Name: $\qquad$

## CSE 505, Fall 2008, Final Examination 11 December 2008

## Please do not turn the page until everyone is ready.

Rules:

- The exam is closed-book, closed-note, except for one side of one $8.5 \times 11$ in piece of paper.
- Please stop promptly at 10:20.
- You can rip apart the pages.
- There are 100 points total, distributed among 6 questions.
- The questions have multiple parts.

Advice:

- Read questions carefully. Understand a question before you start writing.
- Write down thoughts and intermediate steps so you can get partial credit.
- The questions are not necessarily in order of difficulty. Skip around. In particular, make sure you get to all the problems.
- If you have questions, ask.
- Relax. You are here to learn.

Name: $\qquad$
For your reference (page 1 of 2 ):

$$
\begin{aligned}
e & ::=\lambda x . e|x| e e|c|\left\{l_{1}=e_{1}, \ldots, l_{n}=e_{n}\right\}\left|e . l_{i}\right| \text { fix } e \\
v & ::=\lambda x . e|c|\left\{l_{1}=v_{1}, \ldots, l_{n}=v_{n}\right\} \\
\tau & ::=\text { int }|\tau \rightarrow \tau|\left\{l_{1}: \tau_{1}, \ldots, l_{n}: \tau_{n}\right\}
\end{aligned}
$$

$e \rightarrow e^{\prime}$ and $\Gamma \vdash e: \tau$ and $\tau_{1} \leq \tau_{2}$
$\overline{(\lambda x . e) v \rightarrow e[v / x]} \quad \frac{e_{1} \rightarrow e_{1}^{\prime}}{e_{1} e_{2} \rightarrow e_{1}^{\prime} e_{2}} \quad \frac{e_{2} \rightarrow e_{2}^{\prime}}{v e_{2} \rightarrow v e_{2}^{\prime}} \quad \frac{e \rightarrow e^{\prime}}{\text { fix } e \rightarrow \text { fix } e^{\prime}} \quad \overline{\text { fix } \lambda x . e \rightarrow e[\mathrm{fix} \lambda x . e / x]}$

$$
\overline{\left\{l_{1}=v_{1}, \ldots, l_{n}=v_{n}\right\} \cdot l_{i} \rightarrow v_{i}}
$$

$$
\begin{gathered}
e_{i} \rightarrow e_{i}^{\prime} \\
\left\{l_{1}=v_{1}, \ldots, l_{i-1}=v_{i-1}, l_{i}=e_{i}, \ldots, l_{n}=e_{n}\right\} \rightarrow\left\{l_{1}=v_{1}, \ldots, l_{i-1}=v_{i-1}, l_{i}=e_{i}^{\prime}, \ldots, l_{n}=e_{n}\right\}
\end{gathered}
$$

$$
\overline{\Gamma \vdash c: \text { int }} \quad \overline{\Gamma \vdash x: \Gamma(x)} \quad \frac{\Gamma, x: \tau_{1} \vdash e: \tau_{2}}{\Gamma \vdash \lambda x . e: \tau_{1} \rightarrow \tau_{2}} \quad \frac{\Gamma \vdash e_{1}: \tau_{2} \rightarrow \tau_{1} \quad \Gamma \vdash e_{2}: \tau_{2}}{\Gamma \vdash e_{1} e_{2}: \tau_{1}} \quad \frac{\Gamma \vdash e: \tau \rightarrow \tau}{\Gamma \vdash \mathrm{fix} e: \tau}
$$

$$
\frac{\Gamma \vdash e: \tau \quad \tau \leq \tau^{\prime}}{\Gamma \vdash e: \tau^{\prime}}
$$

$$
\overline{\left\{l_{1}: \tau_{1}, \ldots, l_{n}: \tau_{n}, l: \tau\right\} \leq\left\{l_{1}: \tau_{1}, \ldots, l_{n}: \tau_{n}\right\}}
$$

$$
\overline{\left\{l_{1}: \tau_{1}, \ldots, l_{i-1}: \tau_{i-1}, l_{i}: \tau_{i}, \ldots, l_{n}: \tau_{n}\right\} \leq\left\{l_{1}: \tau_{1}, \ldots, l_{i}: \tau_{i}, l_{i-1}: \tau_{i-1}, \ldots, l_{n}: \tau_{n}\right\}}
$$

$$
\frac{\tau_{i} \leq \tau_{i}^{\prime}}{\left\{l_{1}: \tau_{1}, \ldots, l_{i}: \tau_{i}, \ldots, l_{n}: \tau_{n}\right\} \leq\left\{l_{1}: \tau_{1}, \ldots, l_{i}: \tau_{i}^{\prime}, \ldots, l_{n}: \tau_{n}\right\}}
$$

