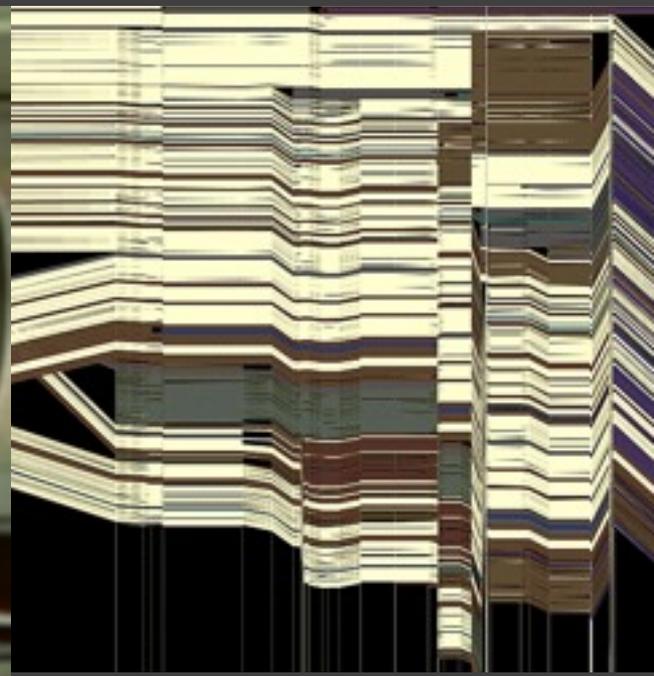
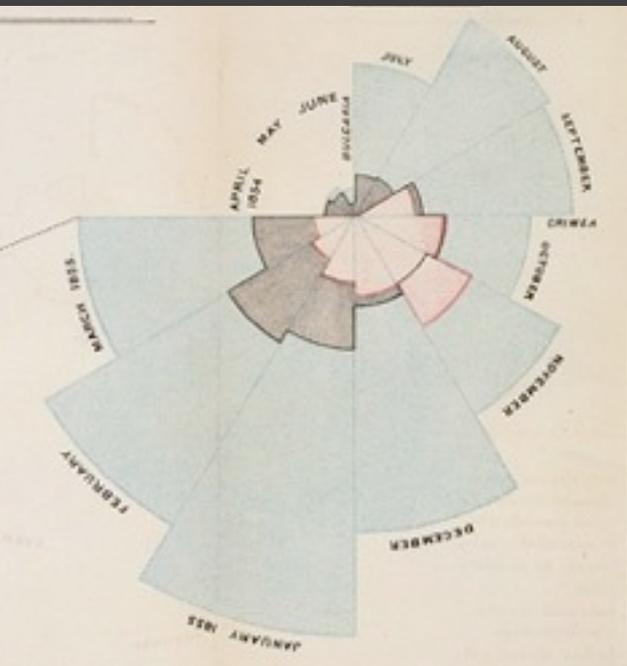


CSE512 :: 21 Jan 2014

# Multi-Dimensional Vis



**Jeffrey Heer** University of Washington

# Last Time: Exploratory Data Analysis



Exposure, the effective laying open of the data to display the unanticipated, is to us a major portion of data analysis. Formal statistics has given almost no guidance to exposure; indeed, it is not clear how the informality and flexibility appropriate to the exploratory character of exposure can be fitted into any of the structures of formal statistics so far proposed.

### Graph Viewer

Roll-up by:

All

Visualization:

Node-Link

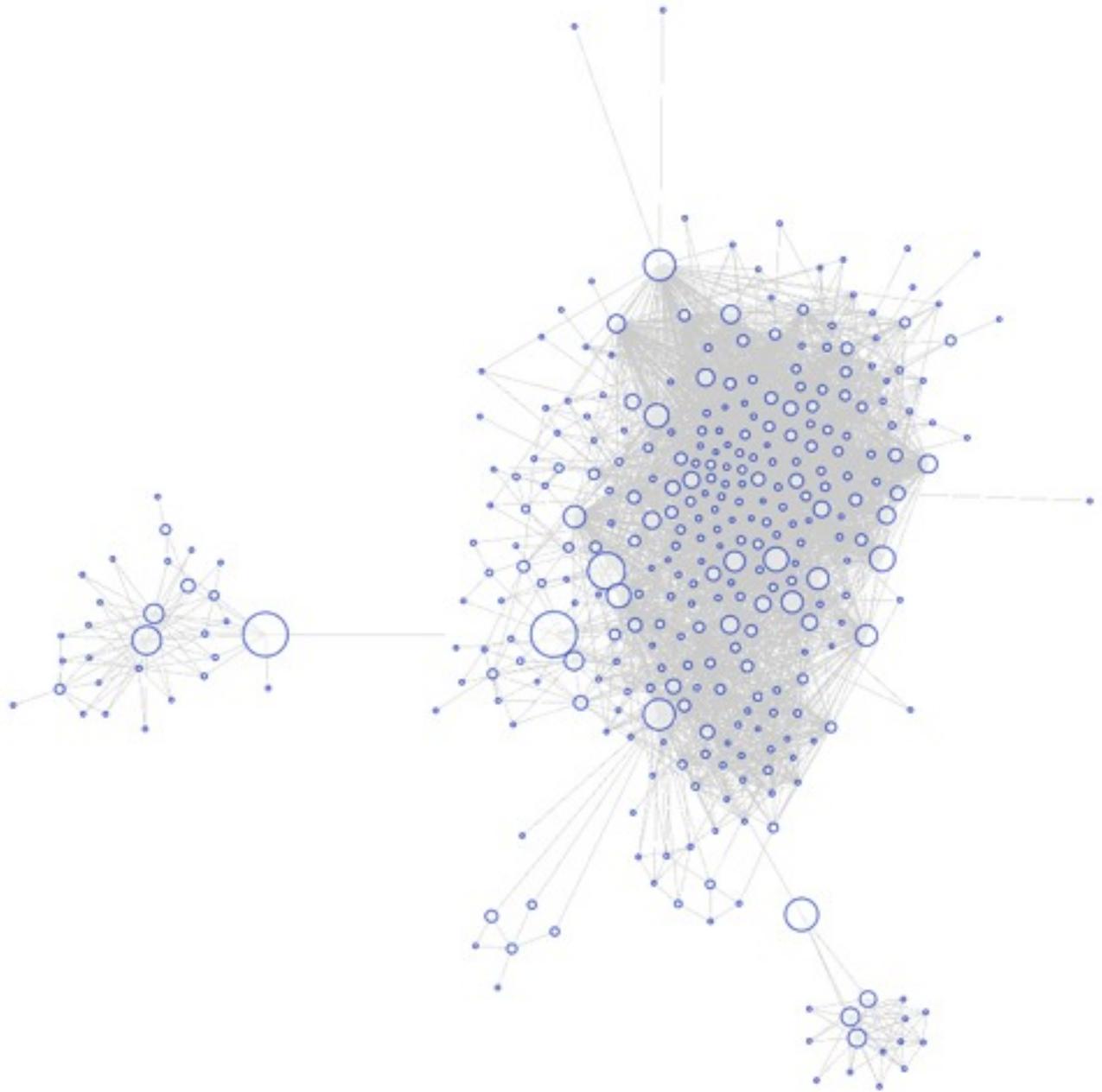
Sort by:

None

Edge centrality filters:

Two horizontal sliders for edge centrality filtering.

- Images
- Animate



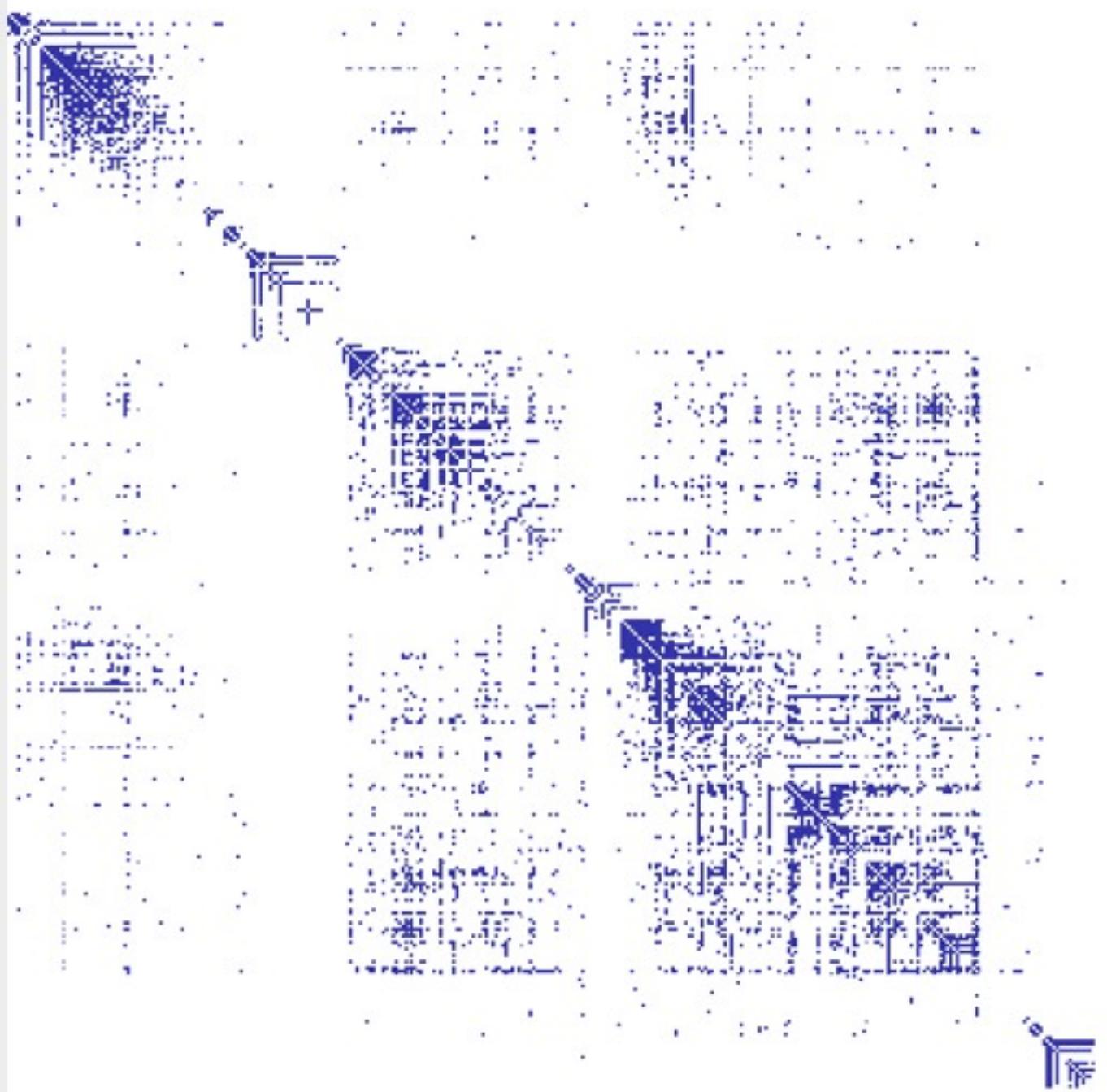
# Graph Viewer

Roll-up by:

Visualization:

Sort by:

Edge centrality filters:



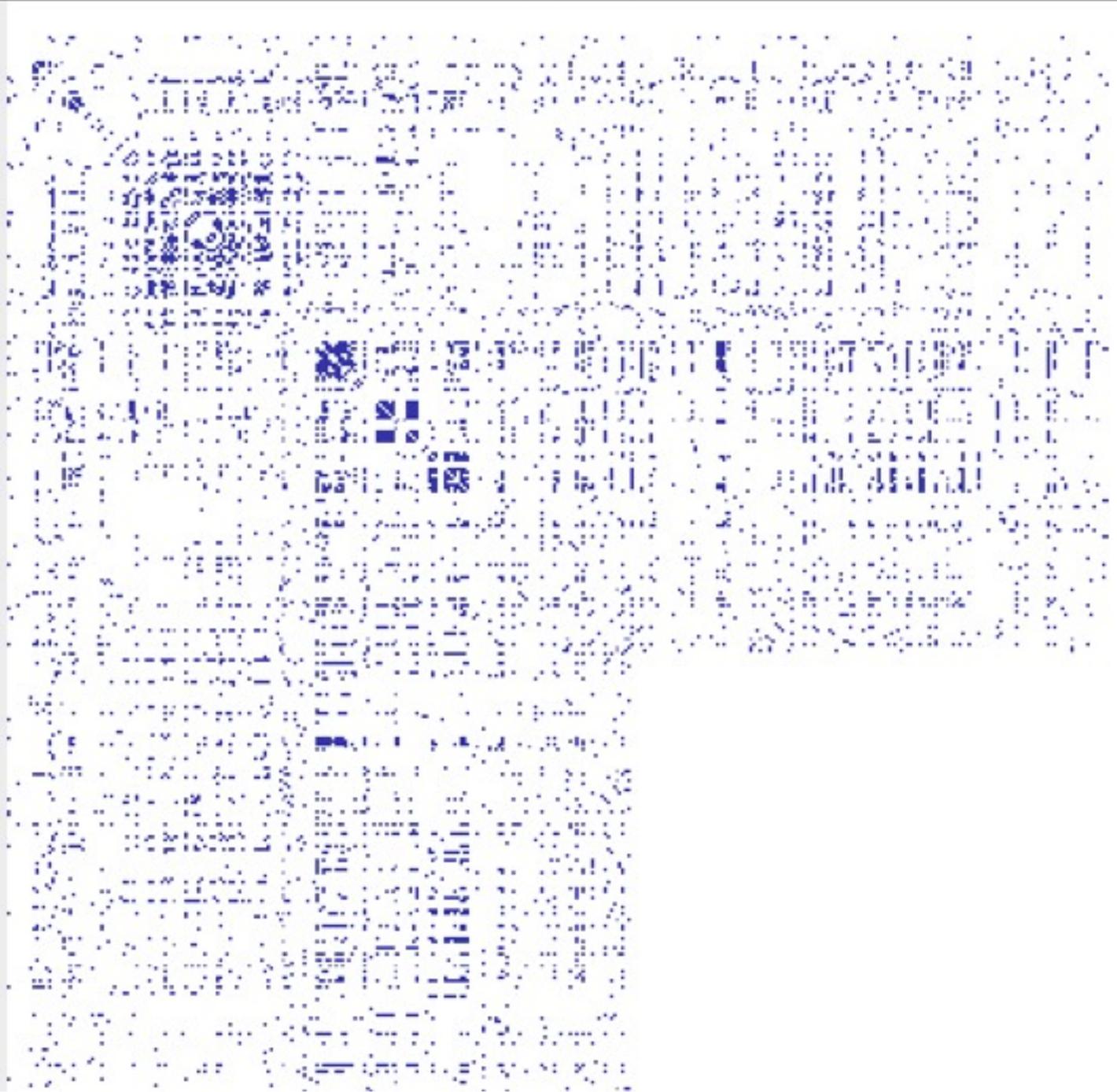
# Graph Viewer

Roll-up by:

Visualization:

Sort by:

Edge centrality filters:

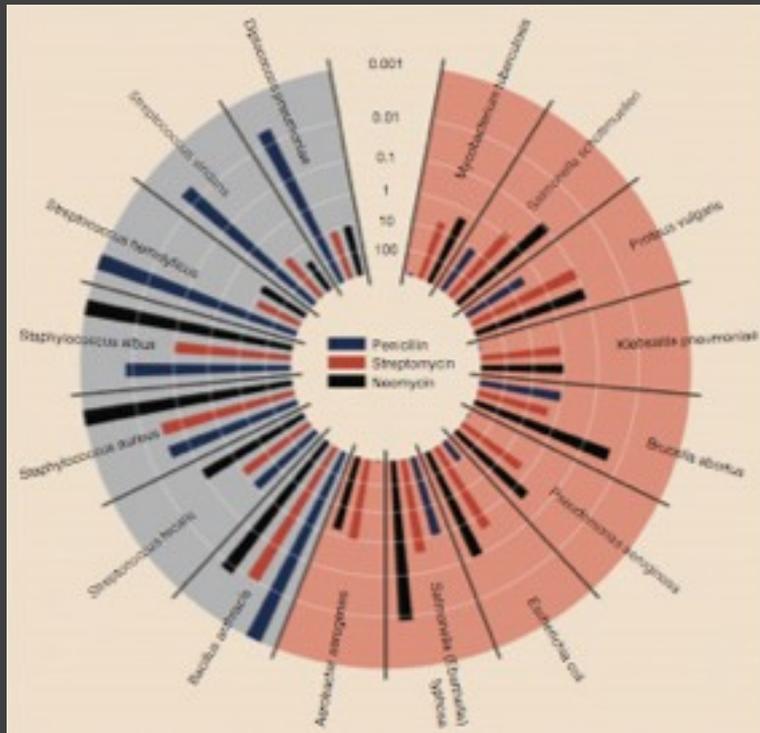


# Antibiotic Effectiveness

Table 1: Burtin's data.

