
NON-GOVERNMENT EXCLUSIVE	

ALLOCATION USAGE DESIGNATION

SERVICE	EXAMPLE	DESCRIPTION
Primary	FIXED	Capitol Building
Co-primary	Mobile	Cellular



Issues:

Too many colors

Hard to remember mapping

Colors not distinctive, some are very similar

Poor grouping: similar colors, different values

Labels cause clutter

Color surround effects

Colors interactions may not look good together




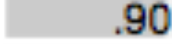
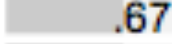





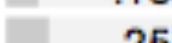

Palette Design & Color Names

Minimize overlap and ambiguity of colors.

Color Name Distance

0.00	1.00	1.00	1.00	0.98	1.00	1.00	1.00	1.00	1.00	0.20
1.00	0.00	1.00	0.97	1.00	1.00	1.00	1.00	0.96	1.00	1.00
1.00	1.00	0.00	1.00	1.00	1.00	1.00	1.00	0.90	0.99	1.00
1.00	0.97	1.00	0.00	1.00	0.95	0.99	1.00	1.00	1.00	1.00
0.98	1.00	1.00	1.00	0.00	0.96	0.91	0.97	1.00	0.99	1.00
1.00	1.00	1.00	0.95	0.96	0.00	0.97	0.93	0.98	1.00	1.00
1.00	1.00	1.00	0.99	0.91	0.97	0.00	1.00	1.00	1.00	1.00
1.00	1.00	1.00	1.00	0.97	0.93	1.00	0.00	1.00	1.00	1.00
1.00	0.96	0.90	1.00	1.00	0.98	1.00	1.00	0.00	1.00	1.00
0.20	1.00	0.99	1.00	0.99	1.00	1.00	1.00	1.00	1.00	0.00

Saliency

 .47
 .90
 .67
 .66
 .47
 .37
 .58
 .67
 .18
 .25

Name

blue 62.9%
orange 93.9%
green 79.8%
red 80.4%
purple 51.4%
brown 54.0%
pink 71.7%
grey 79.4%
yellow 31.2%
blue 25.4%

Tableau-10











Average 0.97

.52

Palette Design & Color Names

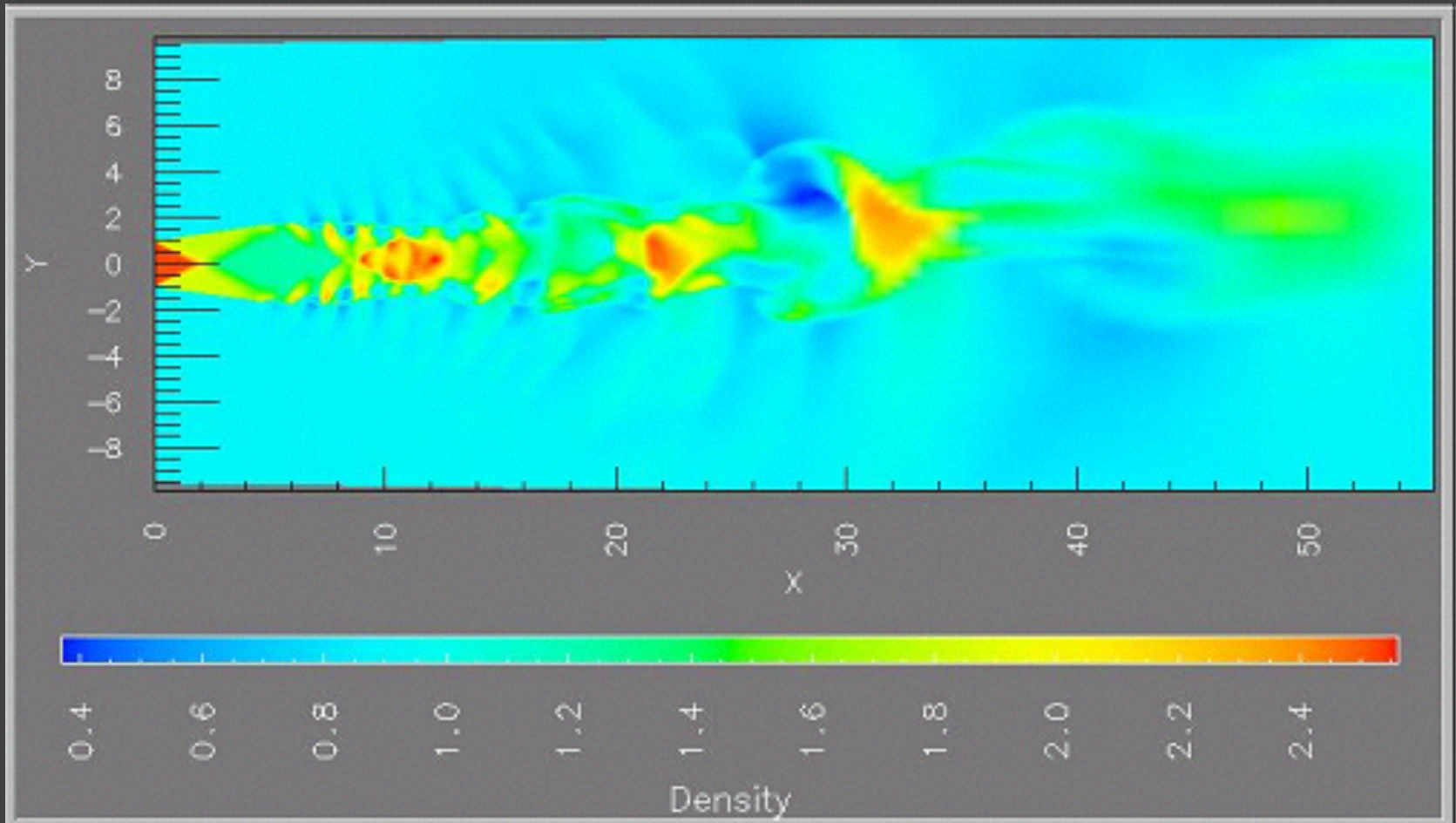
Minimize overlap and ambiguity of colors.