$$
\frac{\tau_{3} \leq \tau_{1} \quad \tau_{2} \leq \tau_{4}}{\tau_{1} \rightarrow \tau_{2} \leq \tau_{3} \rightarrow \tau_{4}} \quad \overline{\tau \leq \tau} \quad \frac{\tau_{1} \leq \tau_{2} \quad \tau_{2} \leq \tau_{3}}{\tau_{1} \leq \tau_{3}}
$$

| $e$ | $::=c\|x\| \lambda x: \tau . e\|e e\| \Lambda \alpha . e \mid e[\tau]$ | $\Gamma$ | $::=\cdot \mid \Gamma, x: \tau$ |
| :--- | :--- | :--- | :--- |
| $\tau$ | $::=$ int $\|\tau \rightarrow \tau\| \alpha \mid \forall \alpha . \tau$ | $\Delta$ | $::=\cdot \mid \Delta, \alpha$ |
| $v$ | $::=c\|\lambda x: \tau . e\| \Lambda \alpha . e$ |  |  |

$e \rightarrow e^{\prime}$ and $\Delta ; \Gamma \vdash e: \tau$

$$
\begin{aligned}
& \frac{e \rightarrow e^{\prime}}{e e_{2} \rightarrow e^{\prime} e_{2}} \quad \frac{e \rightarrow e^{\prime}}{v e \rightarrow v e^{\prime}} \quad \frac{e \rightarrow e^{\prime}}{e[\tau] \rightarrow e^{\prime}[\tau]} \quad \overline{(\lambda x: \tau . e) v \rightarrow e[v / x]} \quad \overline{(\Lambda \alpha . e)[\tau] \rightarrow e[\tau / \alpha]} \\
& \overline{\Delta ; \Gamma \vdash x: \Gamma(x)} \quad \overline{\Delta ; \Gamma \vdash c: \operatorname{int}} \quad \frac{\Delta ; \Gamma, x: \tau_{1} \vdash e: \tau_{2} \quad \Delta \vdash \tau_{1}}{\Delta ; \Gamma \vdash \lambda x: \tau_{1} \cdot e: \tau_{1} \rightarrow \tau_{2}} \quad \frac{\Delta, \alpha ; \Gamma \vdash e: \tau_{1}}{\Delta ; \Gamma \vdash \Lambda \alpha \cdot e: \forall \alpha \cdot \tau_{1}} \\
& \frac{\Delta ; \Gamma \vdash e_{1}: \tau_{2} \rightarrow \tau_{1} \quad \Delta ; \Gamma \vdash e_{2}: \tau_{2}}{\Delta ; \Gamma \vdash e_{1} e_{2}: \tau_{1}} \quad \frac{\Delta ; \Gamma \vdash e: \forall \alpha \cdot \tau_{1} \quad \Delta \vdash \tau_{2}}{\Delta ; \Gamma \vdash e\left[\tau_{2}\right]: \tau_{1}\left[\tau_{2} / \alpha\right]}
\end{aligned}
$$

Name: $\qquad$

$$
\begin{array}{ll}
e & ::=\ldots|\mathrm{A}(e)| \mathrm{B}(e) \mid(\text { match } e \text { with } \mathrm{A} x . e \mid \mathrm{B} x . e) \mid \text { roll }_{\tau} e \mid \text { unroll } e \\
\tau & ::=\ldots\left|\tau_{1}+\tau_{2}\right| \mu \alpha . \tau \\
v & ::=\ldots|\mathrm{A}(v)| \mathrm{B}(v) \mid \text { roll } \\
\tau
\end{array}
$$

$e \rightarrow e^{\prime}$ and $\Delta ; \Gamma \vdash e: \tau$

$$
\begin{array}{l|l}
\hline \text { match } \mathrm{A}(v) \text { with } \mathrm{A} x . e_{1} \mid \mathrm{B} y . e_{2} \rightarrow e_{1}[v / x] & \quad \text { match } \mathrm{B}(v) \text { with } \mathrm{A} x . e_{1} \mid \mathrm{B} y . e_{2} \rightarrow e_{2}[v / y]
\end{array}
$$

$$
\frac{e \rightarrow e^{\prime}}{\mathrm{A}(e) \rightarrow \mathrm{A}\left(e^{\prime}\right)} \quad \frac{e \rightarrow e^{\prime}}{\mathrm{B}(e) \rightarrow \mathrm{B}\left(e^{\prime}\right)} \quad \frac{e \rightarrow e^{\prime}}{\text { match } e \text { with } \mathrm{A} x . e_{1} \mid \mathrm{B} y . e_{2} \rightarrow \text { match } e^{\prime} \text { with } \mathrm{A} x . e_{1} \mid \mathrm{B} y \cdot e_{2}}
$$