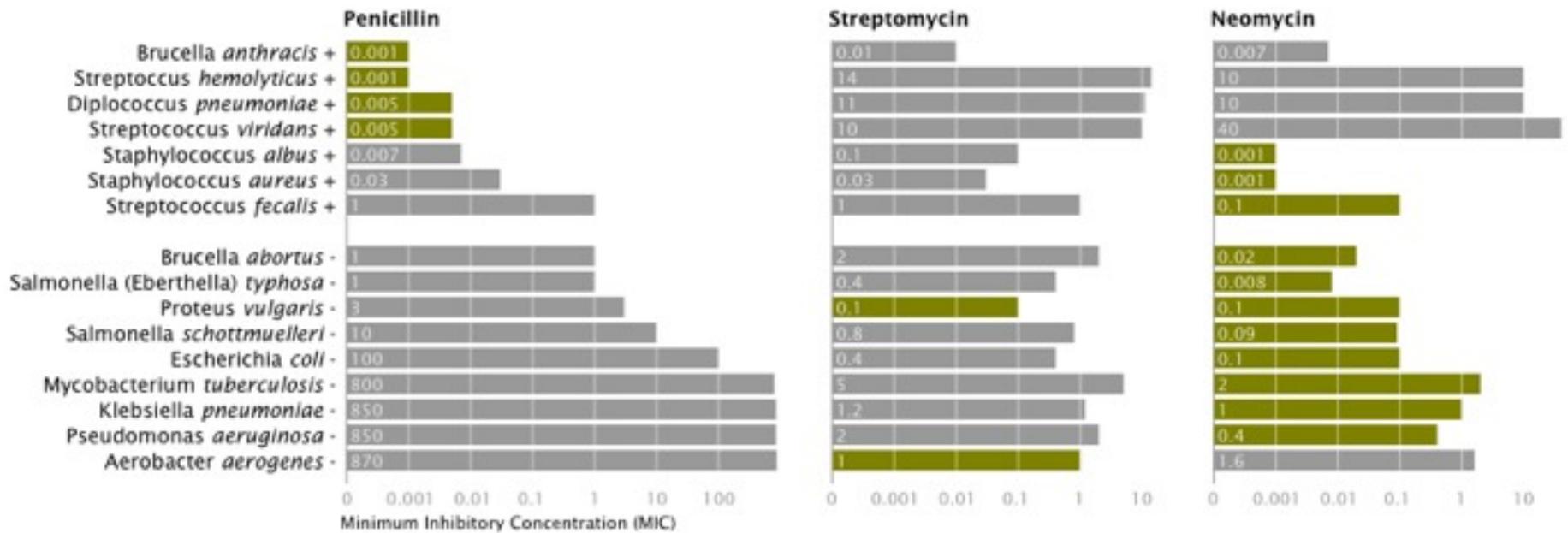
Bacteria	Antibiotic			Gram Staining
	Penicillin	Streptomycin	Neomycin	
<i>Aerobacter aerogenes</i>	870	1	1.6	negative
<i>Brucella abortus</i>	1	2	0.02	negative
<i>Brucella anthracis</i>	0.001	0.01	0.007	positive
<i>Diplococcus pneumoniae</i>	0.005	11	10	positive
<i>Escherichia coli</i>	100	0.4	0.1	negative
<i>Klebsiella pneumoniae</i>	850	1.2	1	negative
<i>Mycobacterium tuberculosis</i>	800	5	2	negative
<i>Proteus vulgaris</i>	3	0.1	0.1	negative
<i>Pseudomonas aeruginosa</i>	850	2	0.4	negative
<i>Salmonella (Eberthella) typhosa</i>	1	0.4	0.008	negative
<i>Salmonella schottmuelleri</i>	10	0.8	0.09	negative
<i>Staphylococcus albus</i>	0.007	0.1	0.001	positive
<i>Staphylococcus aureus</i>	0.03	0.03	0.001	positive
<i>Streptococcus fecalis</i>	1	1	0.1	positive
<i>Streptococcus hemolyticus</i>	0.001	14	10	positive
<i>Streptococcus viridans</i>	0.005	10	40	positive

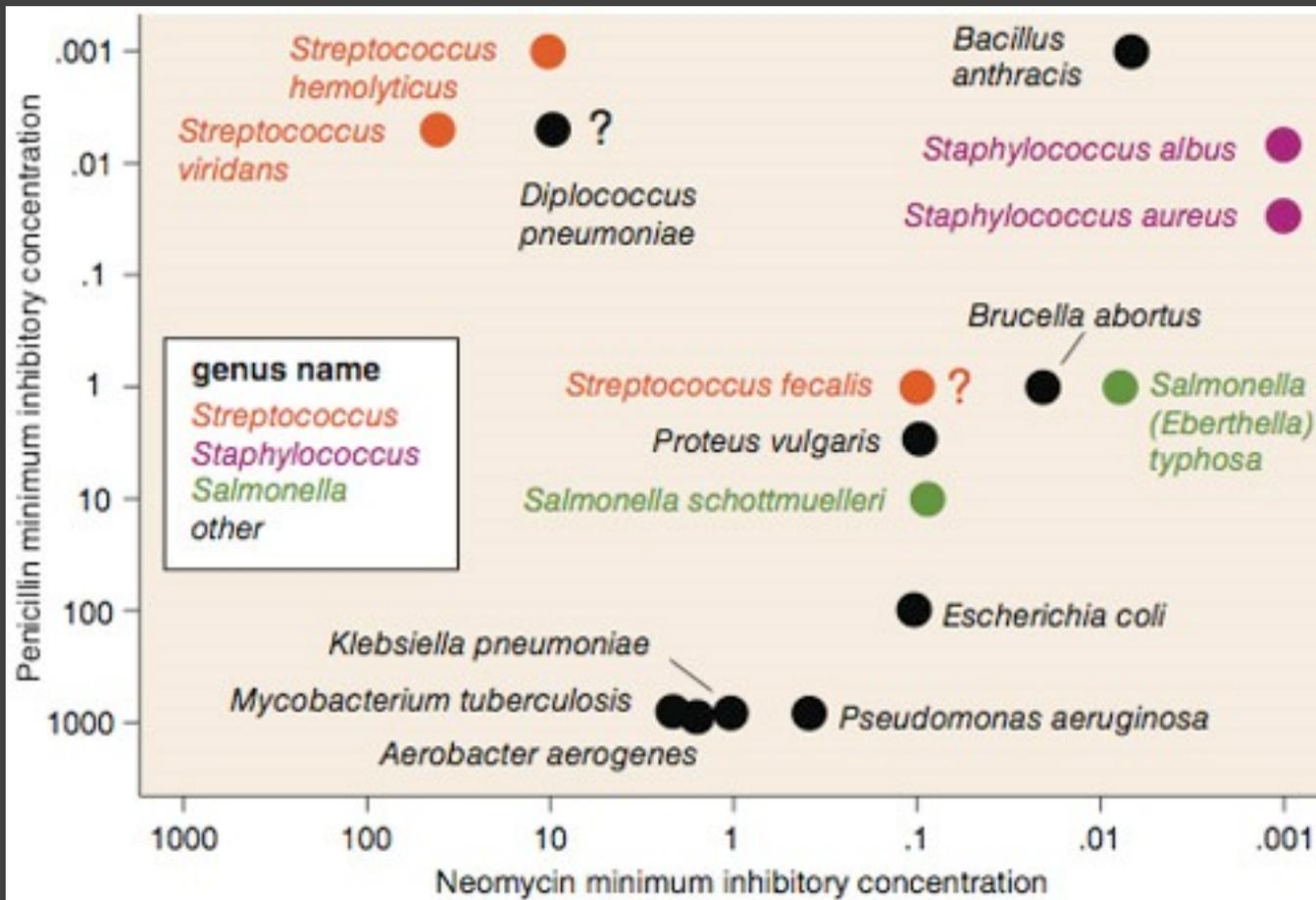
# Will Burtin, 1951



Bacteria	Penicillin	Antibiotic Streptomycin	Neomycin	Gram stain
<i>Aerobacter aerogenes</i>	870	1	1.6	-
<i>Brucella abortus</i>	1	2	0.02	-
<i>Bacillus anthracis</i>	0.001	0.01	0.007	+
<i>Diplococcus pneumoniae</i>	0.005	11	10	+
<i>Escherichia coli</i>	100	0.4	0.1	-
<i>Klebsiella pneumoniae</i>	850	1.2	1	-
<i>Mycobacterium tuberculosis</i>	800	5	2	-
<i>Proteus vulgaris</i>	3	0.1	0.1	-
<i>Pseudomonas aeruginosa</i>	850	2	0.4	-
<i>Salmonella (Eberthella) typhosa</i>	1	0.4	0.008	-
<i>Salmonella schottmuelleri</i>	10	0.8	0.09	-
<i>Staphylococcus albus</i>	0.007	0.1	0.001	+
<i>Staphylococcus aureus</i>	0.03	0.03	0.001	+
<i>Streptococcus fecalis</i>	1	1	0.1	+
<i>Streptococcus hemolyticus</i>	0.001	14	10	+
<i>Streptococcus viridans</i>	0.005	10	40	+

How do the drugs compare?



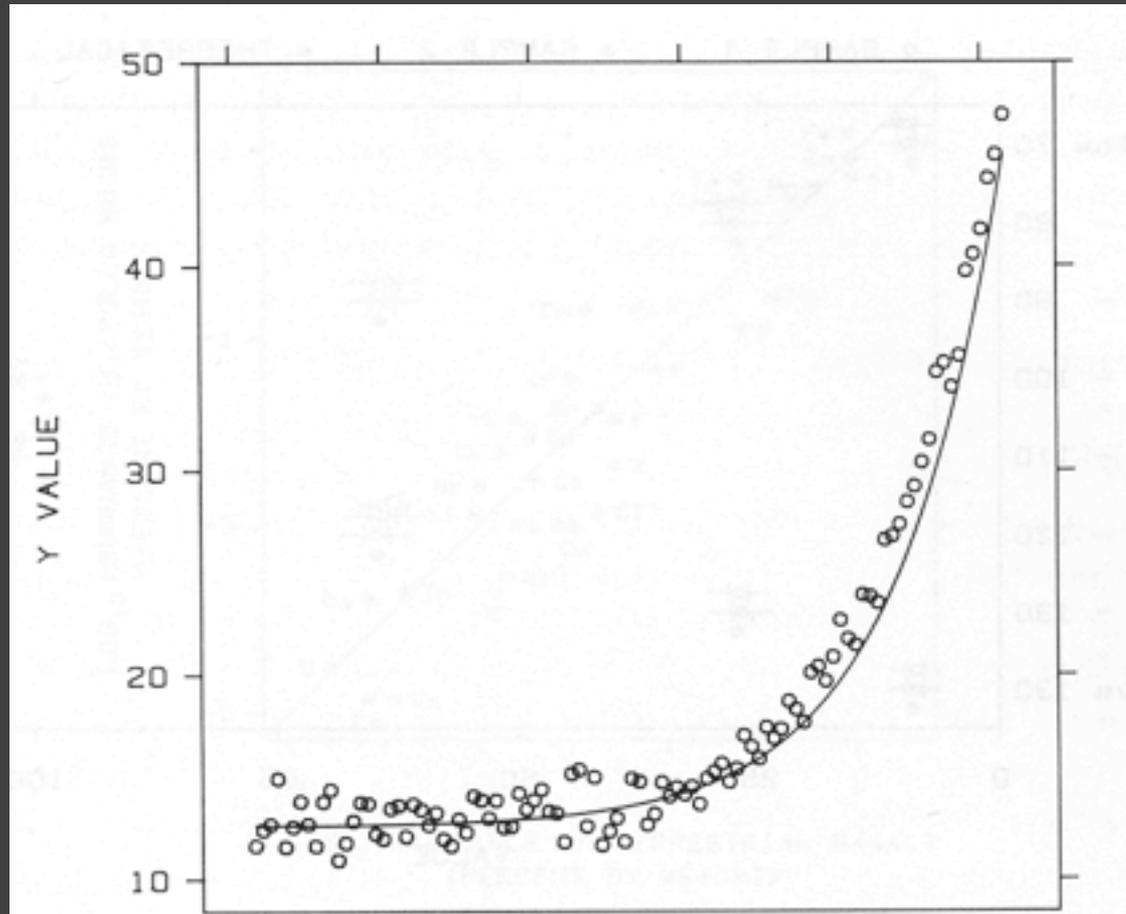


How do the bacteria group w.r.t. resistance?  
 Do different drugs correlate?

Wainer & Lysen  
 American Scientist, 2009

# Transforming data

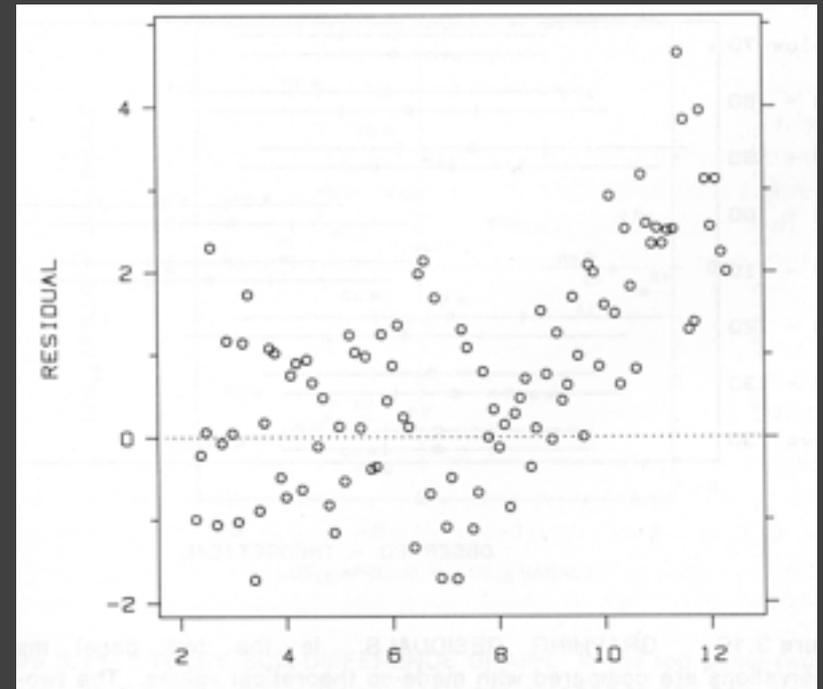
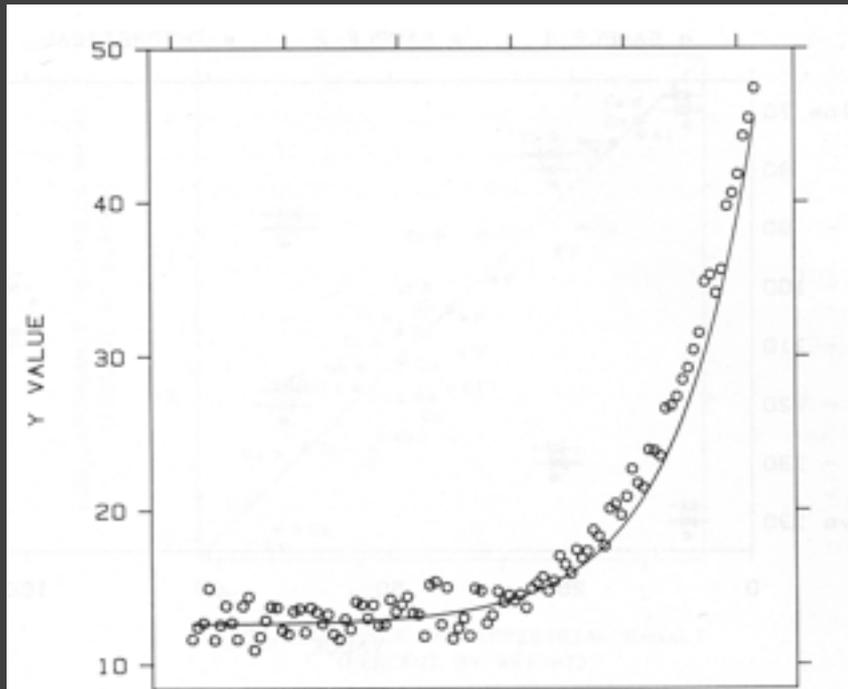
How well does the curve fit data?



[Cleveland 85]

# Plot the Residuals

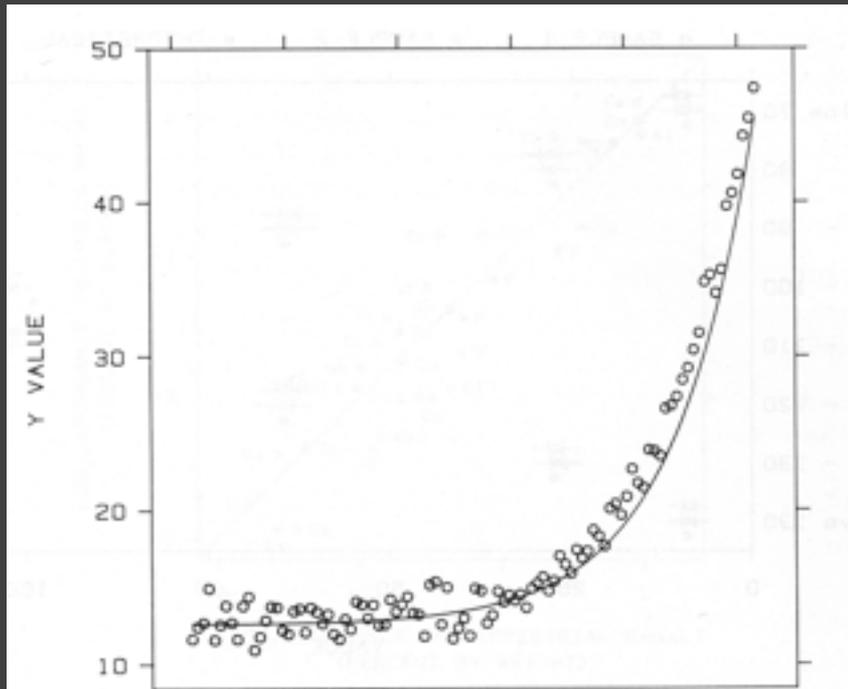
Plot vertical distance from best fit curve  
Residual graph shows accuracy of fit



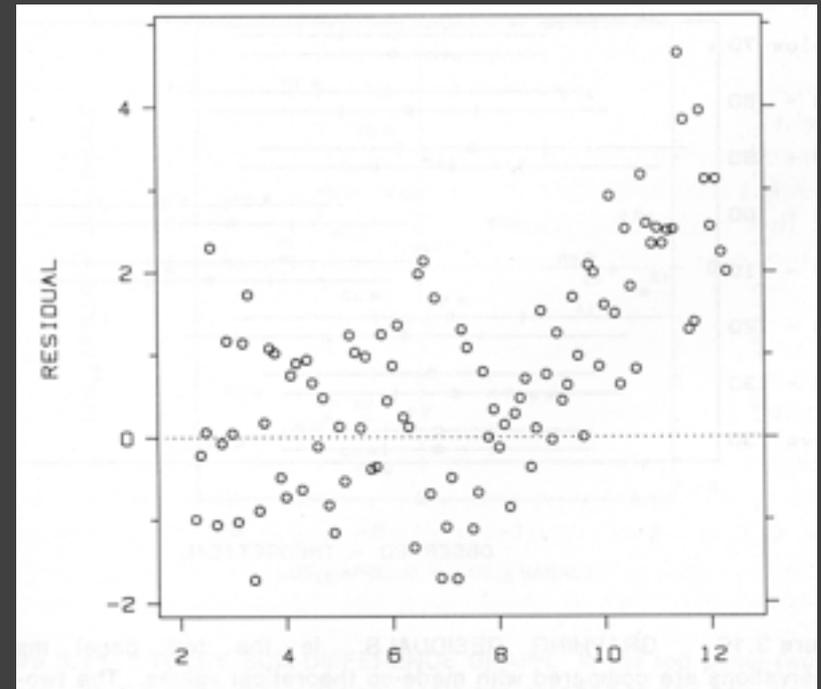
[Cleveland 85]