Color Name Distance

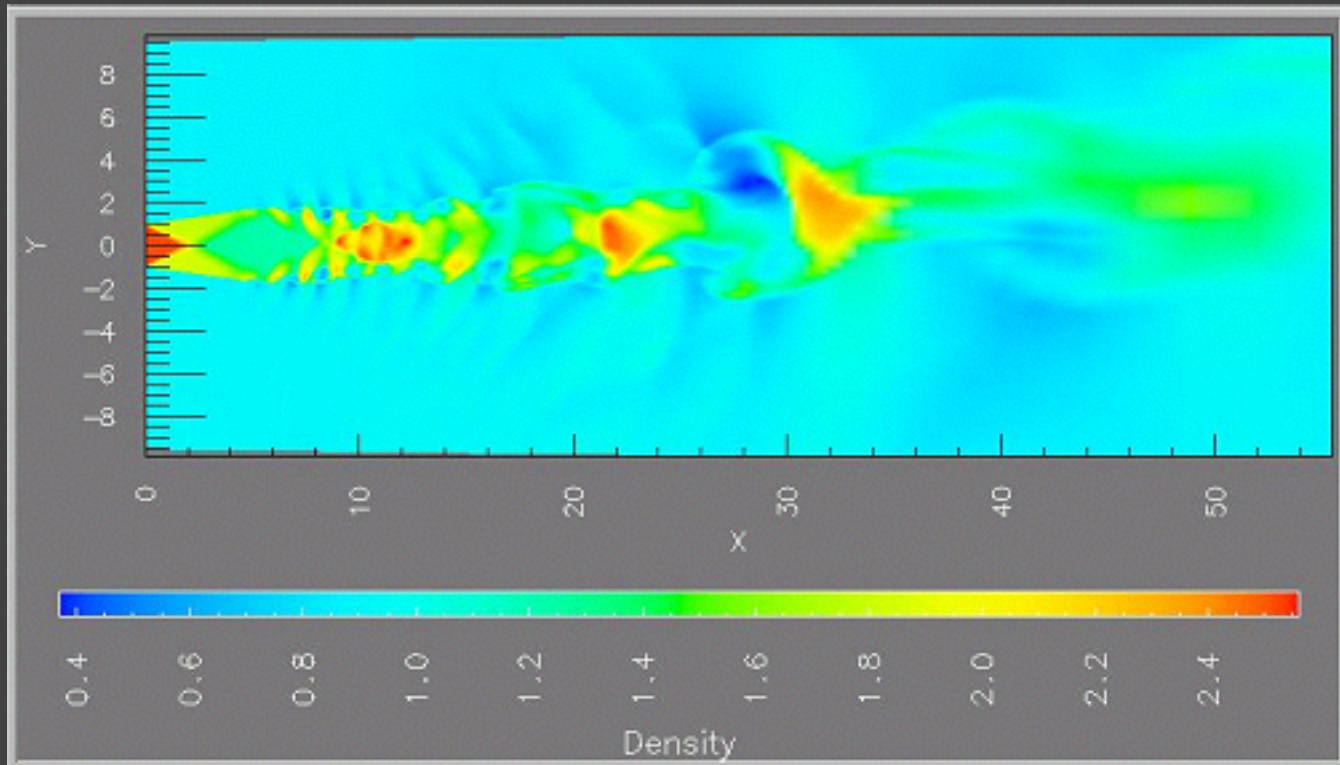
	1	2	3	4	5	6	7	8	9	10	Saliency	Name
0.00	1.00	1.00	0.89	0.07	1.00	0.35	0.99	1.00	0.89	 .30	blue 50.5%	
1.00	0.00	0.99	1.00	1.00	0.92	1.00	0.84	0.98	0.99	 .21	red 27.8%	
1.00	0.99	0.00	1.00	0.98	1.00	1.00	1.00	0.17	1.00	 .34	green 36.8%	
0.89	1.00	1.00	0.00	0.98	1.00	0.71	0.93	1.00	0.32	 .55	purple 67.3%	
0.07	1.00	0.98	0.98	0.00	1.00	0.36	1.00	0.97	0.95	 .20	blue 36.6%	
1.00	0.92	1.00	1.00	1.00	0.00	1.00	0.97	0.99	1.00	 .39	orange 51.9%	
0.35	1.00	1.00	0.71	0.36	1.00	0.00	0.95	0.92	0.42	 .13	blue 15.7%	
0.99	0.84	1.00	0.93	1.00	0.97	0.95	0.00	0.98	0.85	 .16	pink 29.4%	
1.00	0.98	0.17	1.00	0.97	0.99	0.92	0.98	0.00	0.97	 .12	green 21.7%	
0.89	0.99	1.00	0.32	0.95	1.00	0.42	0.85	0.97	0.00	 .30	purple 23.9%	
Excel-10	<i>Average</i> 0.87									.27		