$$
\overline{\text { unroll } \left.\text { (roll }_{\mu \alpha . \tau} v\right) \rightarrow v} \quad \frac{e \rightarrow e^{\prime}}{\operatorname{roll}_{\mu \alpha . \tau} e \rightarrow \operatorname{roll}_{\mu \alpha \tau} e^{\prime}} \quad \frac{e \rightarrow e^{\prime}}{\text { unroll } e \rightarrow \text { unroll } e^{\prime}}
$$

$$
\frac{\Delta ; \Gamma \vdash e: \tau_{1}+\tau_{2} \quad \Delta ; \Gamma, x: \tau_{1} \vdash e_{1}: \tau \quad \Delta ; \Gamma, y: \tau_{2} \vdash e_{2}: \tau}{\Delta ; \Gamma \vdash \text { match } e \text { with A } x \cdot e_{1} \mid \text { By. } e_{2}: \tau}
$$

$\frac{\Delta ; \Gamma \vdash e: \tau_{1}}{\Delta ; \Gamma \vdash \mathrm{A}(e): \tau_{1}+\tau_{2}} \quad \frac{\Delta ; \Gamma \vdash e: \tau_{2}}{\Delta ; \Gamma \vdash \mathrm{B}(e): \tau_{1}+\tau_{2}} \quad \frac{\Delta ; \Gamma \vdash e: \tau[(\mu \alpha . \tau) / \alpha]}{\Delta ; \Gamma \vdash \mathrm{roll}_{\mu \alpha . \tau} e: \mu \alpha . \tau} \quad \frac{\Delta ; \Gamma \vdash e: \mu \alpha . \tau}{\Delta ; \Gamma \vdash \text { unroll } e: \tau[(\mu \alpha . \tau) / \alpha]}$

Module Thread:

```
type t
val create : ('a -> 'b) -> 'a -> t
val join : t -> unit
```

Module Mutex:

```
type t
val create : unit -> t
val lock : t -> unit
val unlock : t -> unit
```

Module Event:

```
type 'a channel
type 'a event
val new_channel : unit -> 'a channel
val send : 'a channel -> 'a -> unit event
val receive : 'a channel -> 'a event
val choose : 'a event list -> 'a event
val wrap : 'a event -> ('a -> 'b) -> 'b event
val sync : 'a event -> 'a
```

Name: $\qquad$

1. (20 points) Assume we have a typed programming language formally defined by a small-step operational semantics and a typing judgment. Assume the appropriate Preservation and Progress Theorems hold for this language. Consider each question below separately and explain your answers briefly.
(a) Suppose we change the operational semantics by adding a new inference rule.
i. Is it possible that the Preservation Theorem is now false?
ii. Is it possible that the Progress Theorem is now false?
(b) Suppose we change the type system by adding a new inference rule.
i. Is it possible that the Preservation Theorem is now false?
ii. Is it possible that the Progress Theorem is now false?
(c) Suppose we change the operational semantics by replacing one of the inference rules with a rule that is just like it except it has some additional hypothesis.
i. Is it possible that the Preservation Theorem is now false?
ii. Is it possible that the Progress Theorem is now false?
(d) Suppose we change the type system by replacing one of the inference rules with a rule that is just like it except it has some additional hypothesis.
i. Is it possible that the Preservation Theorem is now false?
ii. Is it possible that the Progress Theorem is now false?

Name: $\qquad$
2. ( $\mathbf{1 5}$ points) Consider a typed $\lambda$-calculus with recursive types, sum types, pair types, int, and unit. Assume the language uses explicit roll and unroll coercions (not subtyping) for recursive types.
(a) Define a type t 1 for lists where each list element contains either one int or a pair of ints. Use a sum type to tag list elements to distinguish these two possibilities.
(b) Write a typed $\lambda$-calculus program of the form fix ( $\lambda$ sum:t1 $\rightarrow$ int. $\lambda l s t: \mathrm{t} 1$. $\qquad$ ) for adding up all the integers in a list of type t 1 . For example, a list holding the pair $(2,3)$ and the integer 7 would have a sum of 12 . Assume, of course, the expression language has addition.
(c) Define a type t2 for a list where list elements alternate between holding an int and a pair of ints, starting with an int. That is, the first, third, fifth, etc. elements are ints and the second, fourth, sixth elements, etc. are pairs of ints. However, the list may have any number of total elements (including 0 or an odd number). Do not use a sum type for list elements (although you still need sum types for the list itself).
(d) Write a typed $\lambda$-calculus program of the form fix ( $\lambda$ sum:t2 $\rightarrow$ int. $\lambda l s t:$ t2. $\qquad$ ) for adding up all the integers in a list of type t2. For example, a list holding the pair $(2,3)$ and the integer 7 would have a sum of 12 . Assume, of course, the expression language has addition.