# Multiple Plotting Options

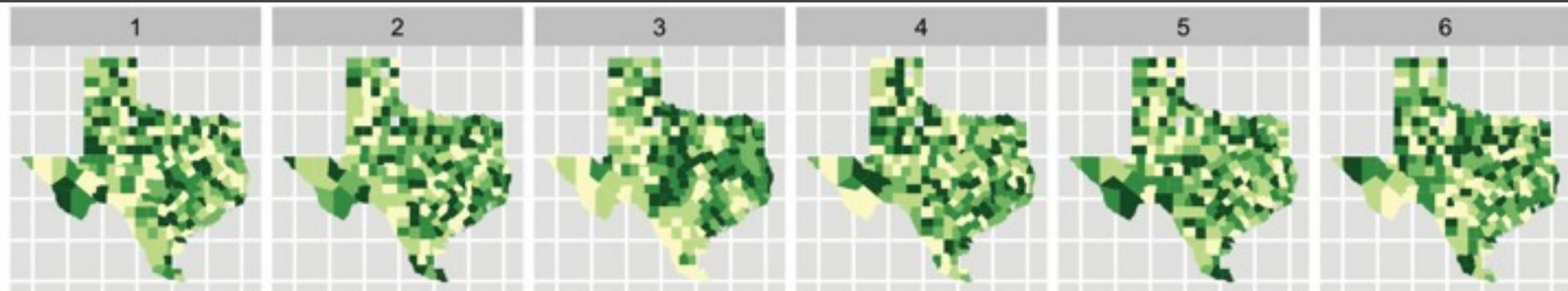
Plot model in data space



Plot data in model space



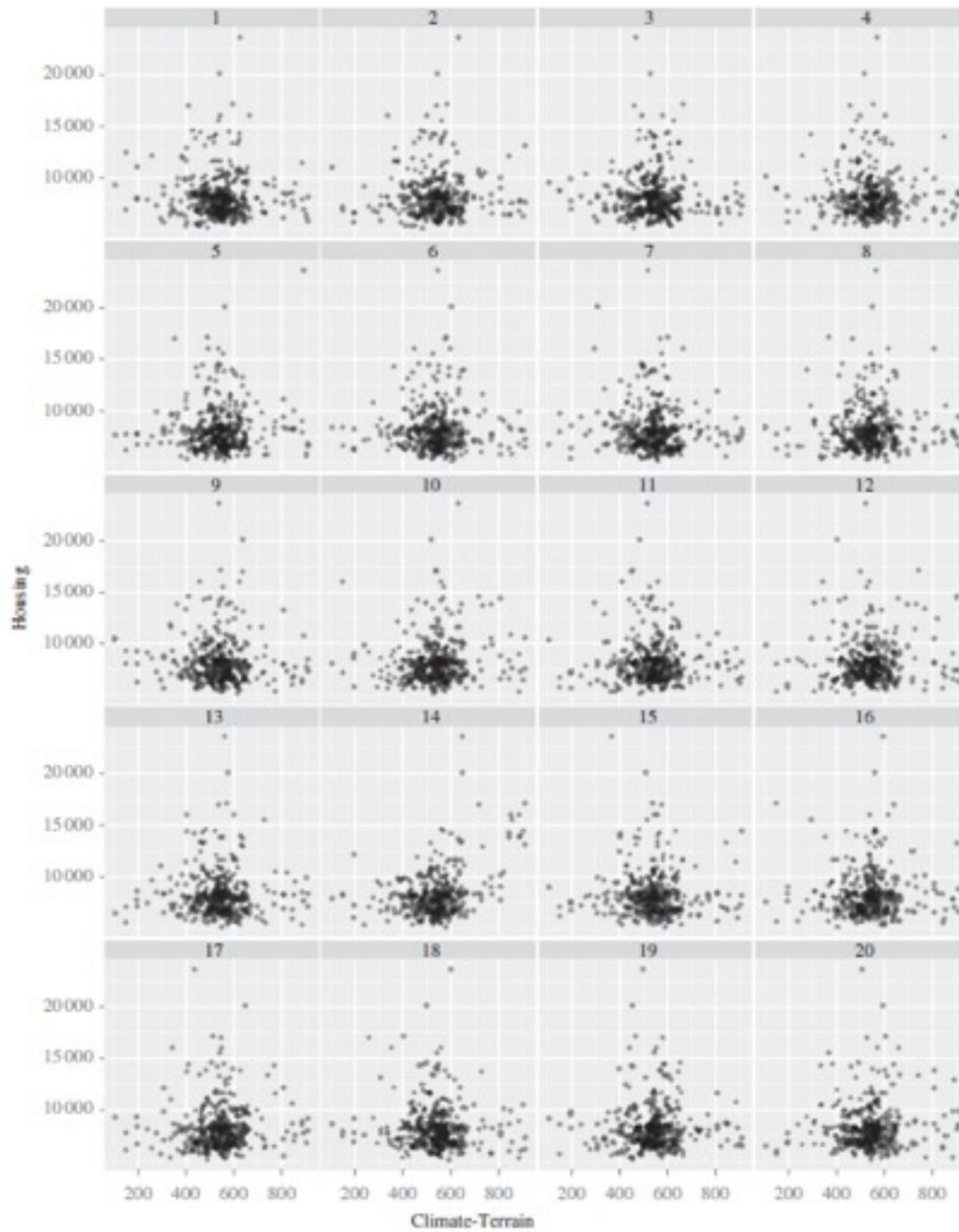
[Cleveland 85]



## **Choropleth maps of cancer deaths in Texas.**

One plot shows a real data sets. The others are simulated under the null hypothesis of spatial independence.

Can you spot the real data? If so, you have some evidence of spatial dependence in the data.



# Multidimensional Visualization

# Visual Encoding Variables

Position  
Length

Area

Volume

Value

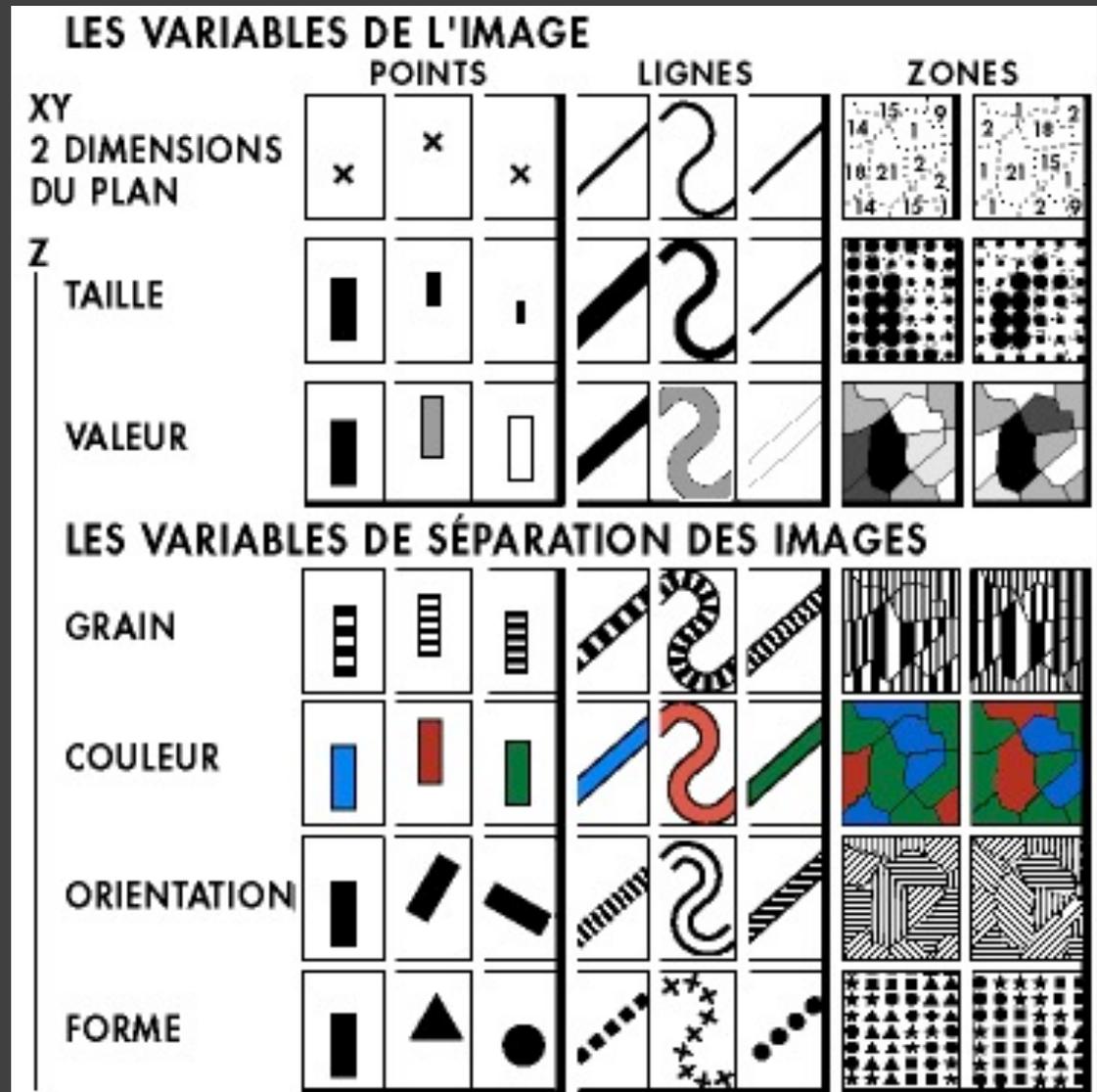
Texture

Color

Orientation

Shape

~8 dimensions?



# Example: Coffee Sales

Sales figures for a fictional coffee chain:

Sales                      Q-Ratio

Profit                      Q-Ratio

Marketing                Q-Ratio

Product Type     $N$  {Coffee, Espresso, Herbal Tea, Tea}

Market                     $N$  {Central, East, South, West}

Filters

YEAR(Date): 2010

Marks

x+ Automatic

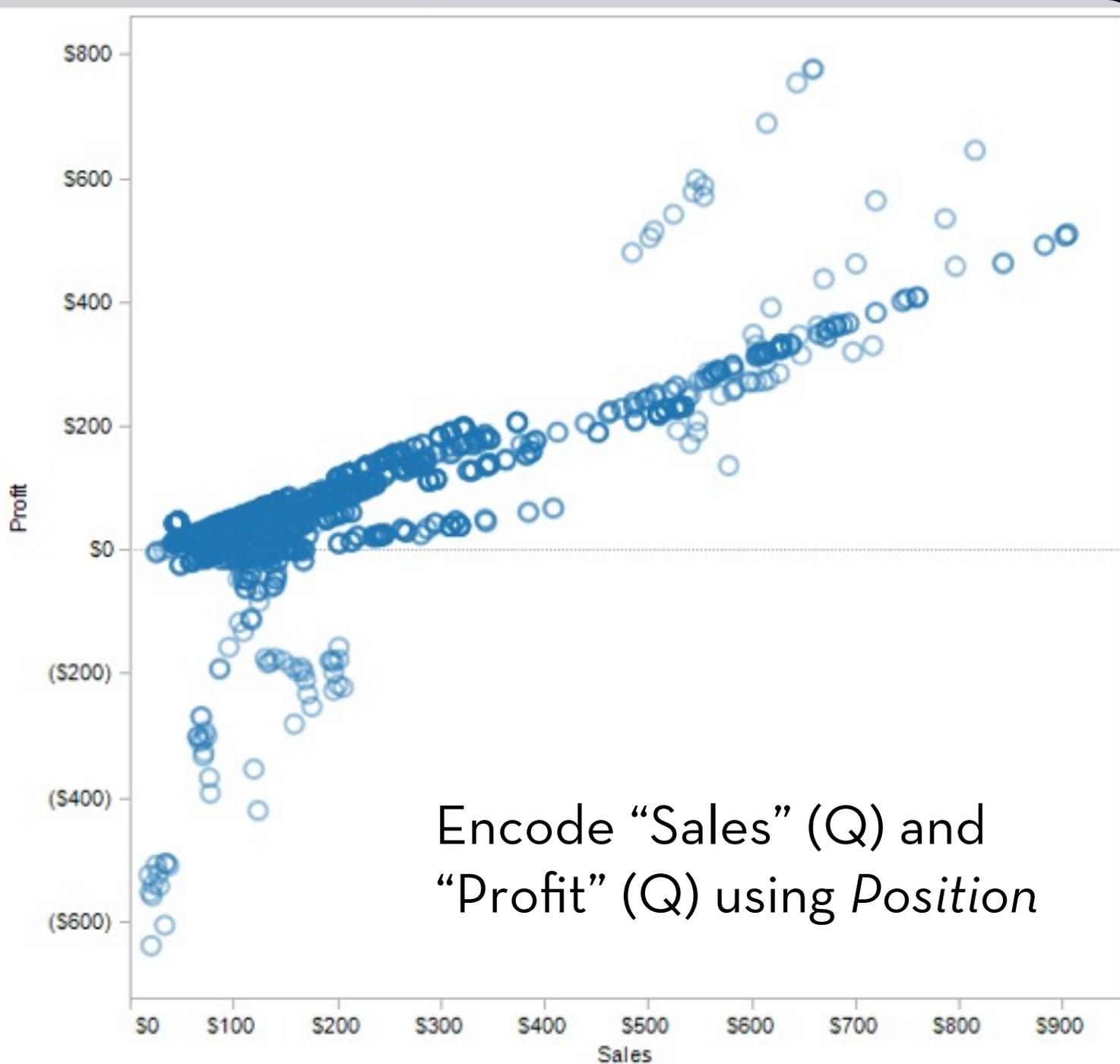
Shape ○

Label ▾

Color ▾

Size

Level of Detail



Filters

YEAR(Date): 2010

Marks

x+ Automatic

Shape ○

Label

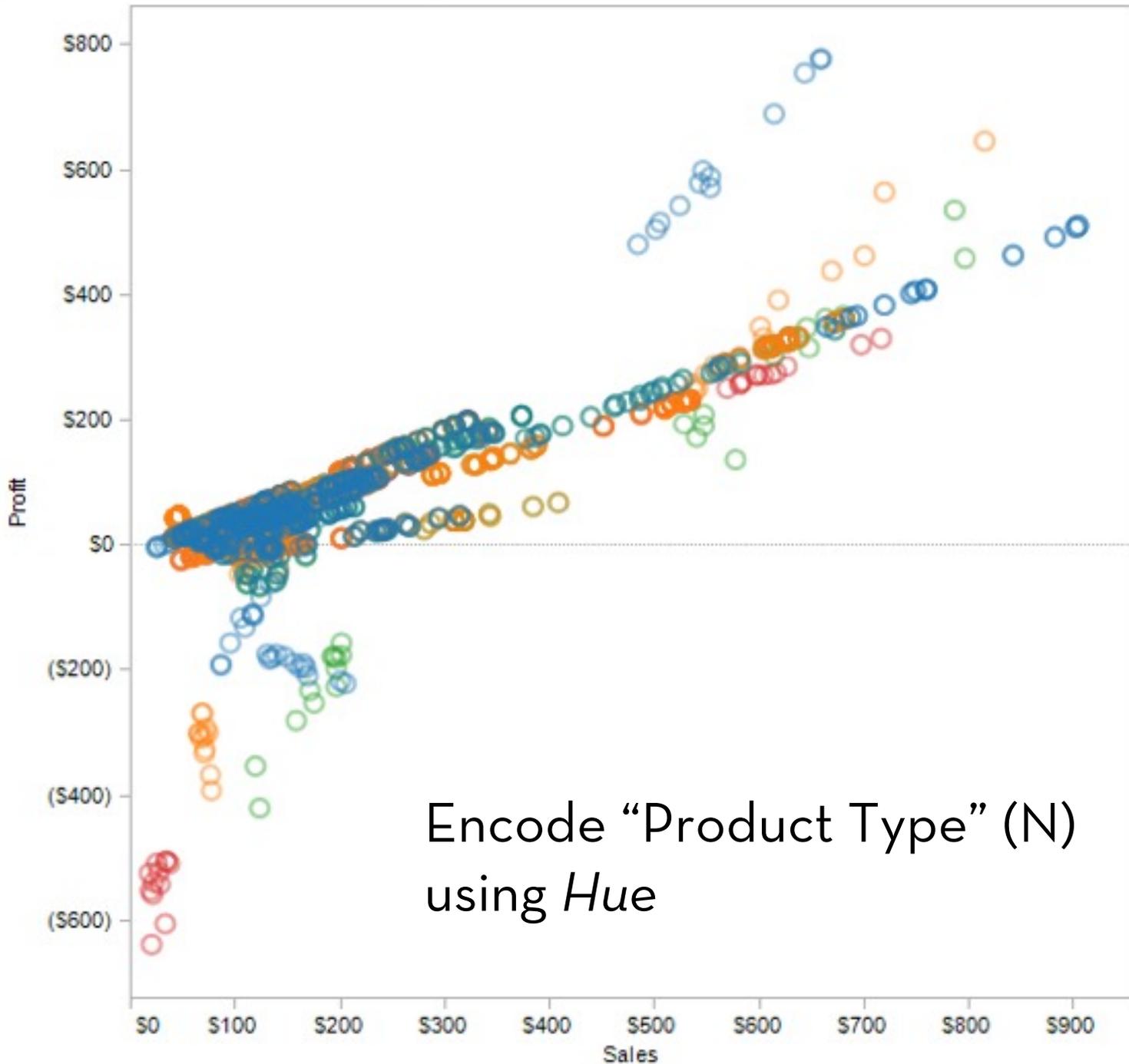
Color Product Type

Size

Level of Detail

Product Type

- Coffee
- Espresso
- Herbal Tea
- Tea



Filters

YEAR(Date): 2010

---

Marks

Automatic

Shape Market

Label Market

Color Product Type

Size

Level of Detail

---

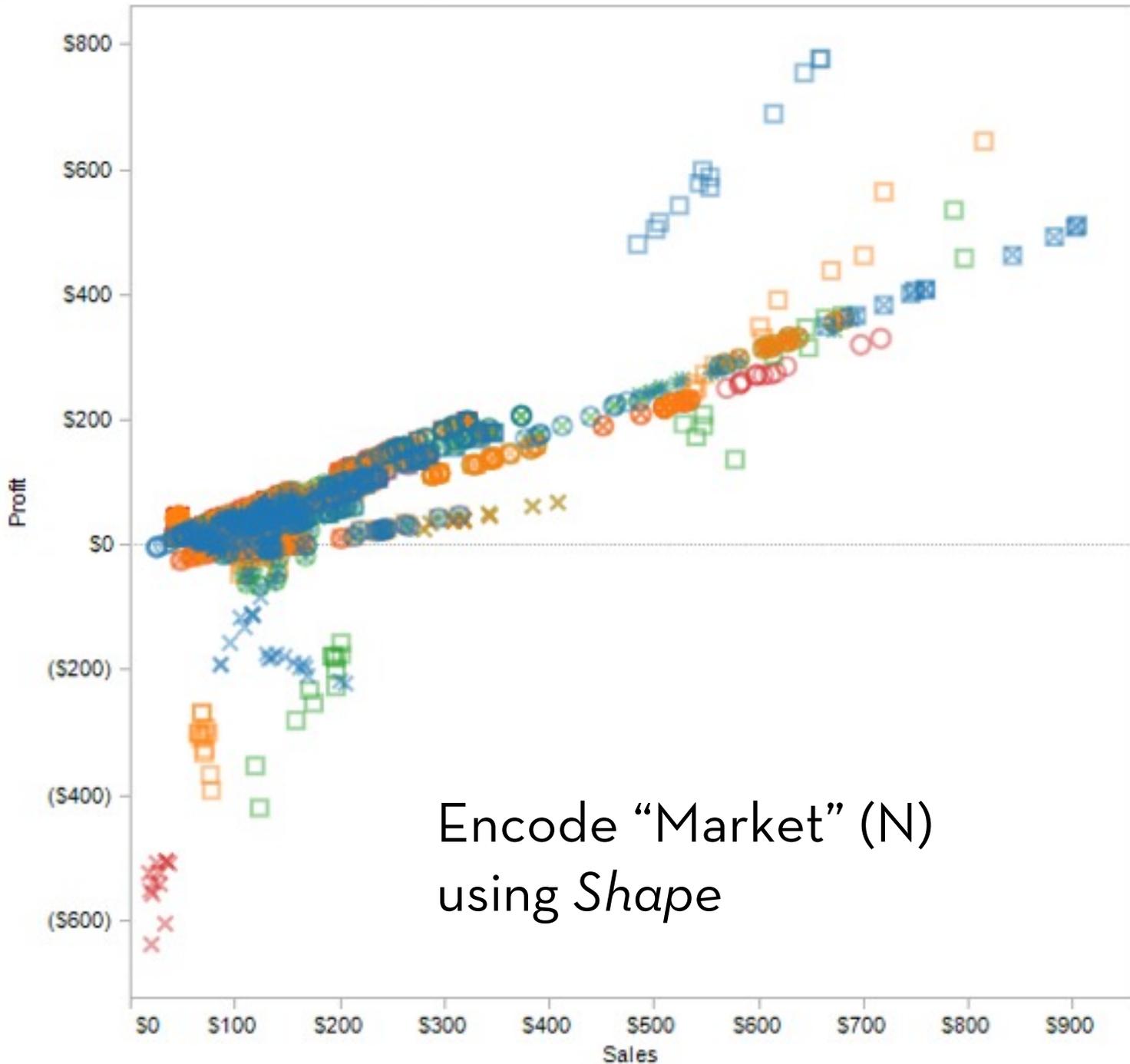
Product Type

- Coffee
- Espresso
- Herbal Tea
- Tea

---

Market

- Central
- East
- South
- West



Filters

YEAR(Date): 2010

---

Marks

Automatic

Shape Market

Label

Color Product Type

Size Marketing

Marketing

Level of Detail

---

Product Type

- Coffee
- Espresso
- Herbal Tea

---

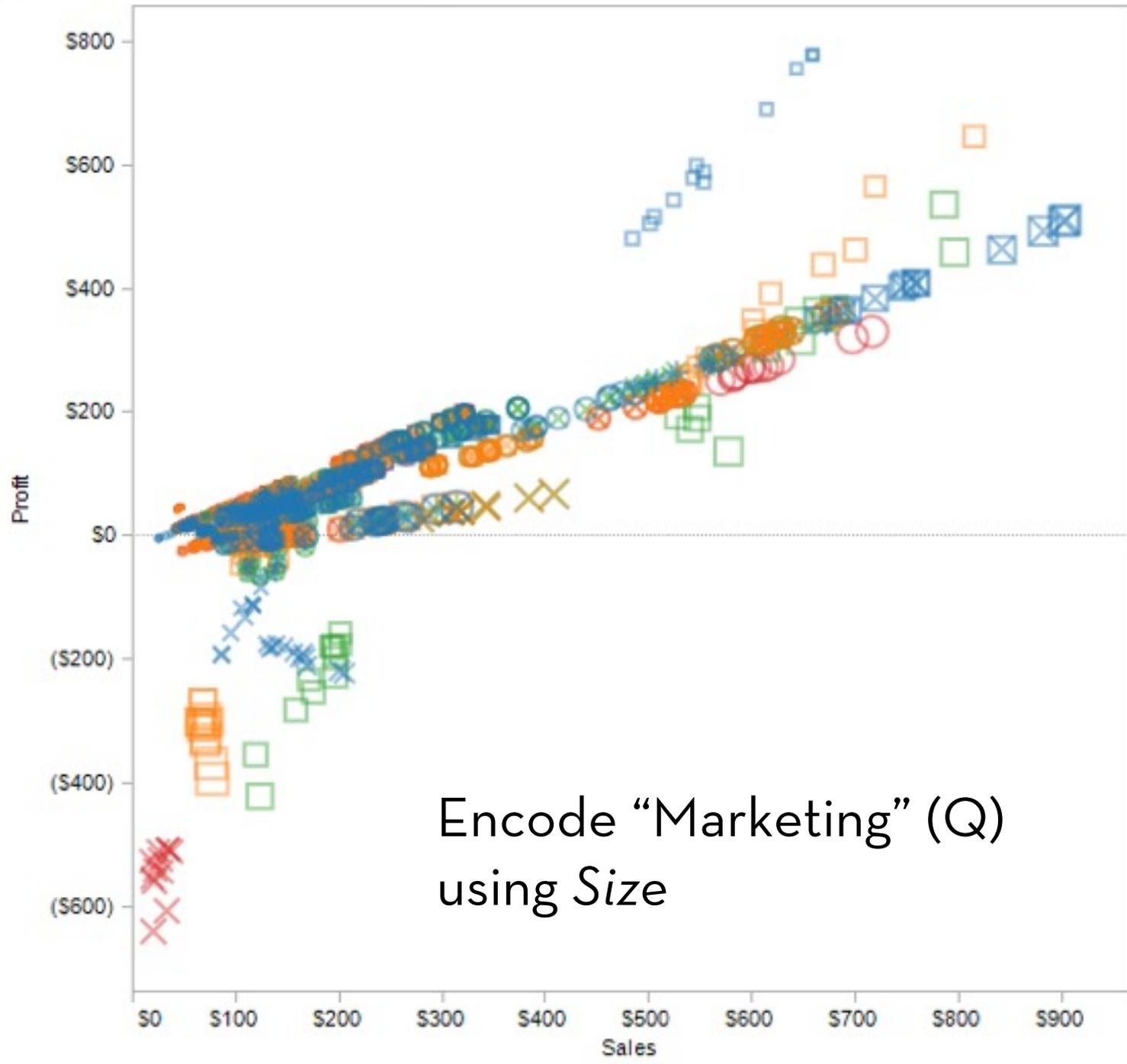
Market

- Central
- East
- South

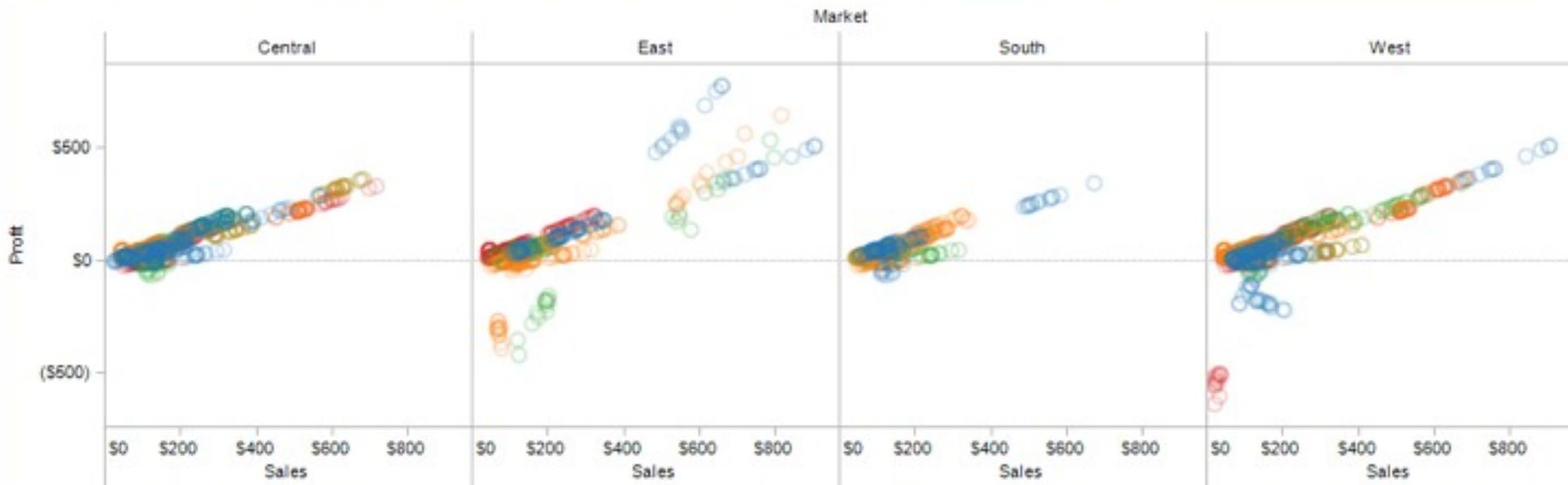
---

Marketing

- \$0
- \$50
- \$100



# Trellis Plots



A *trellis plot* subdivides space to enable comparison across multiple plots.

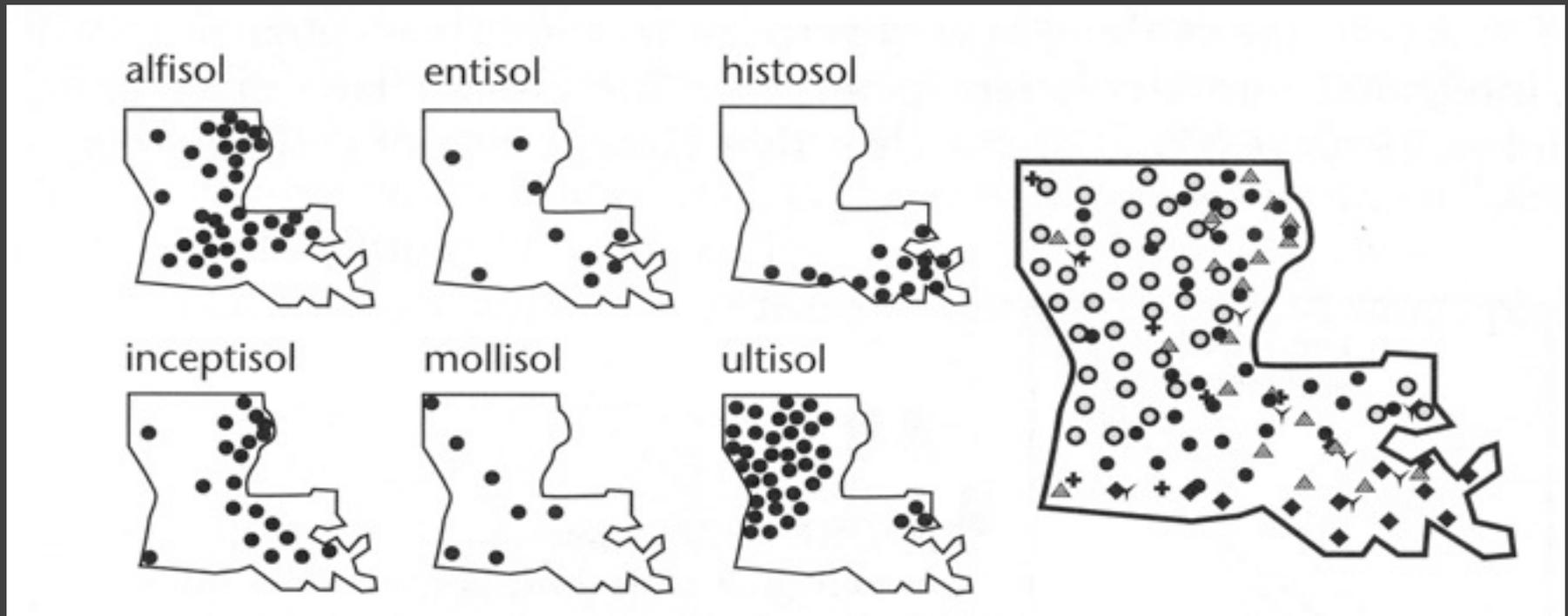
Typically nominal or ordinal variables are used as dimensions for subdivision.

# Separation: Small Multiples



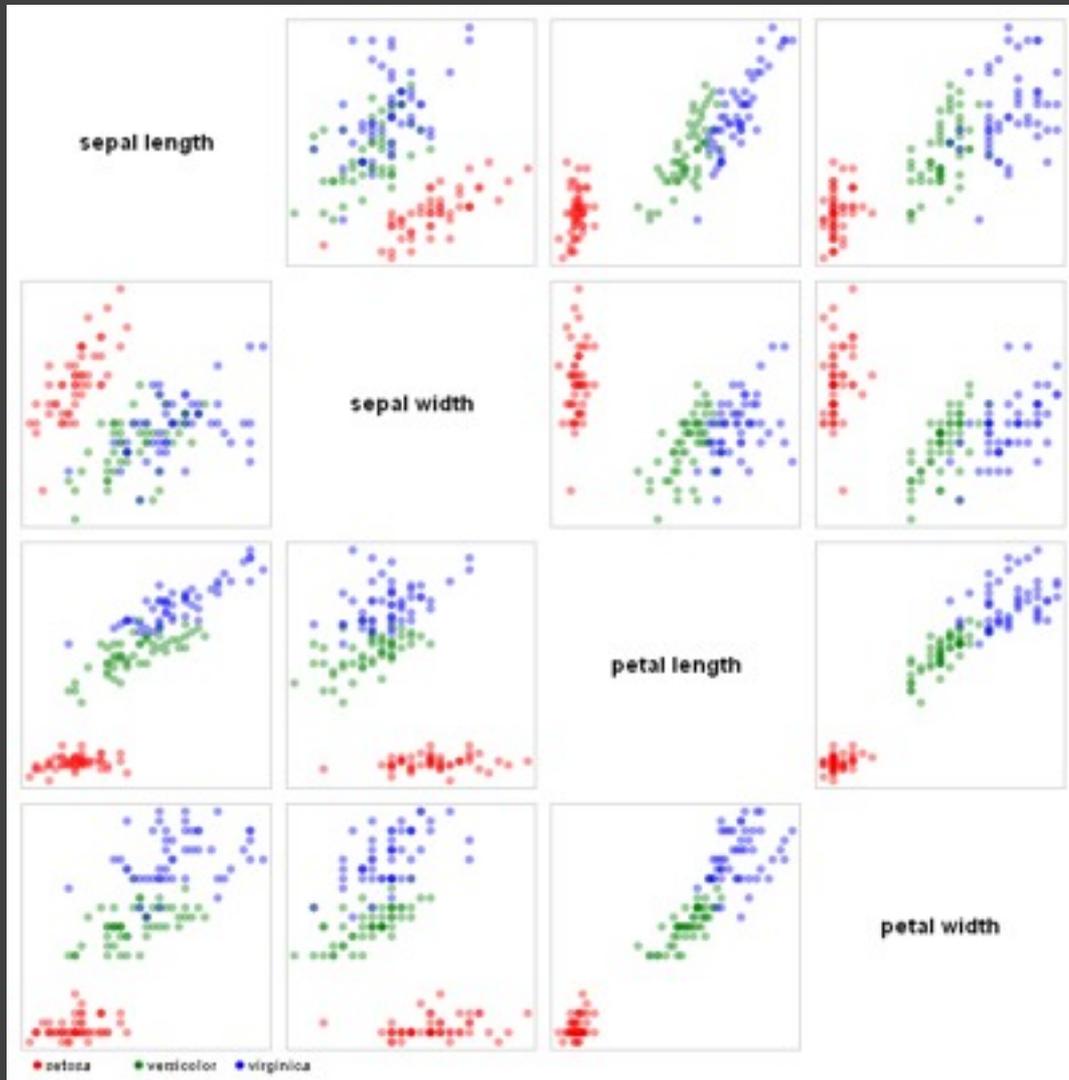
[Figure 2.11, p. 38, MacEachren 95]

# Separation: Small Multiples

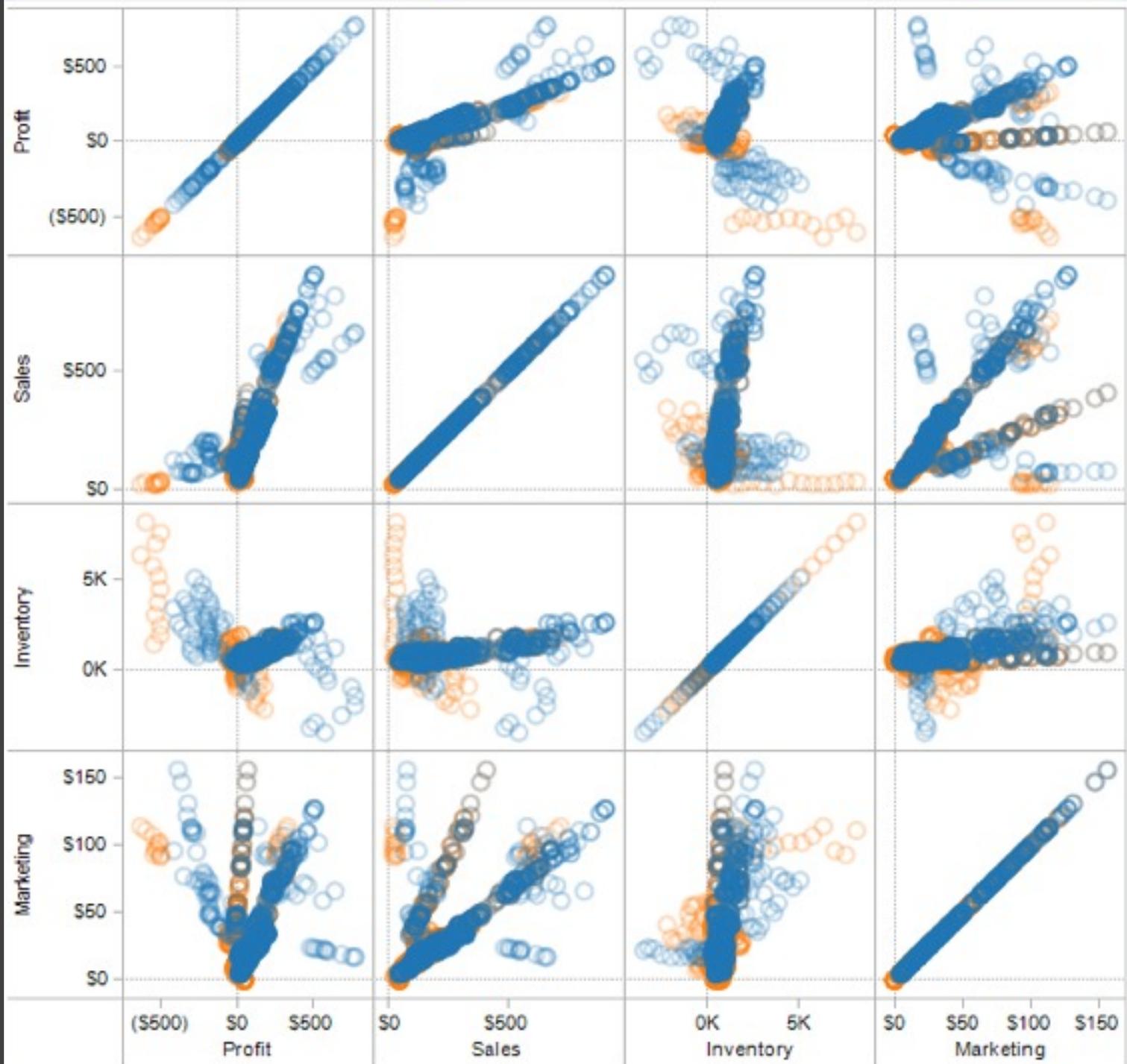


[Figure 2.11, p. 38, MacEachren 95]