Quantitative Color

Rainbow Color Maps

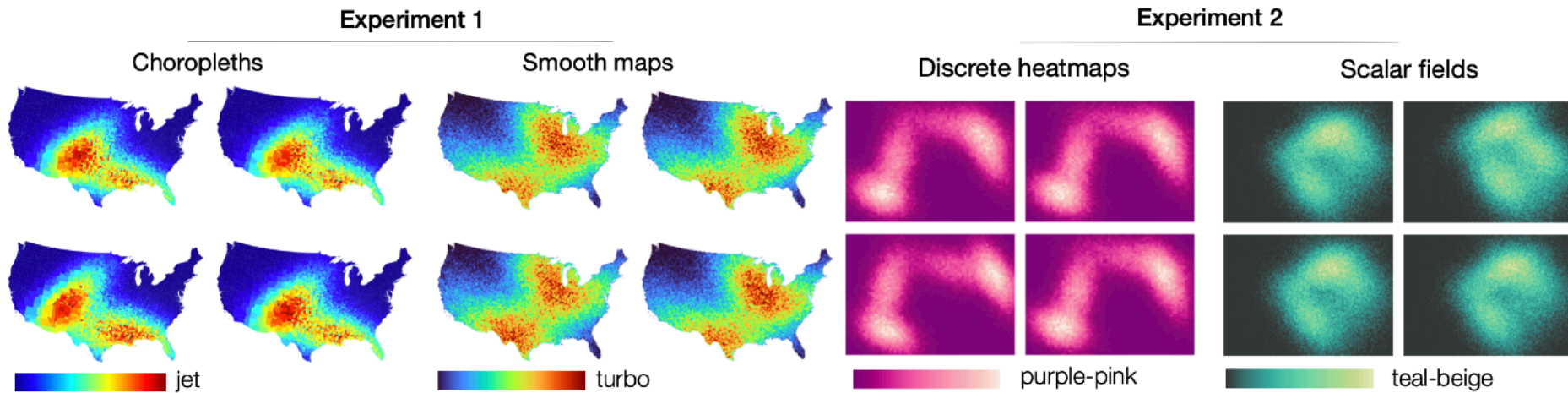


Be wary of naïve rainbows?



1. Naive rainbows are unfriendly to color blind viewers
2. Hues are not naturally ordered
3. Some colors are less effective at high spatial frequencies
4. People segment colors into classes -> perceptual banding

But rainbow helpful for inference?



Reda et al. '21: Color Nameability Predicts Inference Accuracy in Spatial Visualizations

Rainbow found ineffective for *value comparison* [Liu '18]...

...but color name salience found to improve performance on *inference task* of distinguishing distributions [Reda '21]

Task matters!

Steps, rather than Gradients?

number of data classes on your map
3 [learn more >](#)

the nature of your data
sequential [learn more >](#)

pick a color scheme: BuGn

multihue single hue

(optional) only show schemes that are:
 colorblind safe print friendly
 photocopy-able [learn more >](#)

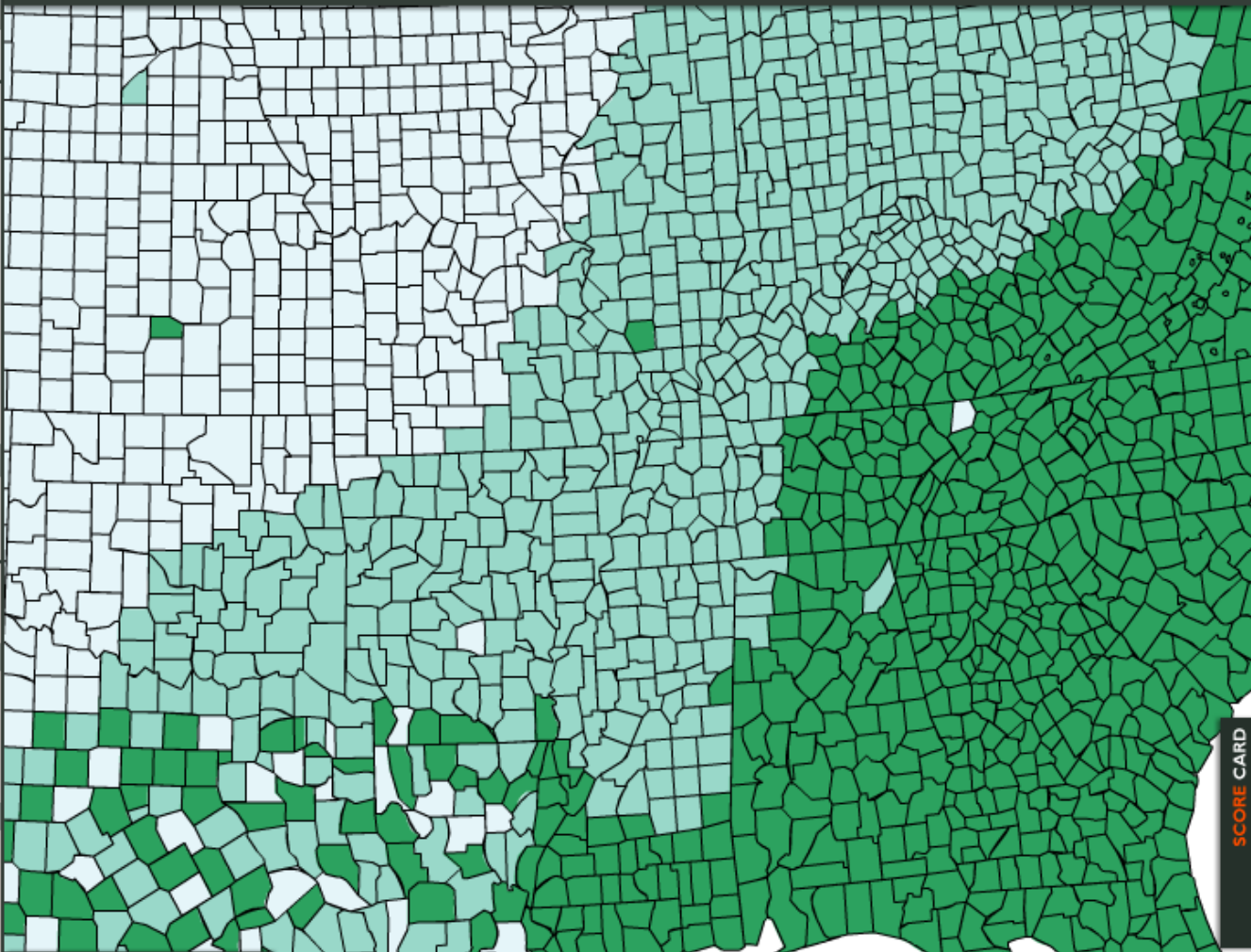
pick a color system
229, 245, 249
153, 216, 201
44, 162, 95