Name: $\qquad$
3. ( $\mathbf{2 0}$ points) In this problem you will use CML to implement futures. Futures have this interface:

```
type 'a promise
val future : (unit -> 'a) -> 'a promise
val force : 'a promise -> 'a
```

Recall a future runs in parallel and force blocks until the result is ready. It is permissable to call force with the same promise multiple times; if the result has already been computed it is simply returned immediately.
(a) Provide an implementation of the interface above in CML. Do not use mutation. Remember to include the definition of type 'a promise.
(b) Consider an extended interface with:
val force_any : 'a promise list -> 'a
Extend your implementation to provide this function. It should block only until one of the promises in the list is ready. If more than one is ready, it can return the result of any of the ready ones.

Name: $\qquad$
4. ( $\mathbf{1 5}$ points) Consider a class-based OOP language like we did in class. Suppose it has abstract methods. Recall that a class that defines or inherits abstract methods cannot have instances unless all abstract methods are overridden.
In this problem, we consider a bad idea for a new language feature: If class $C$ inherits abstract method $m$, then $C$ 's definition can include remove $m$ to mean instances of $C$ do not have method $m$. This allows us to create instances of $C$ unless there are other abstract methods that are neither overridden nor "removed."
(a) Explain why this new feature is unsound if subclasses are subtypes. Give an example with a superclass, a subclass, and "client code" that makes an instance of the subclass. Your example should not require any concrete methods in the superclass.
(b) Explain why this new feature is unsound even if subclasses that remove methods are not subtypes of their superclasses. Give an example with a superclass, a subclass, and "client code" that makes an instance of the subclass.

Name: $\qquad$
5. ( $\mathbf{1 5}$ points) This problem considers the code below in a class-based OOP language. Assume classes A, B, C, and D have no subclasses except those shown.

```
class A {}
class B extends A {}
class C extends B {}
class D {
    int m(A x, A y) { return 1; }
    int m(A x, B y) { return 2; }
    int m(A x, C y) { return 3; }
    int m(B x, A y) { return 4; }
    int m(B x, B y) { return 5; }
    int m(B x, C y) { return 6; }
    int m(C x, A y) { return 7; }
    int m(C x, B y) { return 8; }
    int m(C x, C y) { return 9; }
    int foo(A a, C b) {
        return self.m(a,b);
    }
}
```

(a) Suppose our language has multimethods. What are the possible values that a call (new $D()$ ).foo(e2,e3) could return?
(b) Suppose our language has static overloading. What are the possible values that a call (new D()).foo(e2,e3) could return?
(c) How, if at all, do your answers change if subclasses of D might exist but subclasses of C do not?
(d) How, if at all, do your answers change if subclasses of C might exist but subclasses of D do not?

Name: $\qquad$
6. ( $\mathbf{1 5}$ points) This problem considers a typed language with support for bounded parametric polymorphism, i.e., types of the form $\forall \alpha<\tau_{1} . \tau_{2}$.
(a) The System F typing rule for type application:

$$
\frac{\Delta ; \Gamma \vdash e: \forall \alpha . \tau_{1} \quad \Delta \vdash \tau_{2}}{\Delta ; \Gamma \vdash e\left[\tau_{2}\right]: \tau_{1}\left[\tau_{2} / \alpha\right]}
$$

is no longer appropriate because (1) $e$ does not have a bounded polymorphic type and (2) $\tau_{2}$ is not checked against a bound. Replace this typing rule with a more appropriate one.
(b) Suppose our language has addition, records with mutable fields, and $e_{1} ; e_{2}$ for sequencing. Then this term type-checks:

$$
\lambda x:\left\{l_{1}: \text { int }, l_{2}: \text { int }\right\} .\left(\left(x . l_{1}:=x . l_{1}+x . l_{2}\right) ; x\right)
$$

Use bounded polymorphism to give a value $v$ that has the same run-time behavior as this term but has a much more general type. Use the syntax $\Lambda \alpha<\tau$.e to create a bounded polymorphic expression.
(c) Using the $v$ you defined in part (b), give a $\tau$ and $v_{2}$ such that $v[\tau] v_{2}$ type-checks (using the rule you defined in part (a) and the rule for function application). Choose a $v_{2}$ that takes advantage of the subtyping allowed by bounded polymorphism.
(d) What is the type of the expression ( $v[\tau] v_{2}$ ) in your answer to part (c)? You do not need to write down a typing derivation.