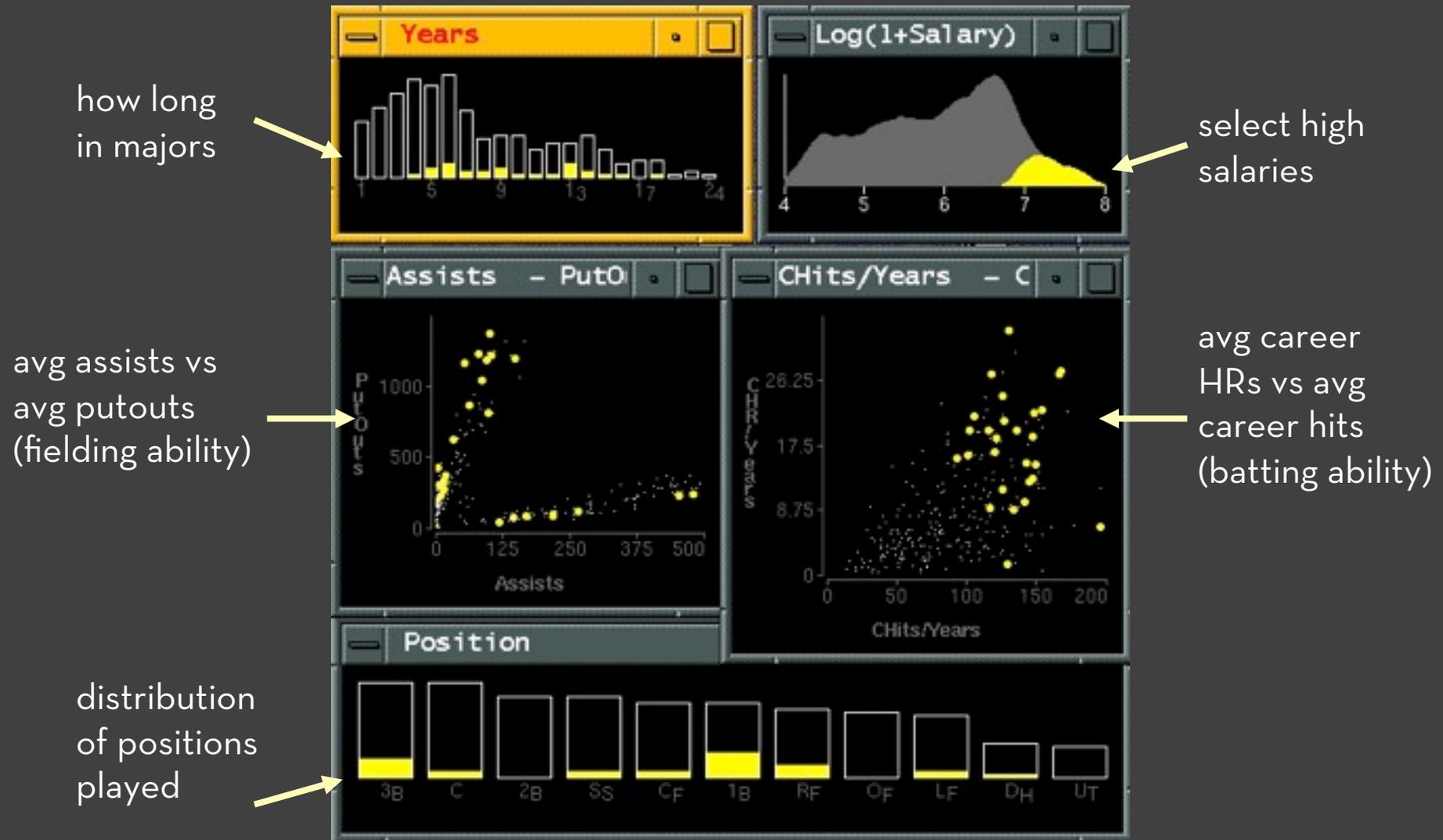
# Scatterplot Matrix (SPLOM)



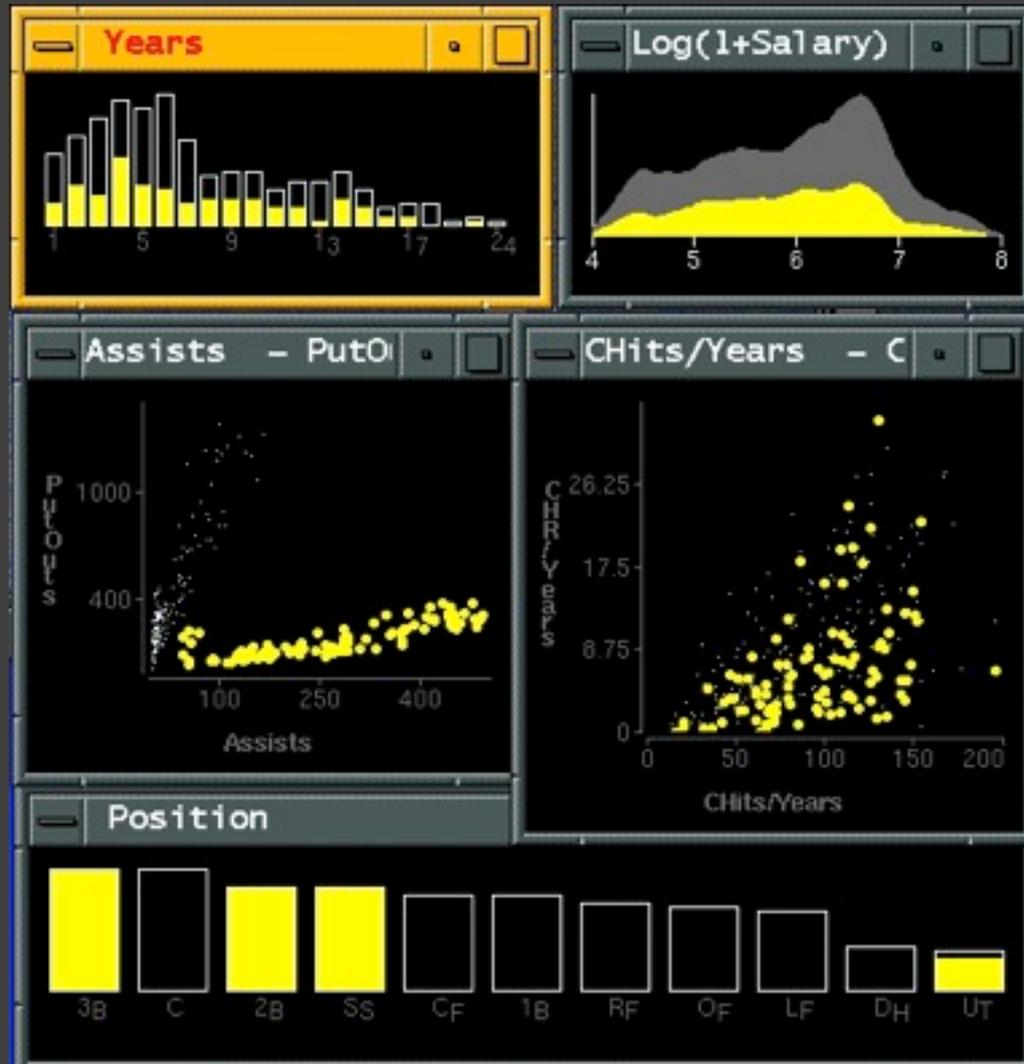
Scatter plots enabling pair-wise comparison of each data dimension.



# Multiple Coordinated Views



# Linking Assists to Positions



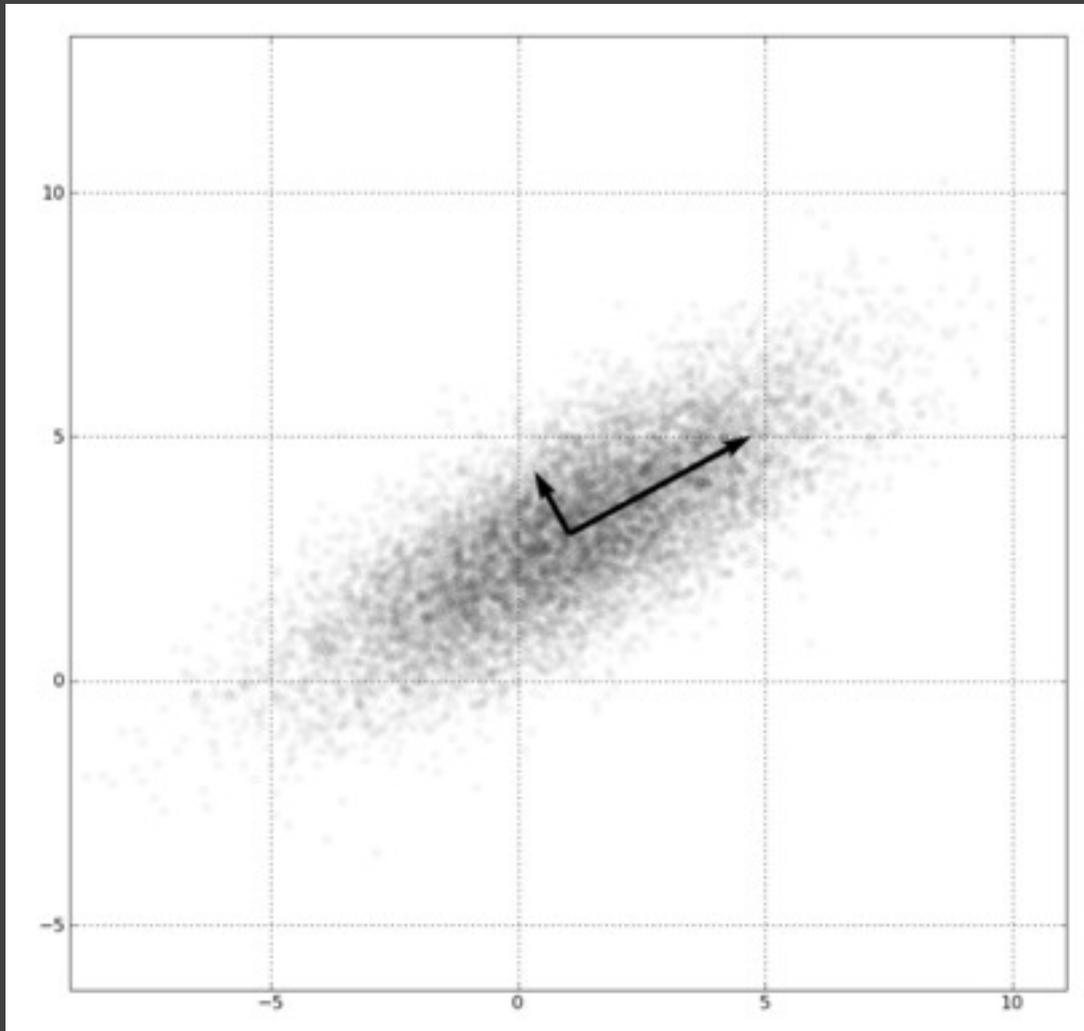
# Dimensionality Reduction



1:0.099,0.367(243.00)  
2:-0.157,0.106(47.74)  
3:-0.251,-0.178(9.00)  
4:-0.442,0.723(1.00)  
5:0.016,0.222(1.00)  
6:0.726,0.461(3.00)  
7:0.424,-0.195(1.00)

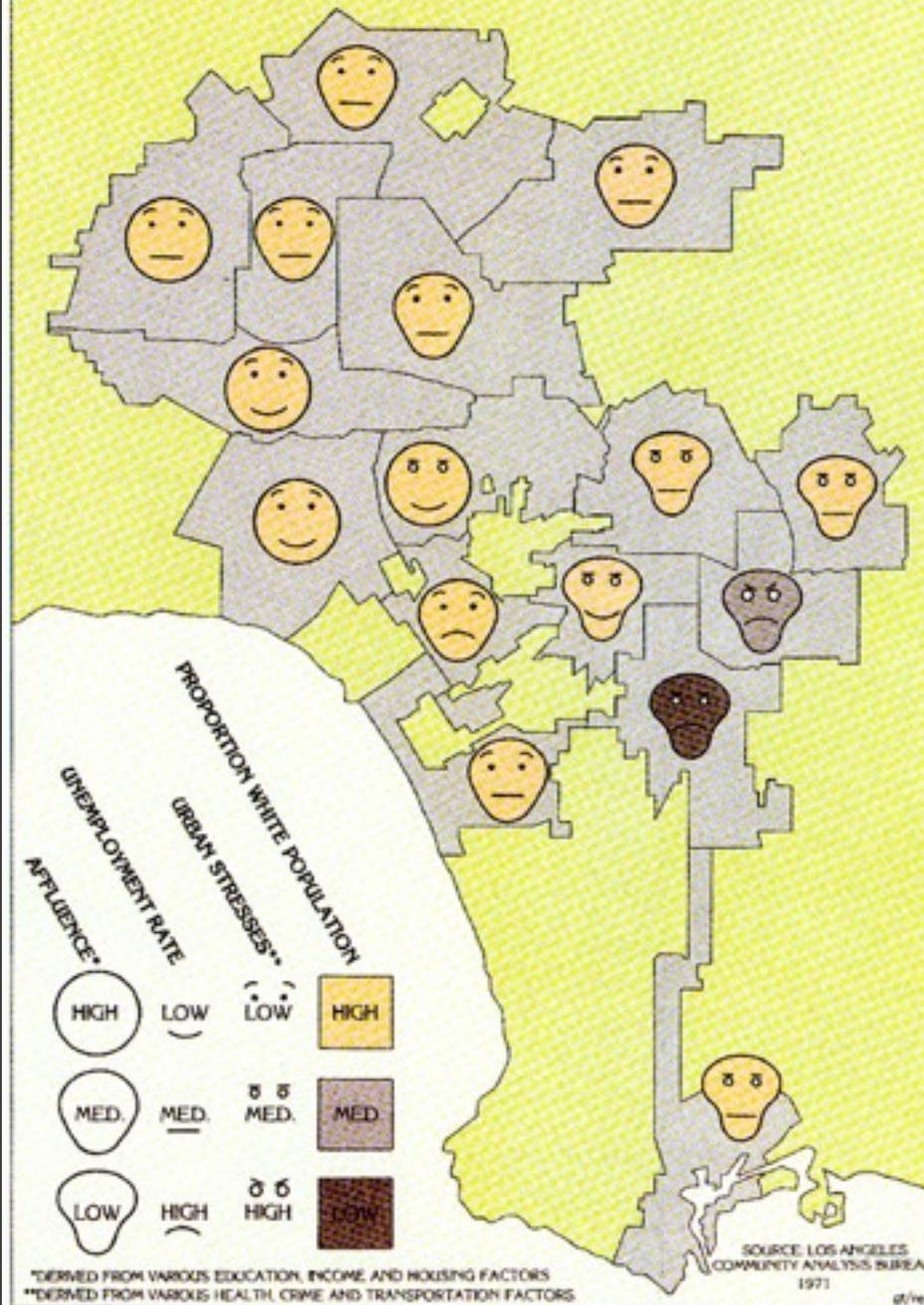
<http://www.ggobi.org/>

# Principal Component Analysis



1. Mean-center the data.
2. Find  $\perp$  basis vectors that maximize the data variance.
3. Plot the data using the top vectors.

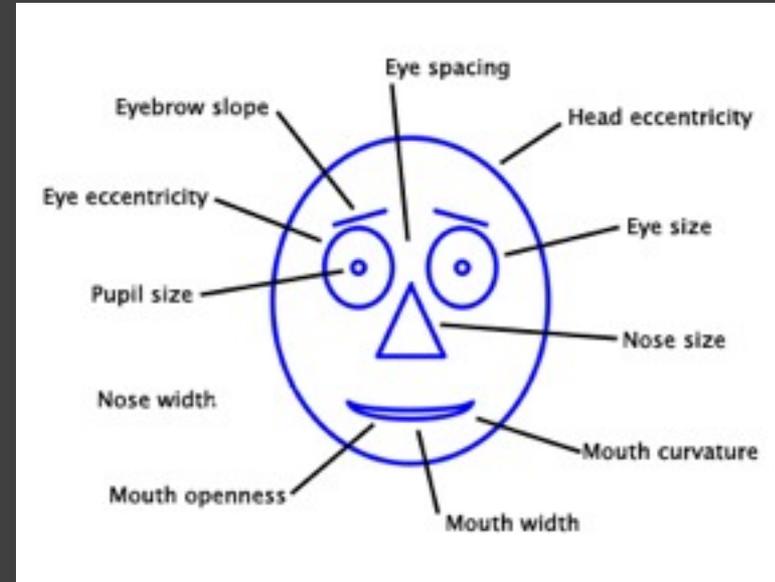
# Life in Los Angeles



# Chernoff Faces (1973)

Observation: We have evolved a sophisticated ability to interpret faces.

Idea: Map data variables to facial features.



Question: Do we process facial features in an uncorrelated way? (i.e., are they *separable*?)