adjust map context
 roads cities borders

select a background
 solid color terrain

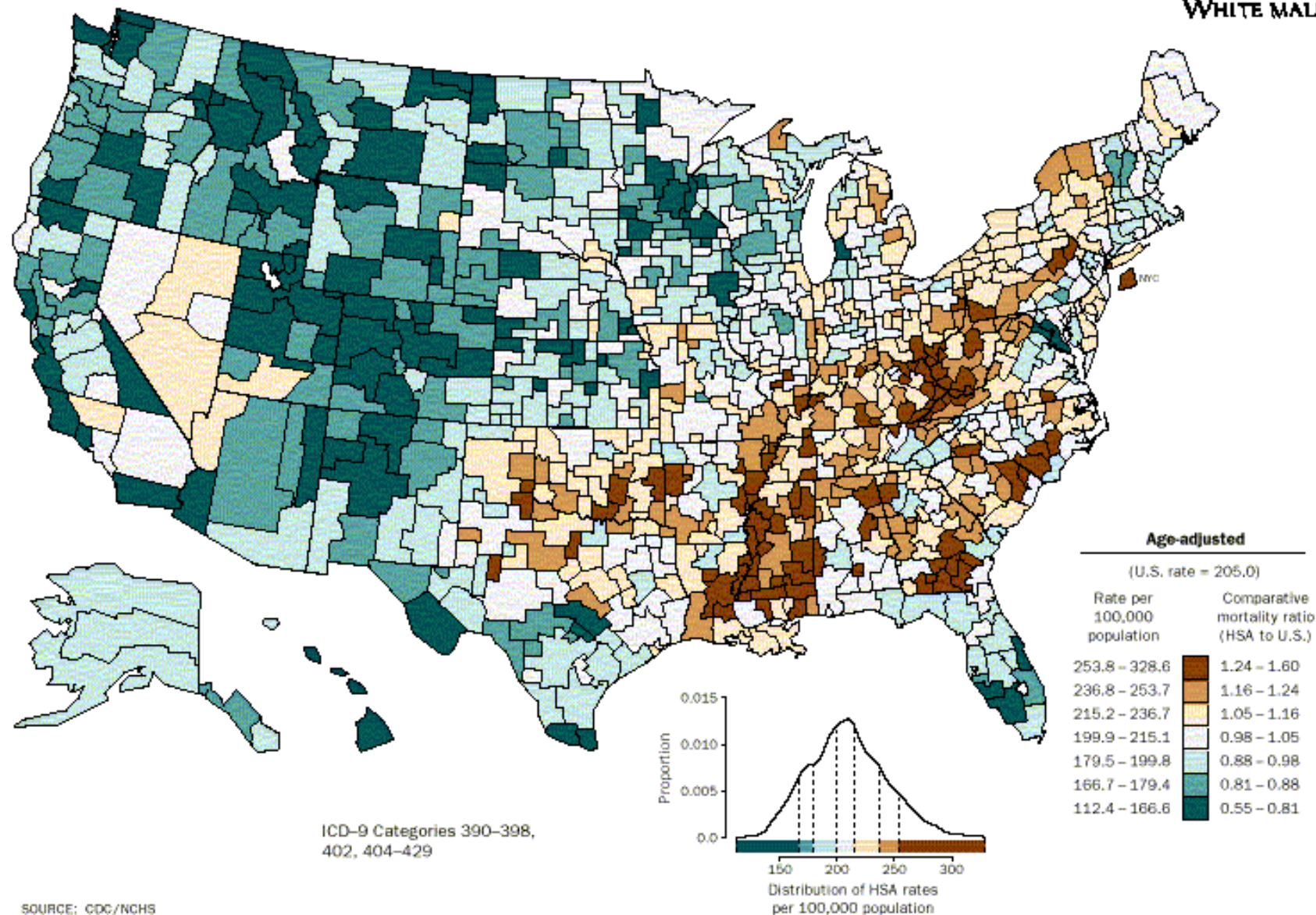
how to use | updates | credits

COLORBREWER 2.0
color advice for cartography



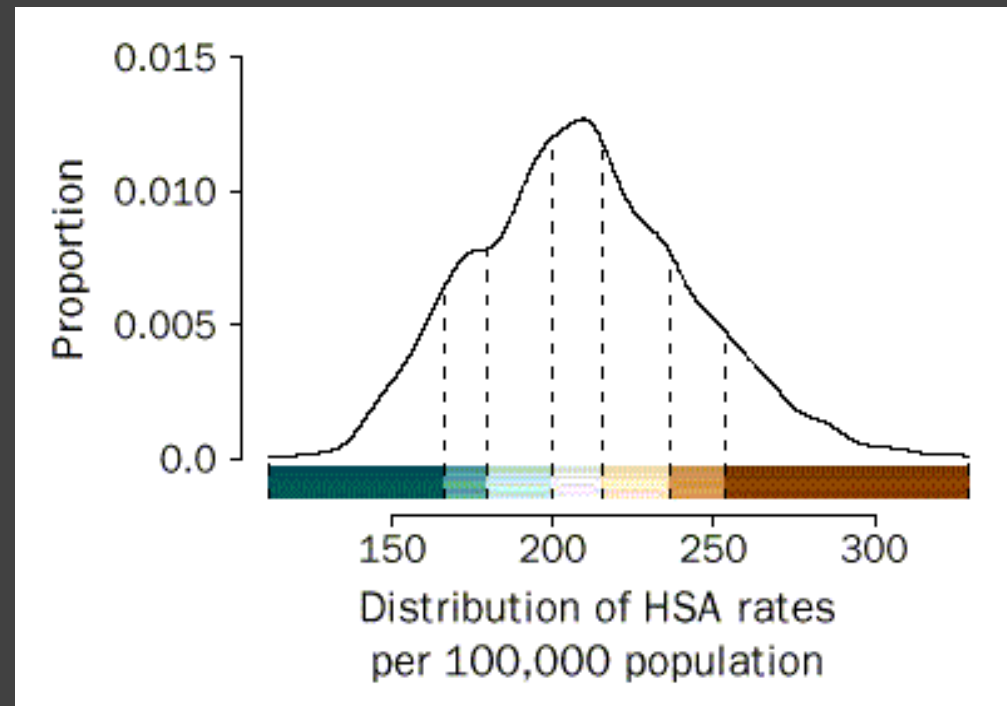
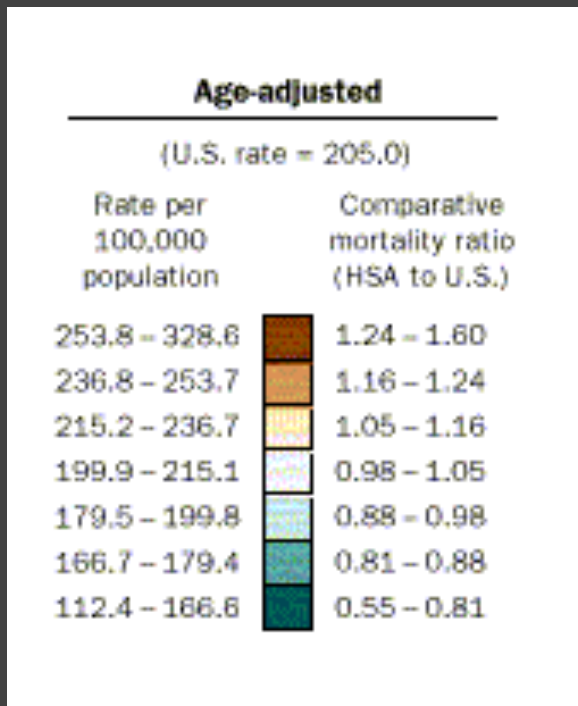
SCORE CARD

AGE-ADJUSTED DEATH RATES BY HSA, 1988-92

HEART DISEASE
WHITE MALE

SOURCE: CDC/NCHS

Classing Quantitative Data



Age-adjusted mortality rates for the United States.
