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<pre> Require Import List. Require Import String. Require Import ZArith. Open Scope list_scope. Open Scope string_scope. Open Scope Z_scope. Require Import StructTactics. Require Import ImpSyntax. Require Import ImpCommon. Require Import ImpEval. Require Import ImpStep. (** eval facts *) Lemma eval_unop_det : forall op v v1 v2, eval_unop op v v1 -> eval_unop op v v2 -> v1 = v2. Proof. intros. repeat on (eval_unop _ _ _), invc; auto. Qed. Lemma eval_binop_det : forall op vL vR v1 v2, eval_binop op vL vR v1 -> eval_binop op vL vR v2 -> v1 = v2. Proof. intros. repeat on (eval_binop _ _ _ _), invc; auto. Qed. Lemma eval_e_det : forall s h e v1 v2, eval_e s h e v1 -> eval_e s h e v2 -> v1 = v2. Proof. intros. prep_induction H. induction H; intros; on (eval_e _ _ _ _), invc; repeat find_apply_hyp_hyp; subst; try congruence. - find_eapply_lem_hyp eval_unop_det; eauto. - find_eapply_lem_hyp eval_binop_det; eauto. Qed. Lemma eval_e_len_a_inv : forall s h e x a l, eval_e s h (Elen e) x -> eval_e s h e (Vaddr a) -> read h a = Some (Vint l) -> x = Vint l. Proof. intros. invc H. - eapply eval_e_det in H0; eauto. congruence. - eapply eval_e_det in H0; eauto. congruence. Qed. Lemma eval_e_idx_a_inv : forall s h e1 e2 x a i l, eval_e s h (Eidx e1 e2) x -> eval_e s h e1 (Vaddr a) -> eval_e s h e2 (Vint i) -> </pre>		

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<pre> read h a = Some (Vint l) -> read h (Z.succ (a + i)) = Some x. Proof. intros. invc H. - eapply eval_e_det in H0; eauto. eapply eval_e_det in H1; eauto. congruence. - eapply eval_e_det in H0; eauto. congruence. Qed. (** step facts *) Lemma nostep_nop : forall s h s' h' p', ~ step s h Snop s' h' p'. Proof. unfold not; intros. inv H. Qed. Lemma nostep_self' : forall s1 h1 p1 s2 h2 p2, step s1 h1 p1 s2 h2 p2 -> p1 <> p2. Proof. induction 1; try congruence. - induction p1; congruence. - induction p2; congruence. - induction p2; congruence. Qed. Lemma nostep_self : forall s1 h1 p1 s2 h2, ~ step s1 h1 p1 s2 h2 p1. Proof. unfold not; intros. find_apply_lem_hyp nostep_self'. congruence. Qed. Lemma step_star_l : forall s1 h1 p1 s2 h2 p2, step s1 h1 p1 s2 h2 p2 -> step_star s1 h1 p1 s2 h2 p2. Proof. repeat ee. Qed. Lemma step_star_r : forall s1 h1 p1 s2 h2 p2 s3 h3 p3, step_star s1 h1 p1 s2 h2 p2 -> step s2 h2 p2 s3 h3 p3 -> step_star s1 h1 p1 </pre>		

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s3 h3 p3.
Proof.
  induction 1; repeat ee.
Qed.

Lemma step_star_app :
  forall s1 h1 p1 s2 h2 p2 s3 h3 p3,
  step_star
    s1 h1 p1
    s2 h2 p2 ->
  step_star
    s2 h2 p2
    s3 h3 p3 ->
  step_star
    s1 h1 p1
    s3 h3 p3.
Proof.
  intros. prep_induction H.
  induction H; intros.
  - assumption.
  - ee.
Qed.

Lemma step_star_seq :
  forall s1 h1 p1 s2 h2 p2 pB,
  step_star
    s1 h1 p1
    s2 h2 p2 ->
  step_star
    s1 h1 (Sseq p1 pB)
    s2 h2 (Sseq p2 pB).
Proof.
  intros. prep_induction H.
  induction H; repeat ee.
Qed.

Lemma eval_step_star :
  forall s h p s' h',
  eval_s
    s h p
    s' h' ->
  step_star
    s h p
    s' h' Snop.
Proof.
  induction 1;
  try (do 2 ee; fail).
  - eapply step_star_l; [ee|].
    eapply step_star_app.
    + eapply step_star_seq; eauto.
    + eapply step_star_l; [ee|].
      assumption.
  - eapply step_star_app.
    + eapply step_star_seq; eauto.
    + eapply step_star_l; [ee|].
      assumption.
Qed.

Ltac invc_eval_s :=
  on (eval_s _ _ _ _ _), invc.

Lemma step_eval_eval :
  forall s1 h1 p1 s2 h2 p2 s3 h3,
  step
    s1 h1 p1
    s2 h2 p2 ->
  eval_s
    s2 h2 p2
    s3 h3 ->

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  eval_s
    s1 h1 p1
    s3 h3.
Proof.
  intros. prep_induction H.
  induction H; intros.
  - invc_eval_s; repeat ee.
  - invc_eval_s; repeat ee.
  - invc_eval_s; repeat ee.
  - eauto using eval_ifelse_t.
  - eauto using eval_ifelse_f.
  - invc_eval_s; repeat ee.
  - invc_eval_s.
    eauto using eval_while_f.
  - repeat ee.
  - invc_eval_s; repeat ee.
Qed.

Lemma step_star_eval :
  forall s1 h1 p1 s2 h2,
  step_star
    s1 h1 p1
    s2 h2 Snop ->
  eval_s
    s1 h1 p1
    s2 h2.
Proof.
  intros. prep_induction H.
  induction H; intros; subst.
  - ee.
  - eauto using step_eval_eval.
Qed.

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