This is just one example of nD “glyphs”

# Visualizing Multiple Dimensions

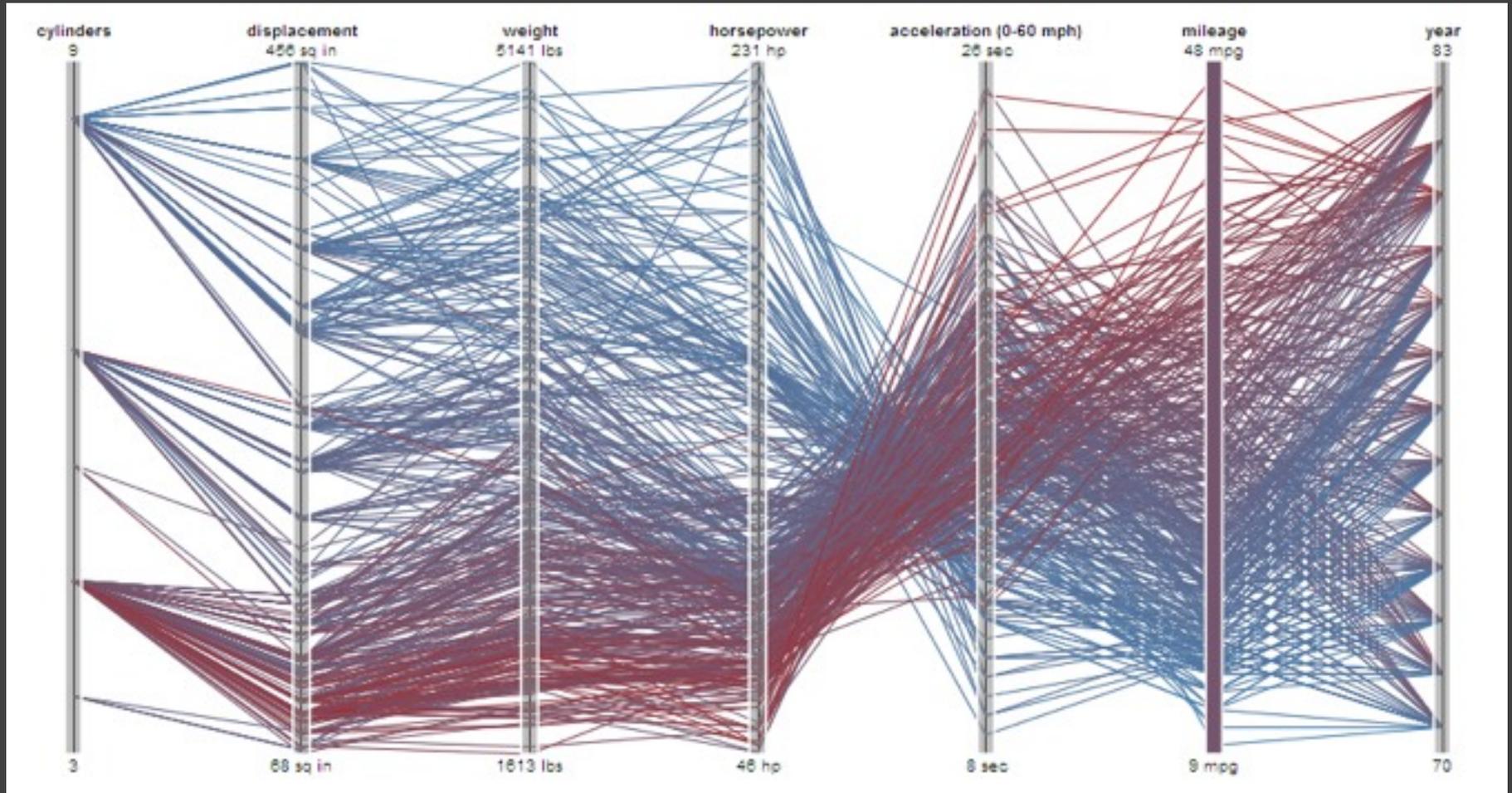
## Strategies

- Avoid “over-encoding”
- Use space and small multiples intelligently
- Reduce the problem space
- Use interaction to generate *relevant* views

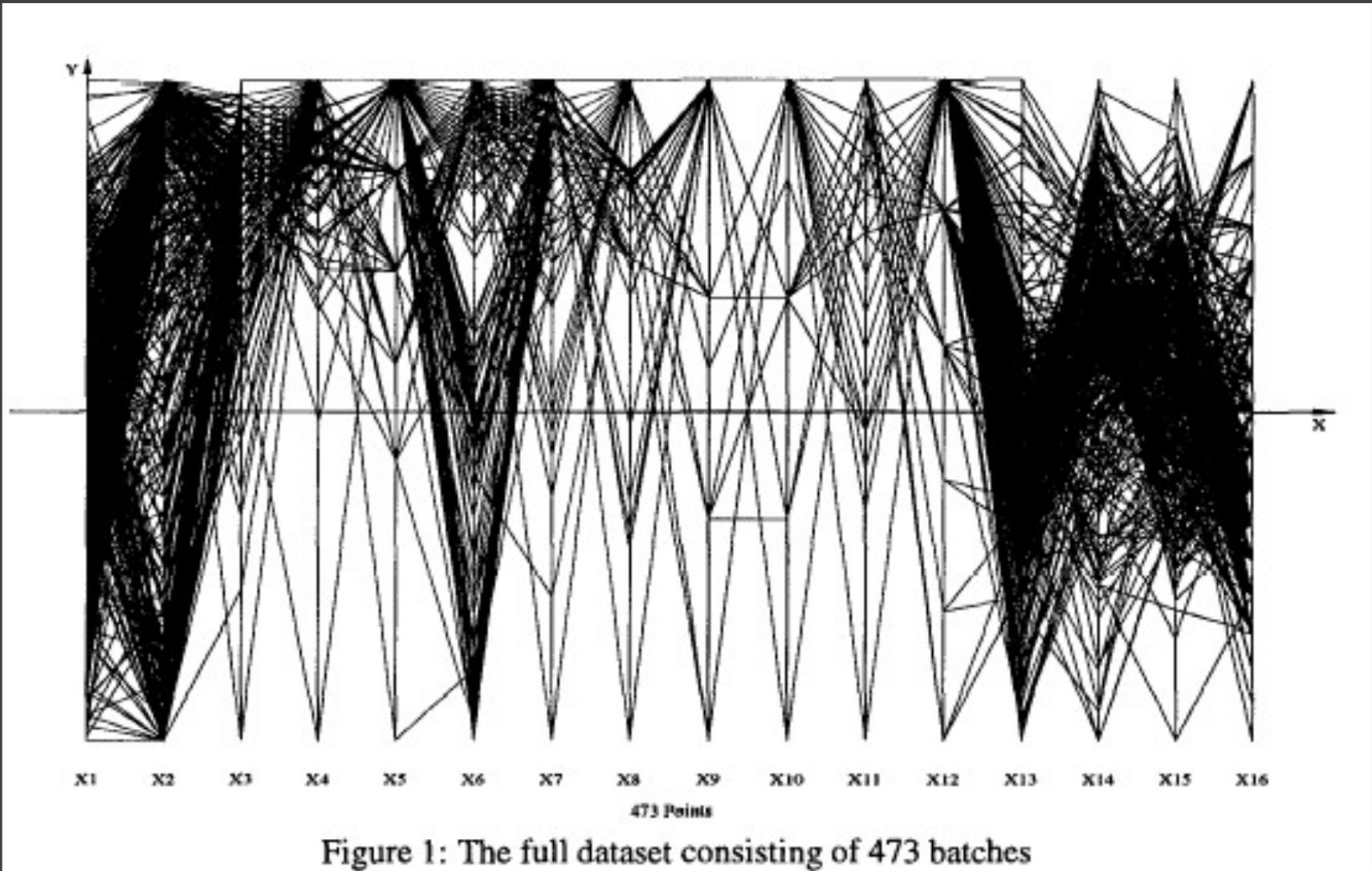
There is rarely a single visualization that answers all questions. Instead, the ability to generate appropriate visualizations quickly is key.

# Parallel Coordinates

# Parallel Coordinates [Inselberg]



# Parallel Coordinates [Inselberg]



# The Multidimensional Detective

The Dataset:

- Production data for 473 batches of a VLSI chip
- 16 process parameters:

$X_1$ : The yield: % of produced chips that are useful

$X_2$ : The quality of the produced chips (speed)

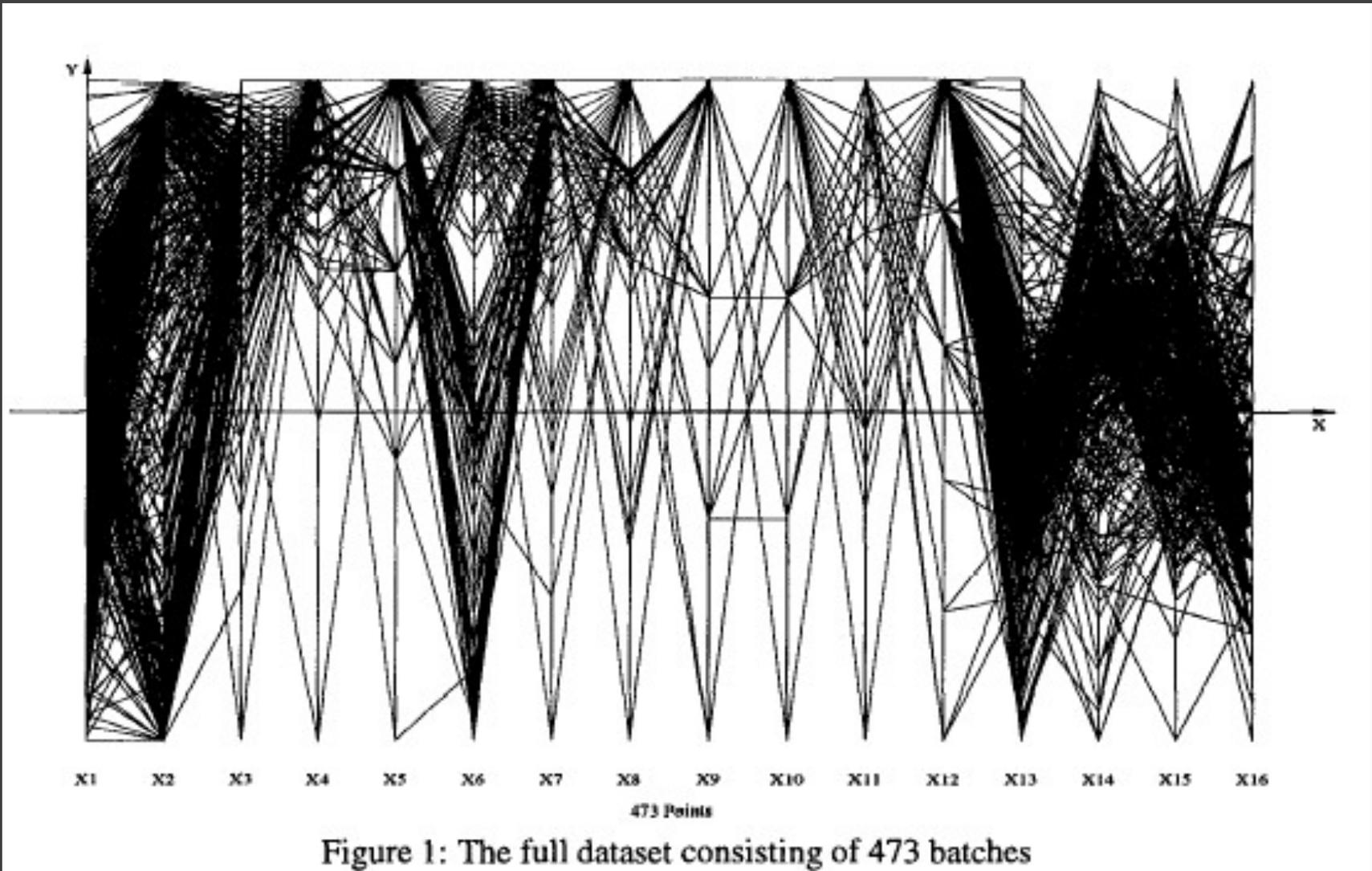
$X_3 \dots X_{12}$ : 10 types of defects (zero defects shown at top)

$X_{13} \dots X_{16}$ : 4 physical parameters

The Objective:

Raise the yield ( $X_1$ ) and maintain high quality ( $X_2$ )

# Parallel Coordinates



# Inselberg's Principles

1. Do not let the picture scare you
2. Understand your objectives
  - Use them to obtain visual cues
3. Carefully scrutinize the picture
4. Test your assumptions, especially the "I am really sure of's"
5. You can't be unlucky all the time!

Each line represents a tuple (e.g., VLSI batch)  
Filtered below for high values of  $X_1$  and  $X_2$

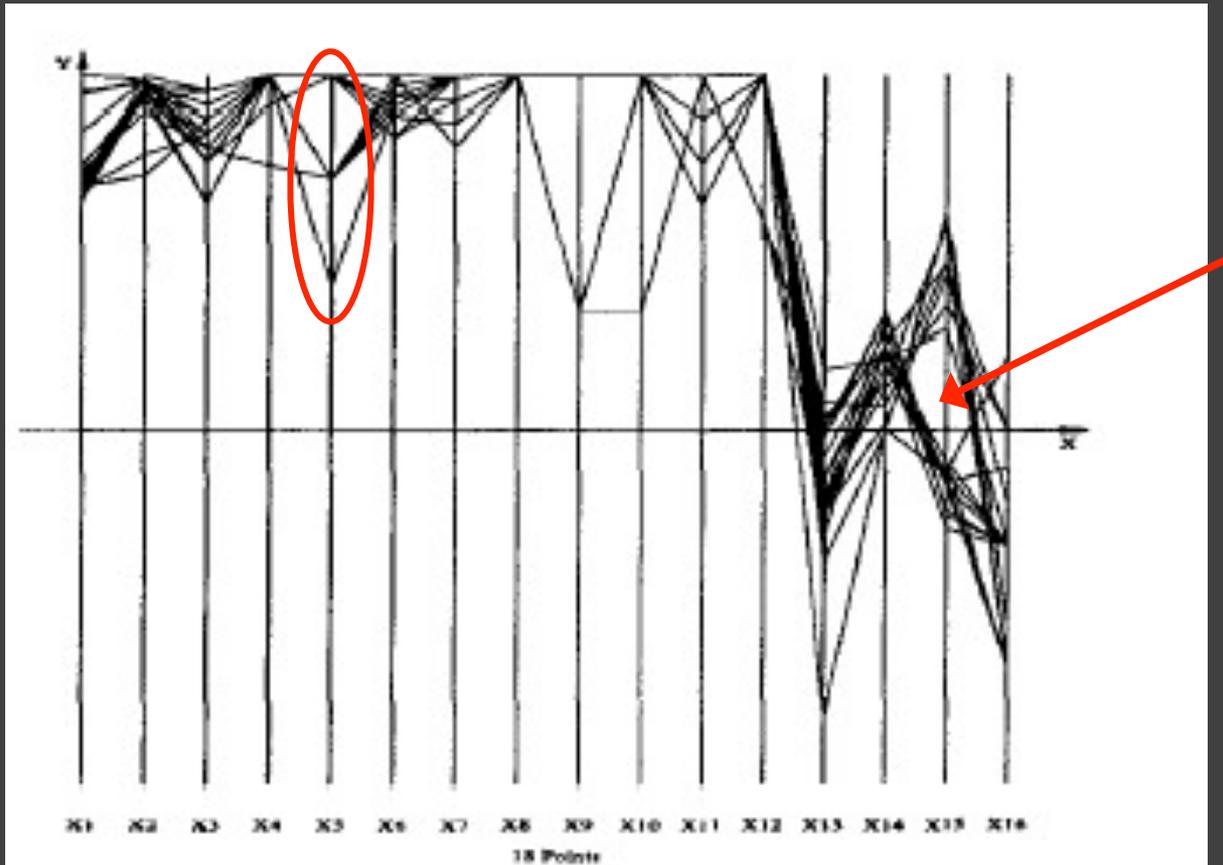


Figure 2: The batches high in Yield,  $X_1$ , and Quality,  $X_2$ .



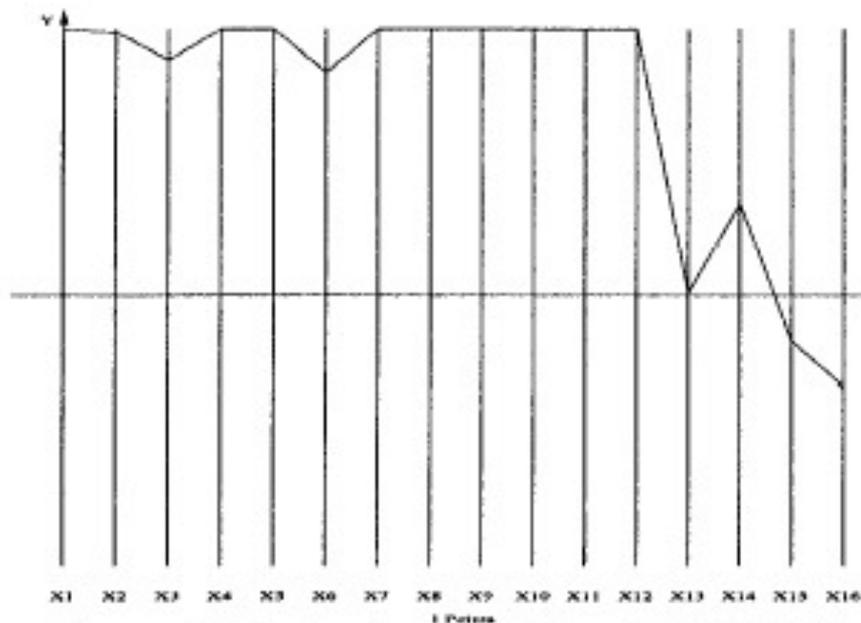


Figure 5: The best batch. Highest in Yield, X1, and very high in Quality, X2.