Common option: break into 5 or 7 quantiles.

Classing Quantitative Data

1. Equal interval (arithmetic progression)
2. Quantiles (***recommended***)
3. Standard deviations
4. Clustering (Jenks' natural breaks / 1D K-Means)
 - Minimize within group variance
 - Maximize between group variance

Quantitative Color Encoding

Sequential color scale

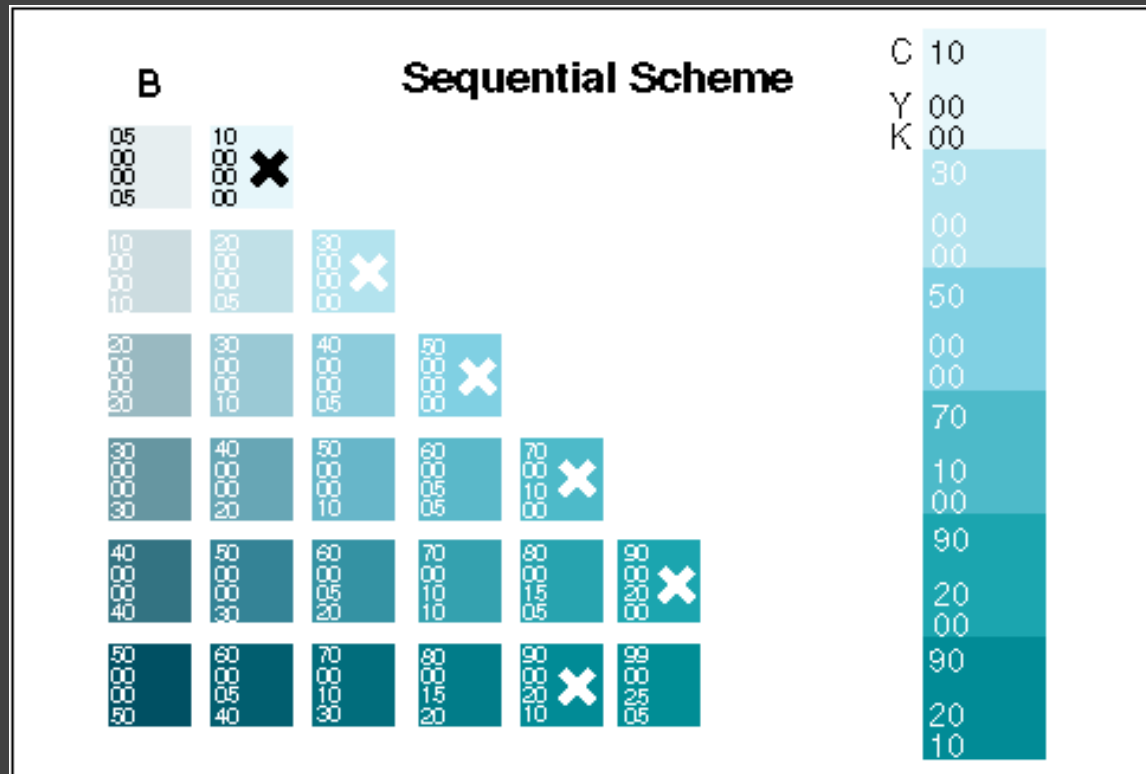
Ramp in luminance, possibly also hue

Higher value -> darker color (or vice versa)



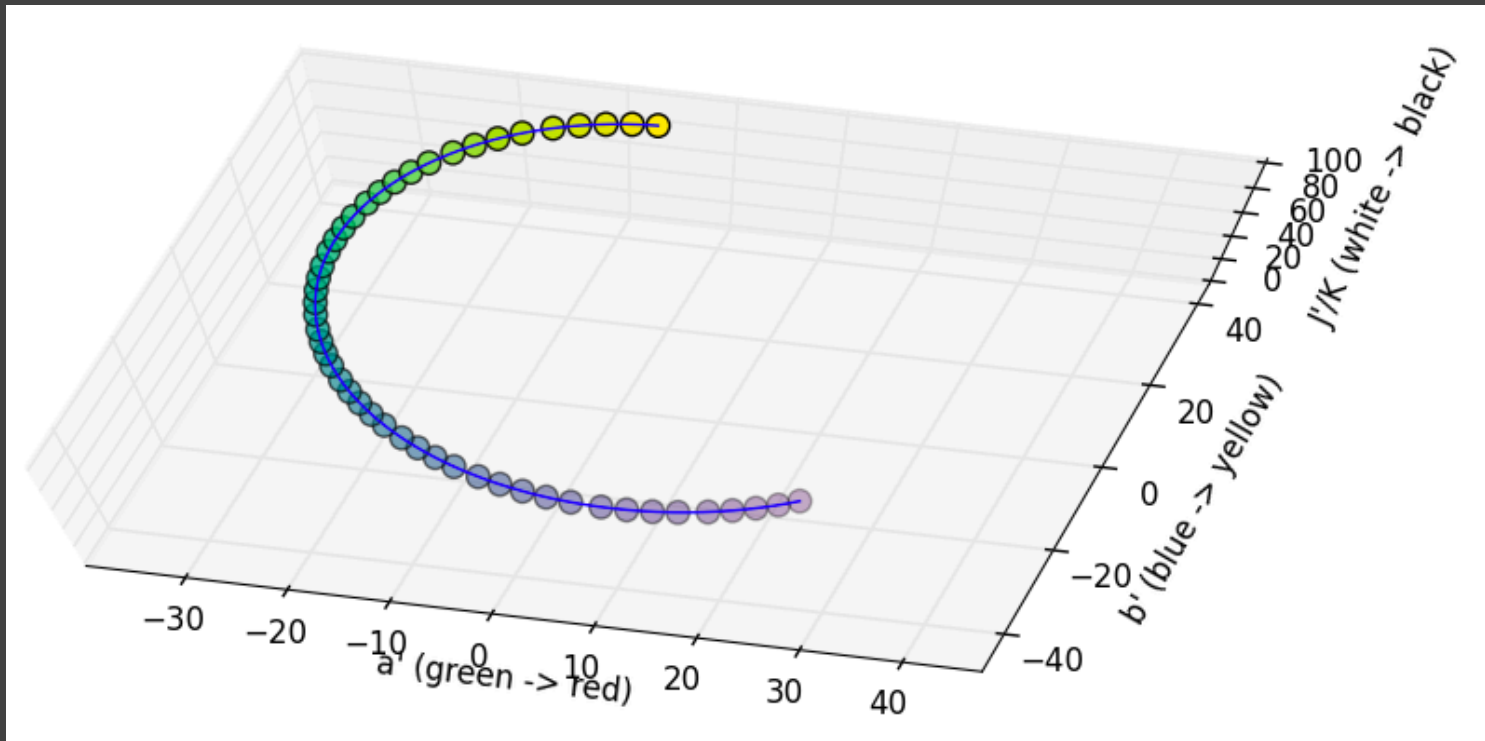
Sequential Scales: Single-Hue

Ramp primarily in luminance, subtle hue difference

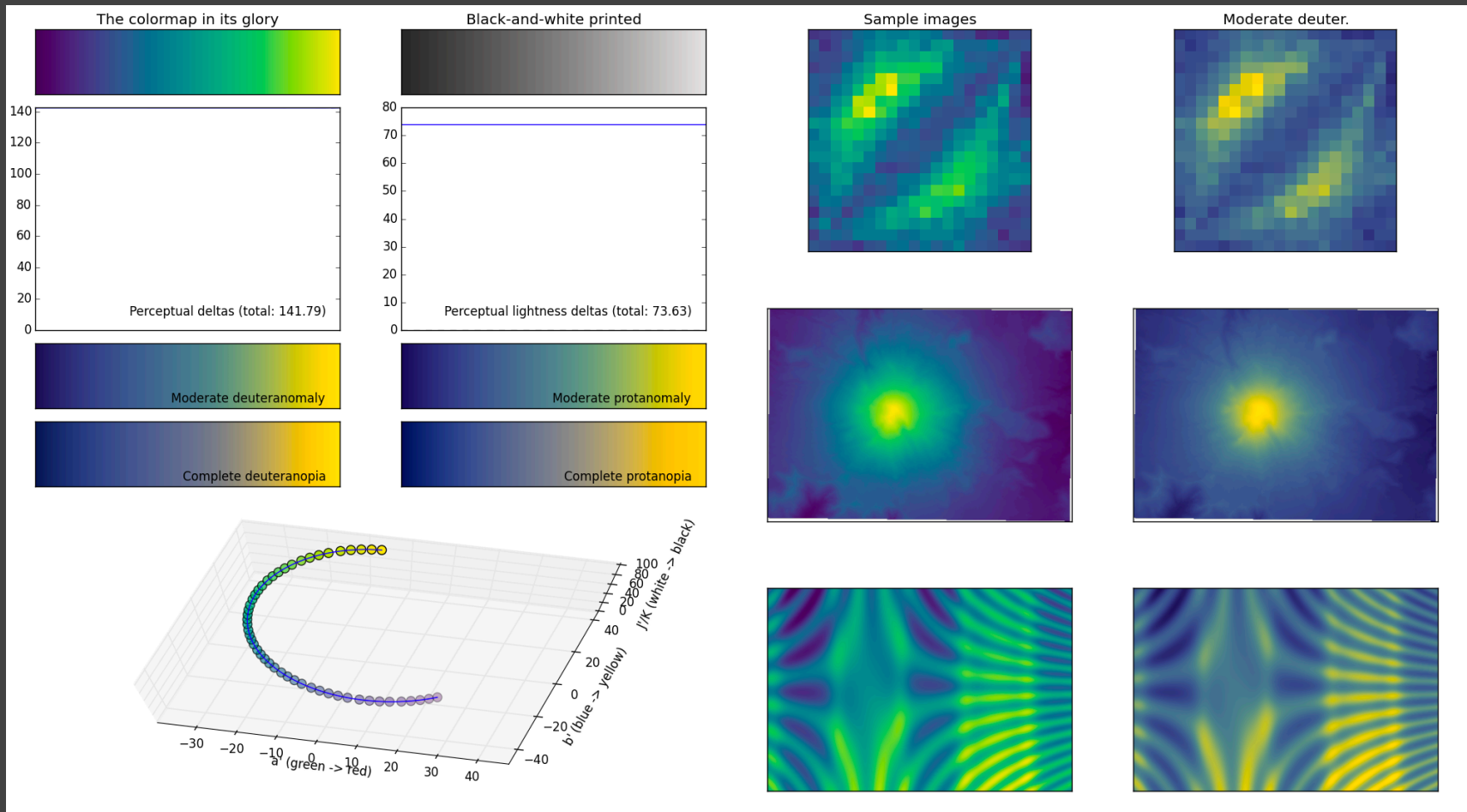


Sequential Scales: Multi-Hue

Ramp luminance & hue in perceptual color space
Avoid contrasts subject to color vision deficiency!