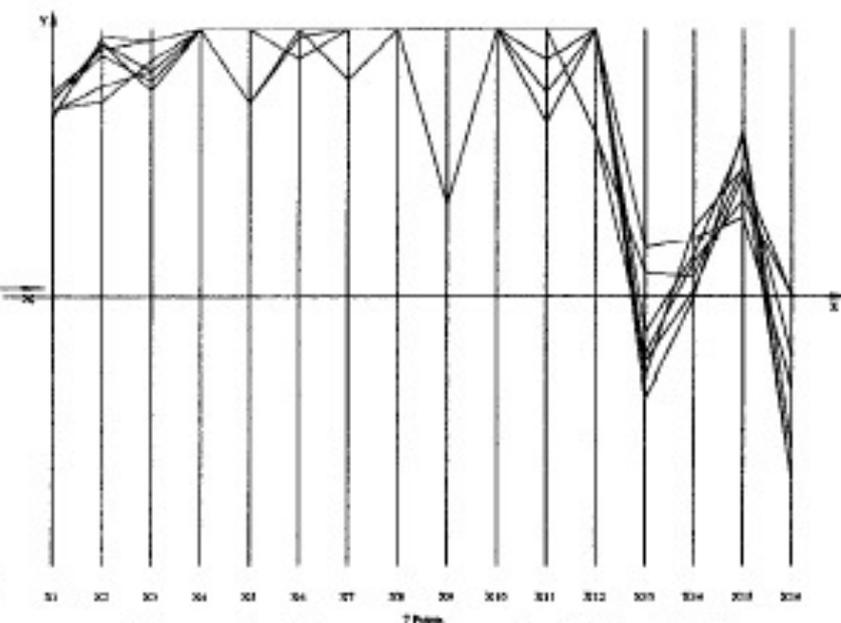
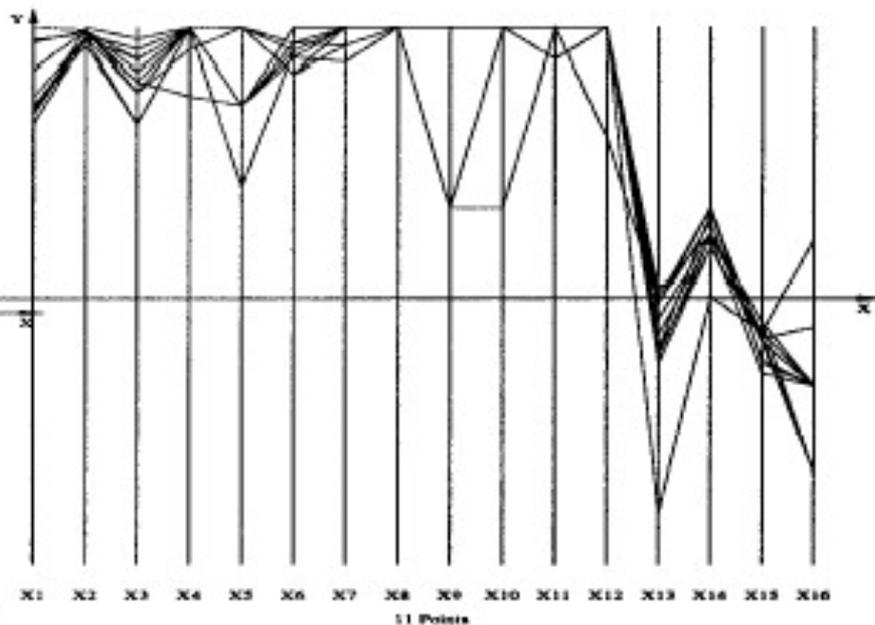
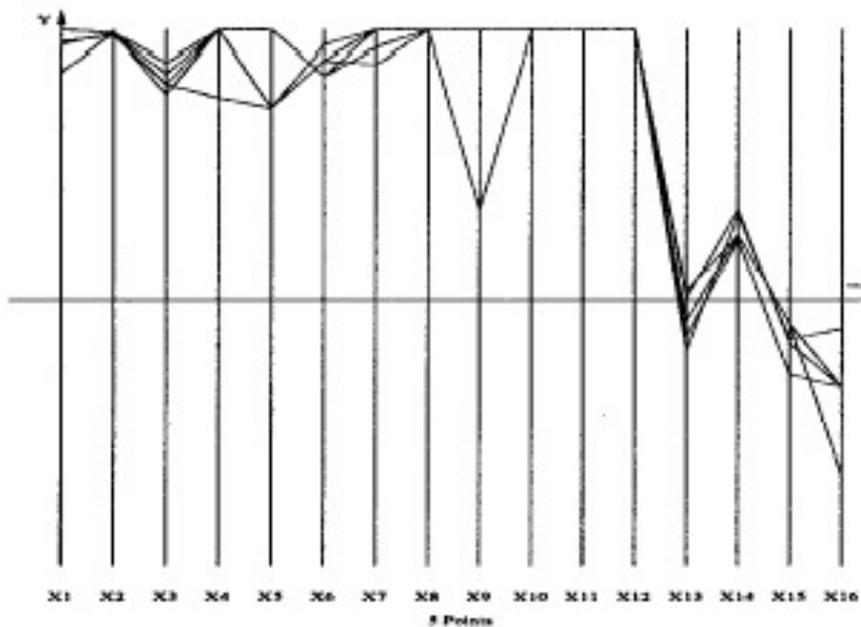
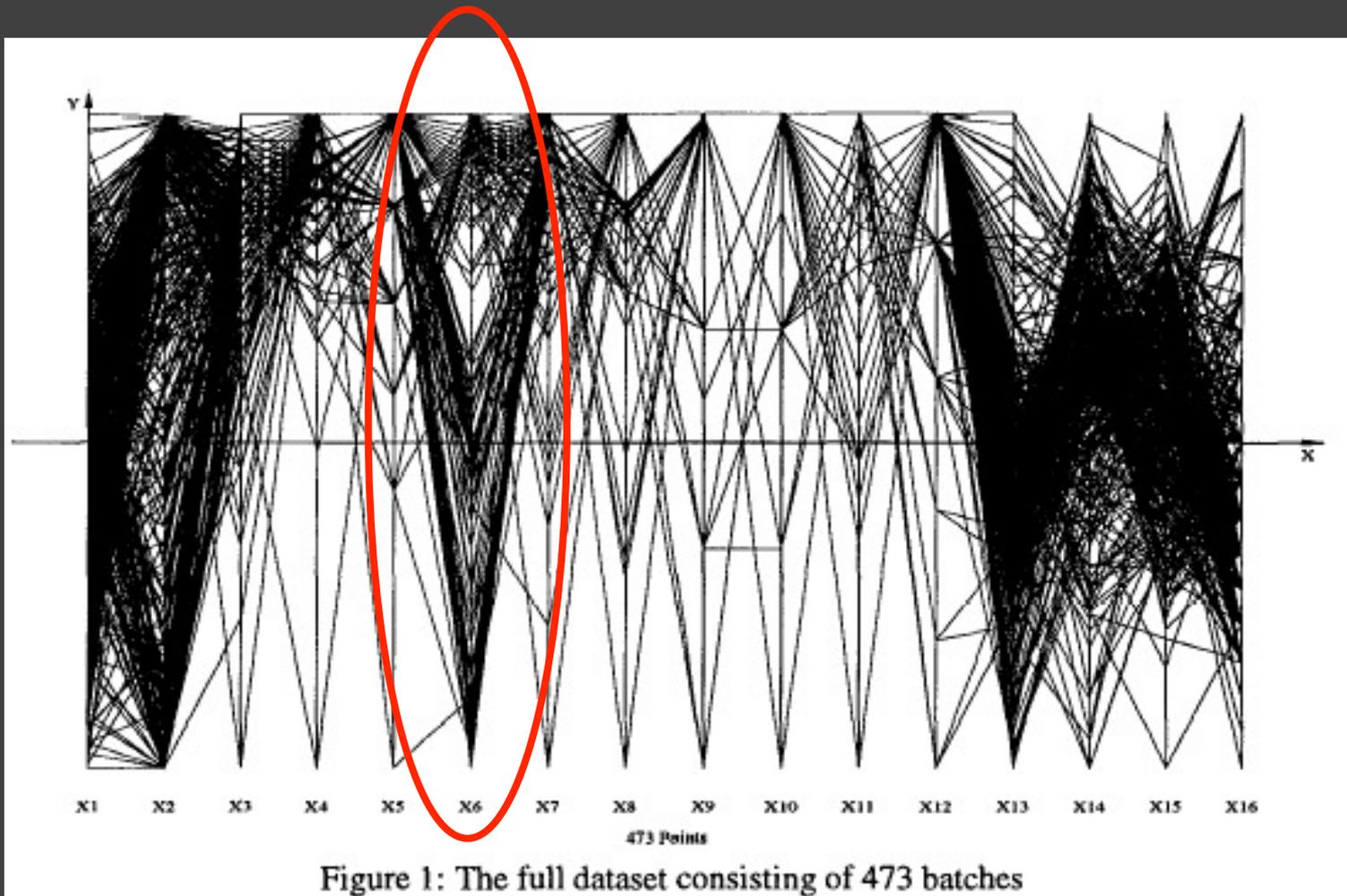


Figure 7: Upper range of split in X15



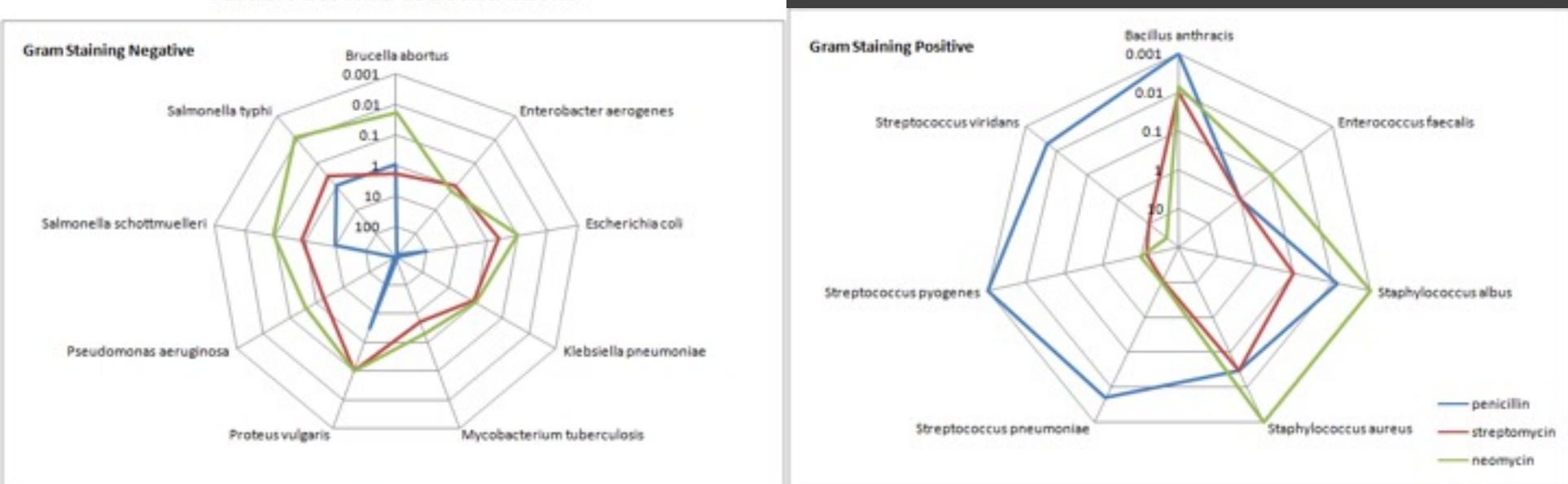
Notice that  $X_6$  behaves differently.

Allow 2 defects, including  $X_6$  -> best batches



# Radar Plot / Star Graph

Antibiotics MIC Concentrations

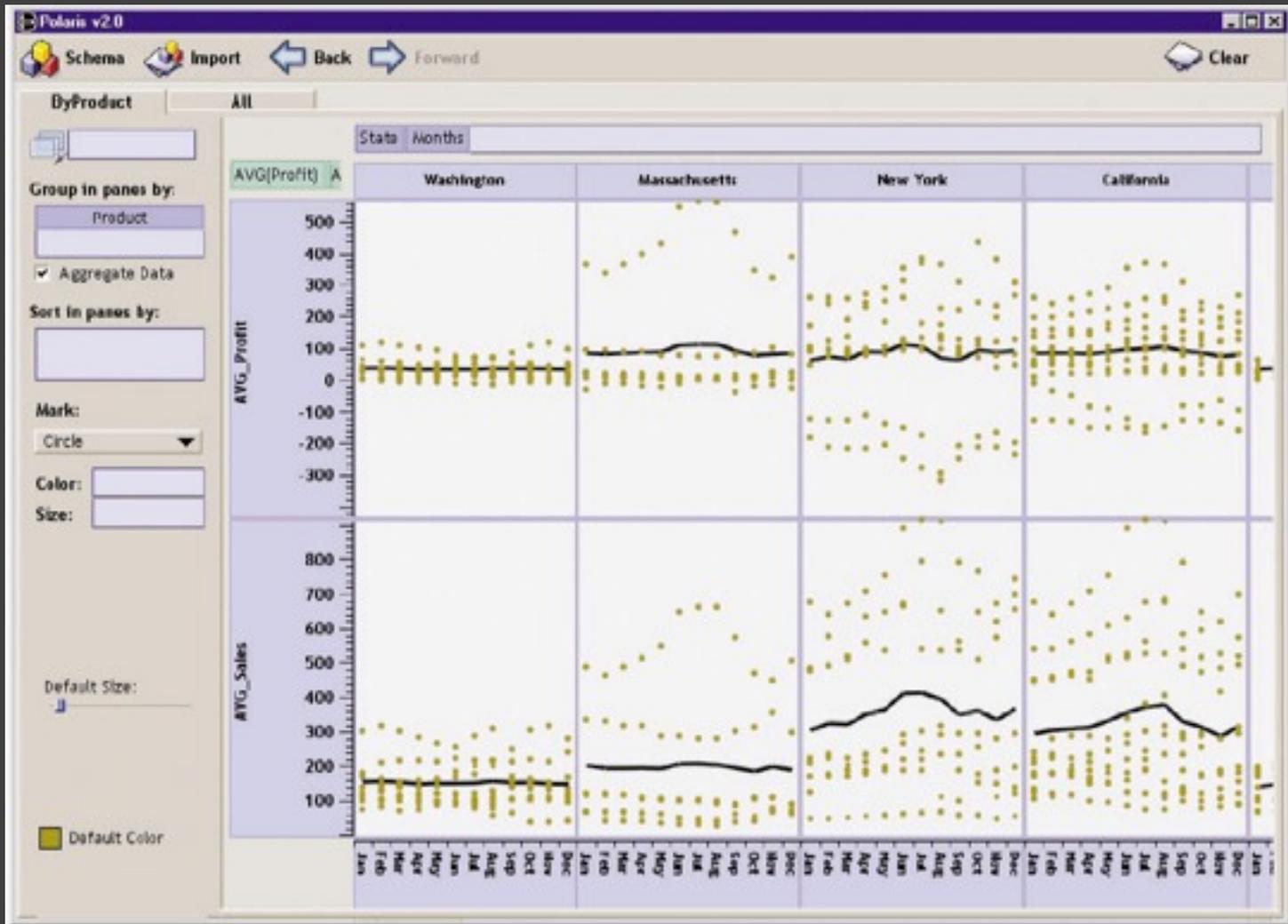


“Parallel” dimensions in polar coordinate space  
Best if same units apply to each axis

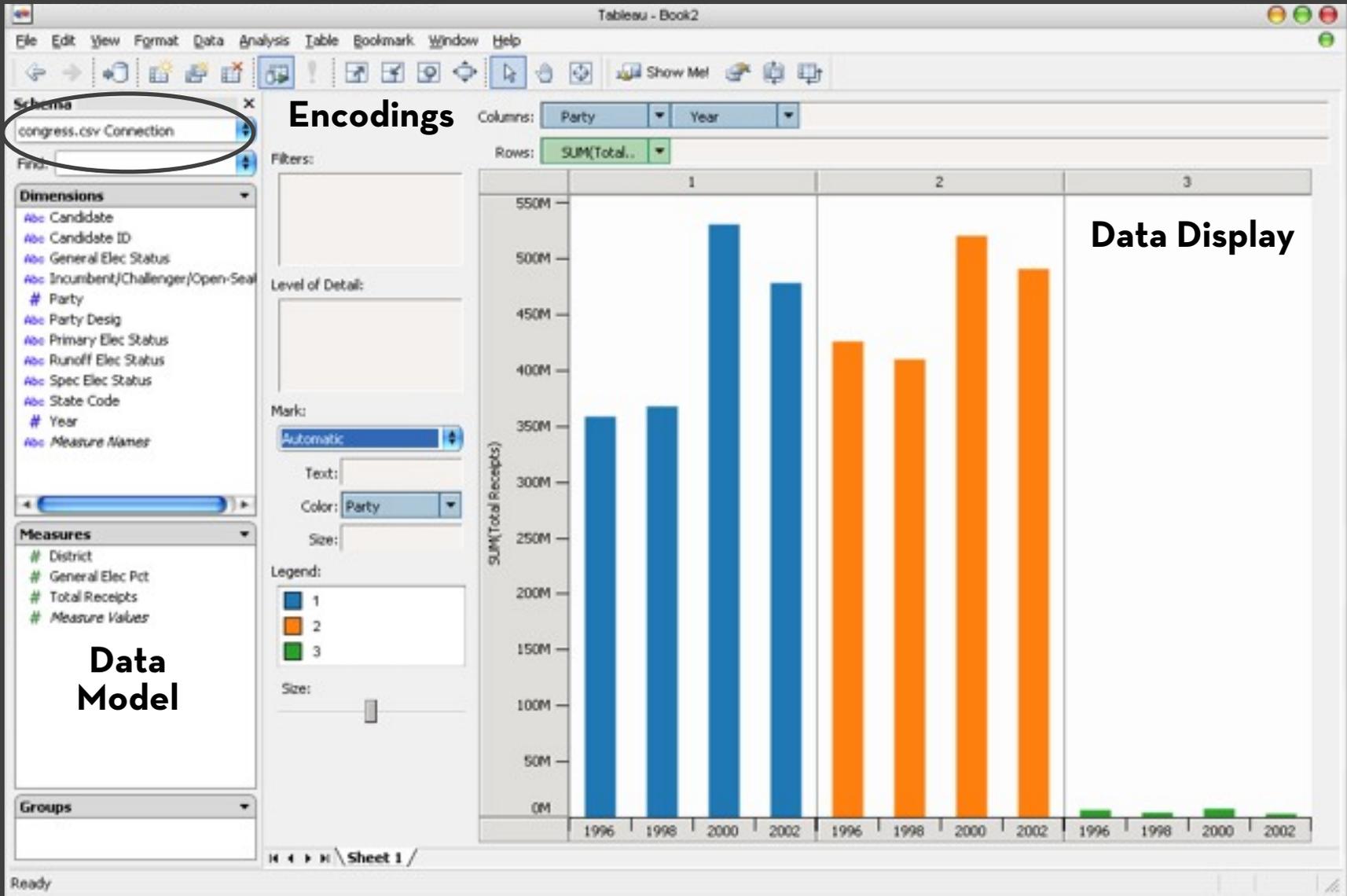
# Tableau / Polaris

# Polaris

Research at Stanford by Stolte, Tang, and Hanrahan.



# Tableau



# Tableau Demo

## The dataset:

Federal Elections Commission Receipts

Every Congressional Candidate from 1996 to 2002

4 Election Cycles

9216 Candidacies

# Data Set Schema

Year (Qi)

Candidate Code (N)

Candidate Name (N)

Incumbent / Challenger / Open-Seat (N)

Party Code (N) [1=Dem,2=Rep,3=Other]

Party Name (N)

Total Receipts (Qr)

State (N)

District (N)

This is a subset of the larger data set available from the FEC

# Hypotheses?

What might we learn from this data?

- ??

# Hypotheses?

What might we learn from this data?

Correlation between receipts and winners?

Do receipts increase over time?

Which states spend the most?

Which party spends the most?

Margin of victory vs. amount spent?

Amount spent between competitors?

# Tableau Demo

# Assignment 2: Exploratory Data Analysis

Use visualization software to form & answer questions.