Sequential Scales: Multi-Hue



Quantitative Color Encoding

Sequential color scale

Ramp in luminance, possibly also hue

Higher value -> darker color (or vice versa)



Diverging color scale

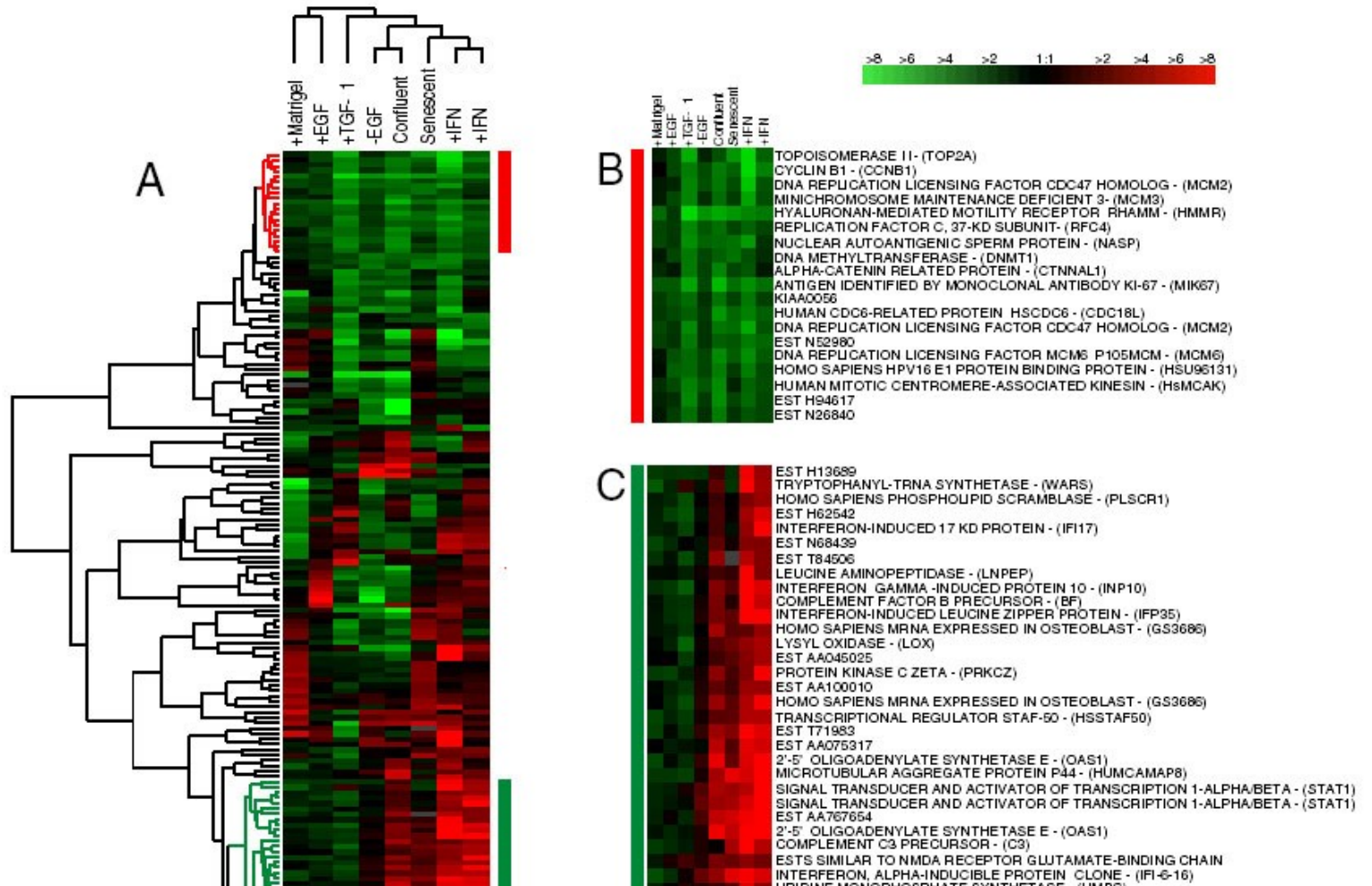
Useful when data has meaningful "midpoint"