First steps:

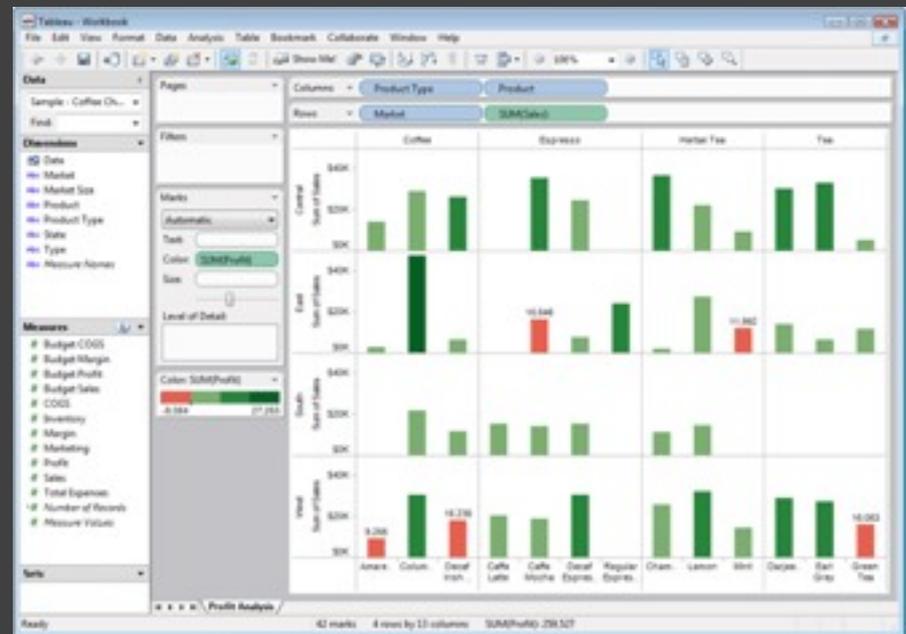
- Step 1: Pick domain & data
- Step 2: Pose questions
- Step 3: Profile the data
- Iterate as needed

Create visualizations

- Interact with data
- Refine your questions

Make wiki notebook

- Keep record of your analysis
- Prepare a final graphic and caption



Due by 5:00pm  
**Monday, Jan 27**

# Polaris/Tableau Approach

Insight: can simultaneously specify both database queries and visualization

Choose data, then visualization, not vice versa

Use smart defaults for visual encodings

More recently: automate visualization design

# Specifying Table Configurations

Operands are the database fields

- Each operand interpreted as a set {...}
- Quantitative and Ordinal fields treated differently

Three operators:

- **concatenation (+)**
- **cross product (x)**
- **nest (/)**

# Table Algebra: Operands

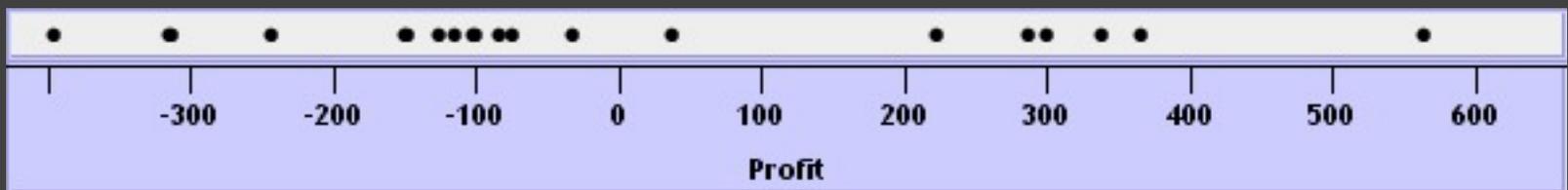
**Ordinal fields:** interpret domain as a set that partitions table into rows and columns.

Quarter = {(Qtr1),(Qtr2),(Qtr3),(Qtr4)} →

Qtr1	Qtr2	Qtr3	Qtr4
95892	101760	105282	98225

**Quantitative fields:** treat domain as single element set and encode spatially as axes:

Profit = {(Profit[-410,650])} →



# Concatenation (+) Operator

Ordered union of set interpretations

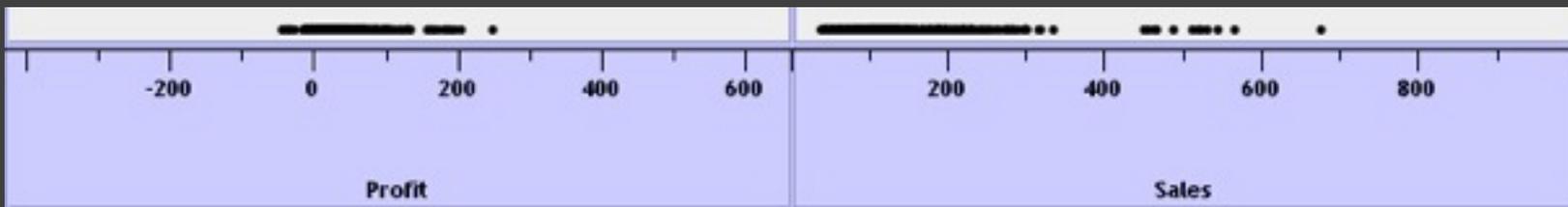
Quarter + Product Type

= {(Qtr1),(Qtr2),(Qtr3),(Qtr4)} + {(Coffee), (Espresso)}

= {(Qtr1),(Qtr2),(Qtr3),(Qtr4),(Coffee),(Espresso)}

Qtr1	Qtr2	Qtr3	Qtr4	Coffee	Espresso
48	59	57	53	151	21

Profit + Sales = {(Profit[-310,620]),(Sales[0,1000])}



# Cross (x) Operator

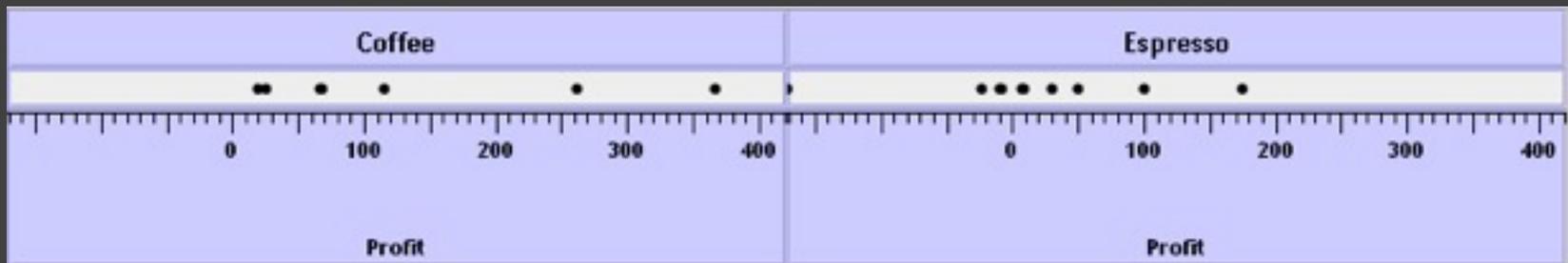
Cross-product of set interpretations

Quarter x Product Type

= {(Qtr1,Coffee), (Qtr1, Tea), (Qtr2, Coffee), (Qtr2, Tea), (Qtr3, Coffee), (Qtr3, Tea), (Qtr4, Coffee), (Qtr4,Tea)}

Qtr1		Qtr2		Qtr3		Qtr4	
Coffee	Espresso	Coffee	Espresso	Coffee	Espresso	Coffee	Espresso
131	19	160	20	178	12	134	33

Product Type x Profit =



# Nest (/) Operator

Cross-product filtered by existing records

Quarter x Month

creates twelve entries for each quarter. i.e.,  
(Qtr1, December)

Quarter / Month

creates three entries per quarter based on  
tuples in database (not semantics)

# Table Algebra

The operators (+, x, /) and operands (O, Q) provide an *algebra* for tabular visualization.

Algebraic statements are then mapped to:

**Visualizations** - trellis plot partitions, visual encodings

**Queries** - selection, projection, group-by aggregation

In Tableau, users make statements via drag-and-drop

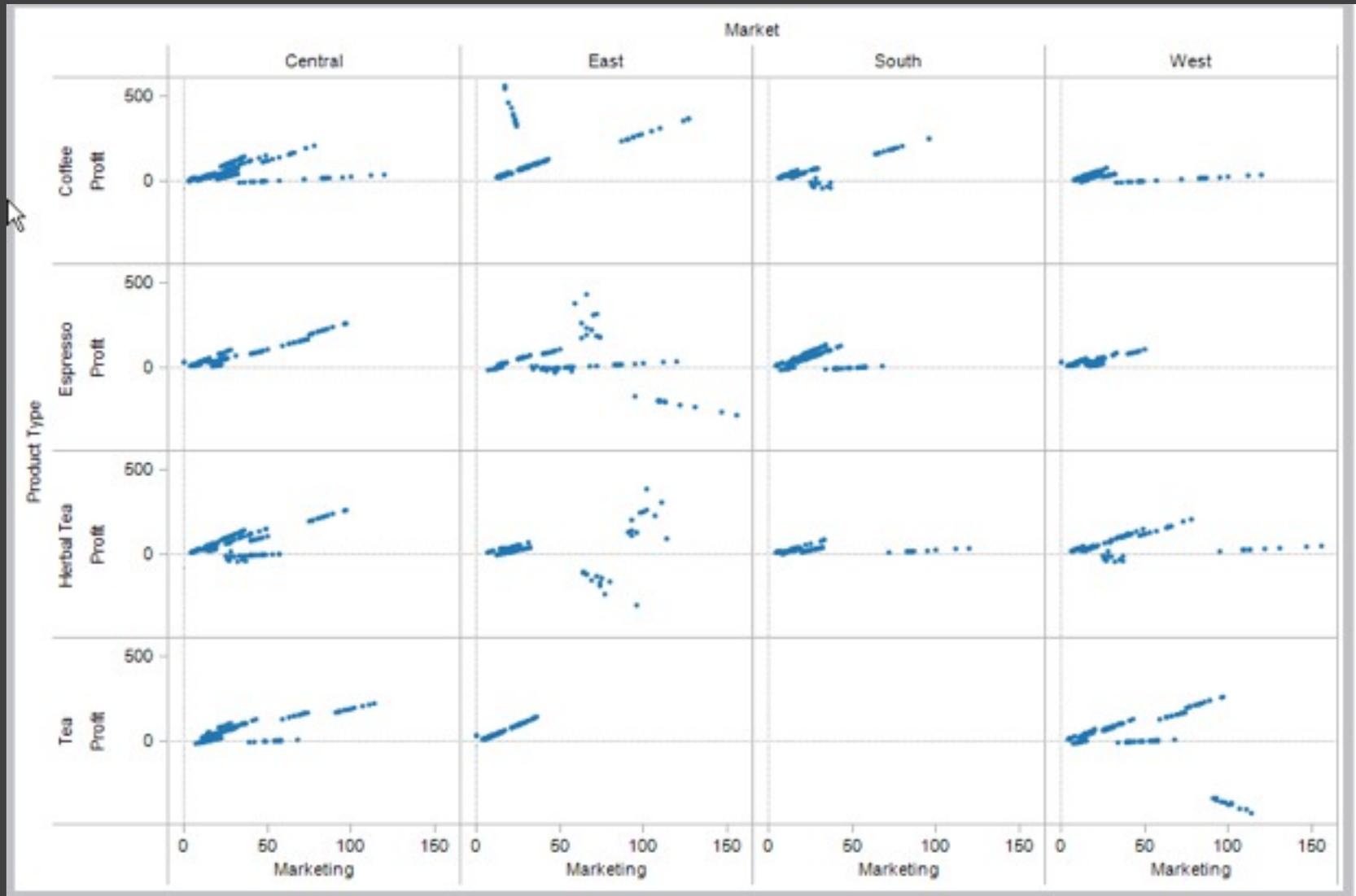
Note that this specifies operands NOT operators!

Operators are inferred by data type (O, Q)

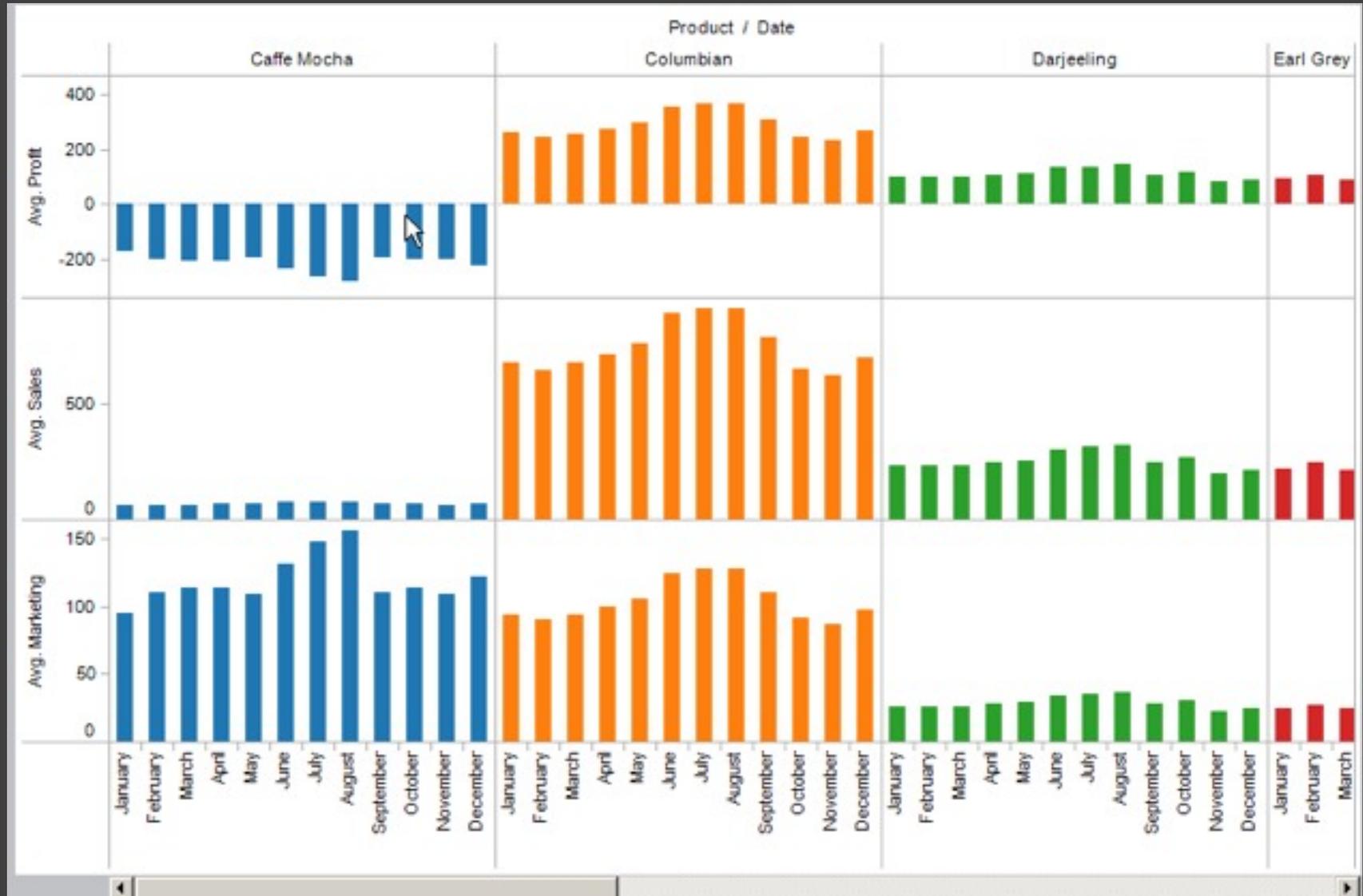
# Ordinal - Ordinal

State	Product Type			
	Coffee	Espresso	Herbal Tea	Tea
Colorado	●	●	●	●
Connecticut	●	●	●	●
Florida	●	●	●	●
Illinois	●	●	●	●
Iowa	●	●	●	●
Louisiana	●	●	●	●
Massachusetts	●	●	●	●
Missouri	●	●	●	●
Nevada	●	●	●	●
New Hampshire	●	●	●	●
New Mexico	●	●	●	●
New York	●	●	●	●
Ohio	●	●	●	●
Oklahoma	●	●	●	●
Oregon	●	●	●	●
Texas	●	●	●	●
Utah	●	●	●	●
Washington	●	●	●	●
Wisconsin	●	●	●	●

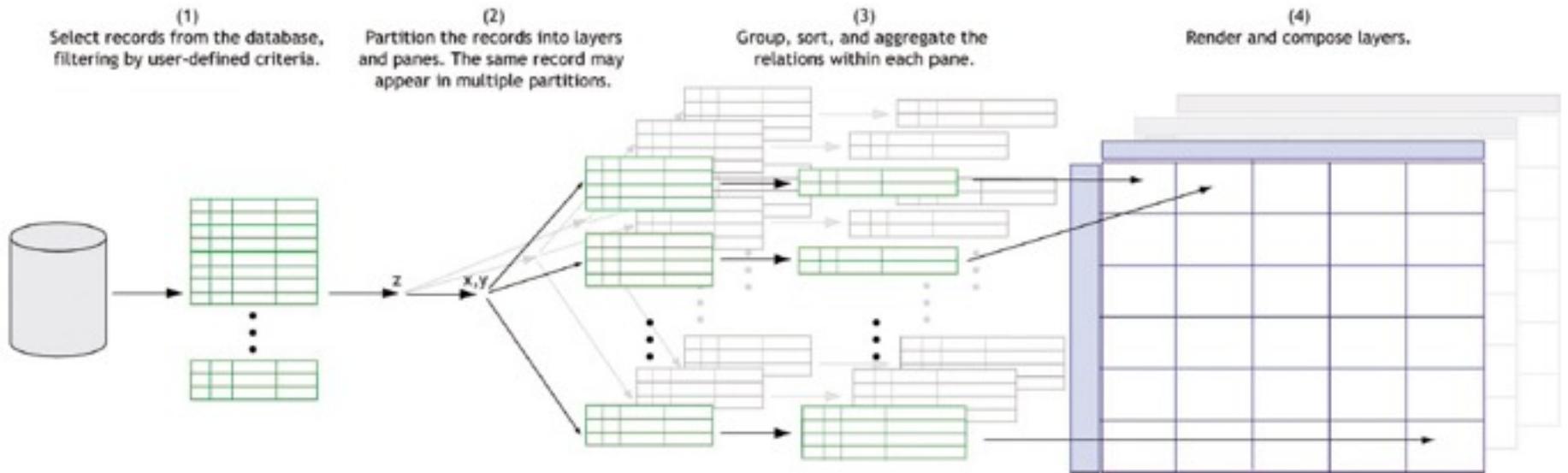
# Quantitative - Quantitative



# Ordinal - Quantitative



# Querying the Database



# Visualizing Multiple Dimensions

## Strategies

- Start by visualizing individual dimensions
- Avoid “over-encoding”
- Use space and small multiples intelligently
- Use interaction to generate *relevant* views

There is rarely a single visualization that answers all questions. Instead, the ability to generate appropriate visualizations quickly is key.