Use neutral color (e.g., grey) for midpoint

Use saturated colors for endpoints



Diverging Color Scheme



Designing Diverging Scales

Hue Transition

Carefully Handle Midpoint

Choose classes of values

Low, Average, High - Average should be gray

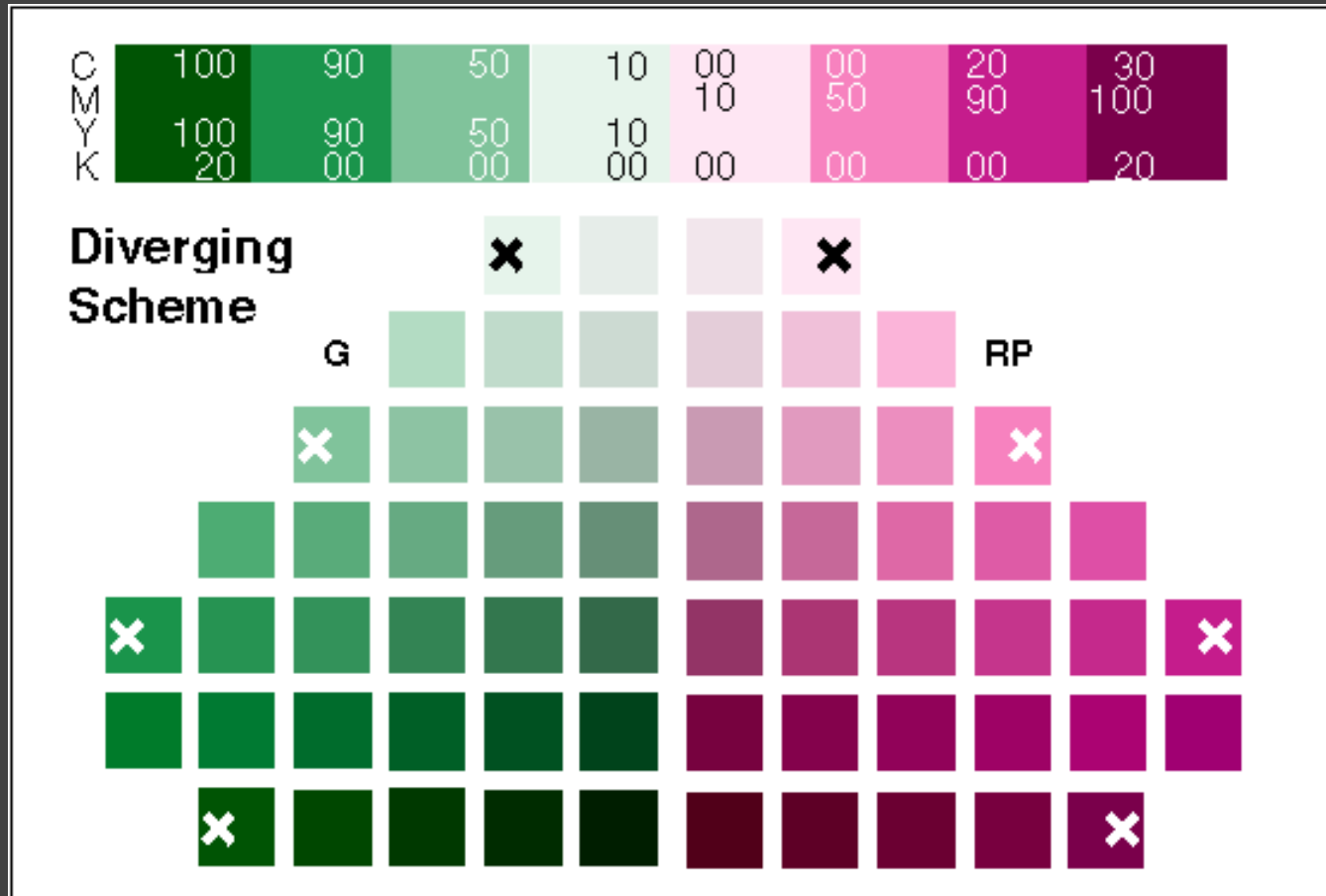
Critical Breakpoint

Defining value e.g., 0

Positive & negative should use different hues

Extremes saturated, middle desaturated

Designing Diverging Scales



Quantitative Color Encoding

Sequential color scale

Ramp in luminance, possibly also hue

Higher value -> darker color (or vice versa)



Diverging color scale

Useful when data has meaningful "midpoint"

Use neutral color (e.g., grey) for midpoint

Use saturated colors for endpoints



Limit number of steps in color to 3-9

Why?

Quantitative Color Encoding

Sequential color scale

Ramp in luminance, possibly also hue

Higher value -> darker color (or vice versa)



Diverging color scale

Useful when data has meaningful "midpoint"

Use neutral color (e.g., grey) for midpoint

Use saturated colors for endpoints



Limit number of steps in color to 3-9

Avoid simultaneous contrast, hold mappings in memory

Hints for the Colorist

Use **only a few** colors (~6 ideal)

Colors should be **distinctive** and **named**

Strive for color **harmony** (natural colors?)

Use **cultural conventions**; appreciate symbolism

Get it right in **black and white**

Respect people with **color vision deficiency**

Take advantage of **perceptual color spaces**

Color is cultural and a matter of taste!